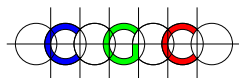
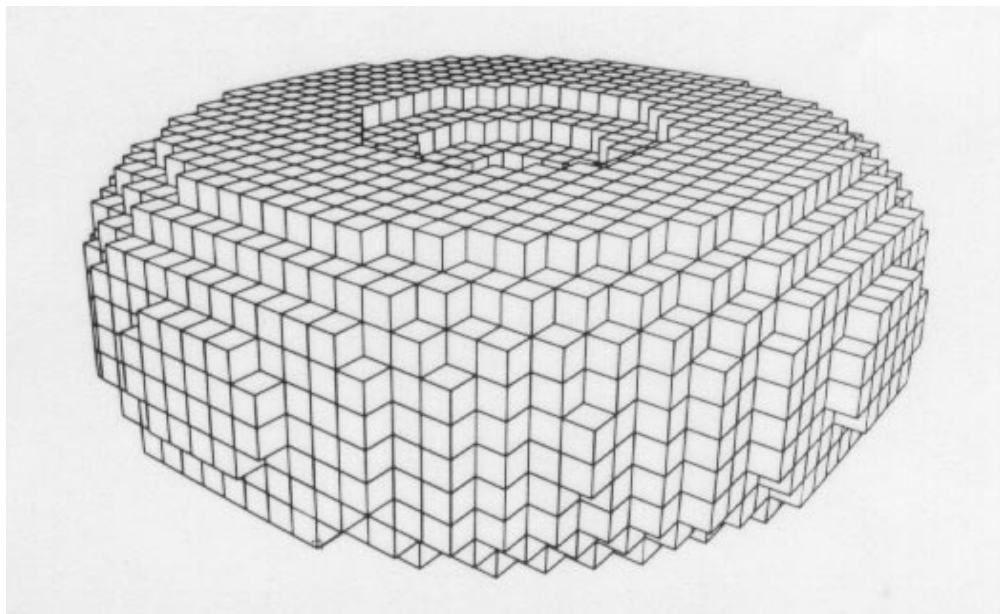


## Spatial Decomposition

- ★ Divide the space into *primitive* cells.
- ★ Represent all cells lying in the object.

### Spatial occupation enumeration

- ★ Divide the space into identical cells arranged in a fixed regular grid structures.
- ★ 3D Analog of 2D images.
- ★ Cells are often cubes and are called *voxels*.
- ★ Popular representation in volume rendering and CAT.
- ★ High storage requirement.

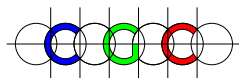
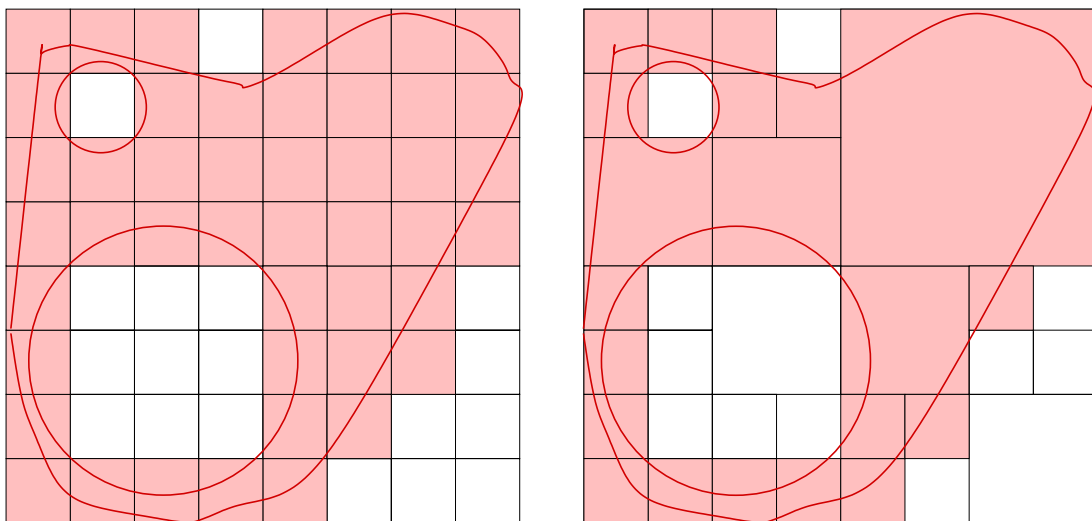


## Oct Trees

- ☆ Hierarchical representation.
- ☆ Requires much less space.
- ☆ Extension of 2D *quad tree*.

### Quad tree:

- ☆ Recursively subdivide the plane into four squares by bisecting it in both directions.
- ☆ A square is *full, empty, partially full*.
- ☆ A partially full square is further subdivided.
- ☆ Parttitioning continues until a cutoff threshold is reached.

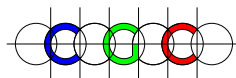
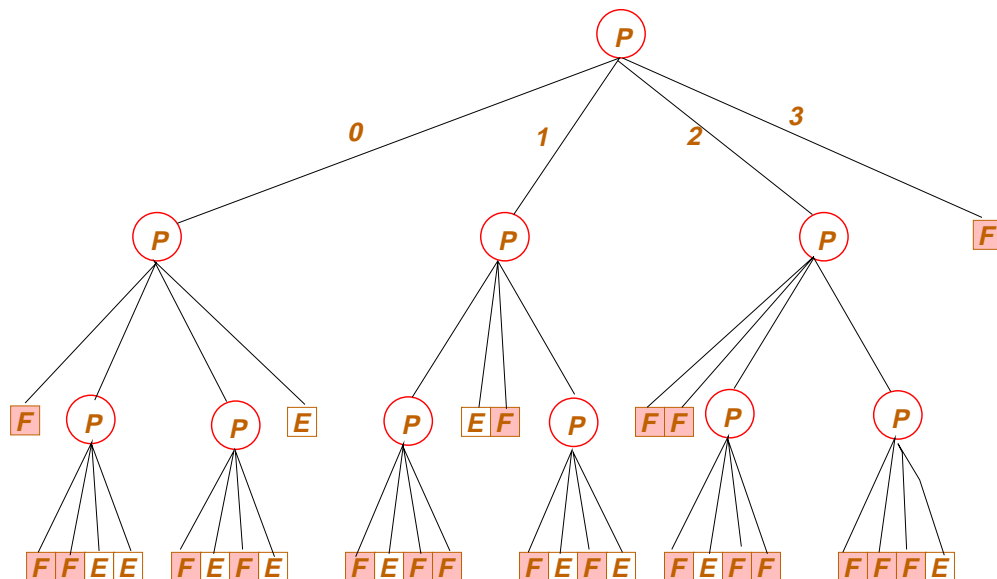


# Quad Trees

- ★ Can be represented as a 4-way tree.
- ★ Each node  $v$  represents a square  $Q_v$ 
  - If  $Q_v \subseteq P$ ,  $v$  is *black*.
  - If  $Q_v \cap P = \emptyset$ ,  $v$  is *white*.
  - Otherwise  $v$  is *gray*.
  - Gray nodes are further subdivided.

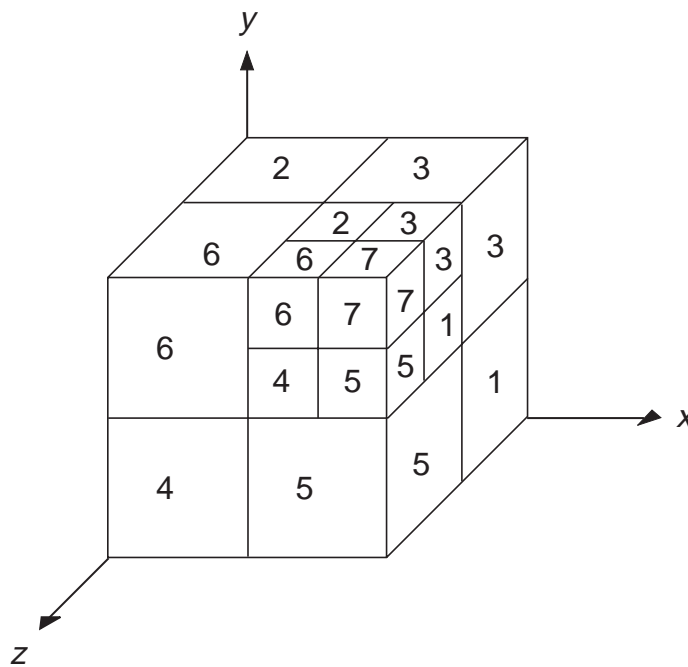
2	3
0	1

Quadrant Numbering

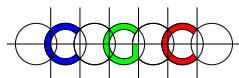


## Oct Trees

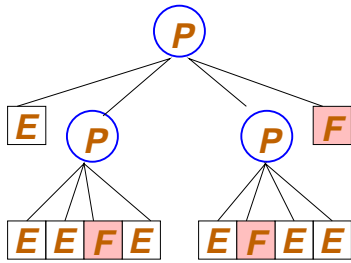
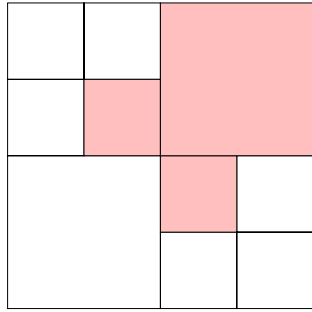
- ★ Oct tree is similar to quadtrees.
- ★ Each cube is divided into eight octants.
- ★ Useful for many operations, e.g., collision detection, ray tracing.



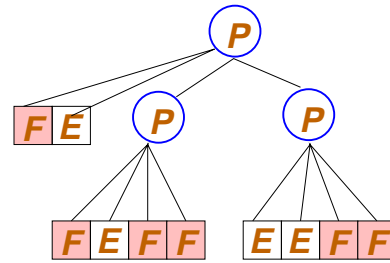
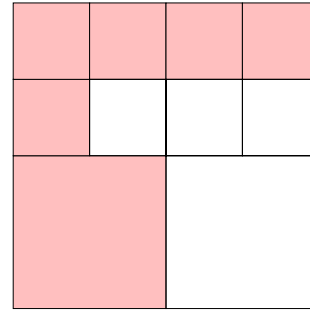
- ★ Space requirement is still large. item Sensitive to the position of the object.
- ★ Only approximate representation for nonorthogonal objects.



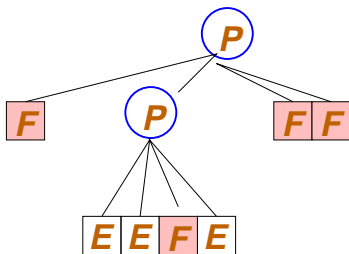
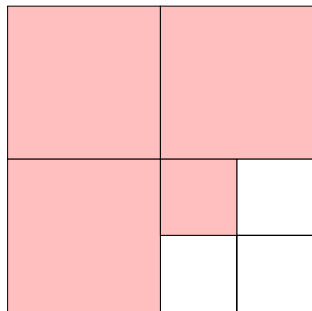
# Boolean Operations on Quad Trees



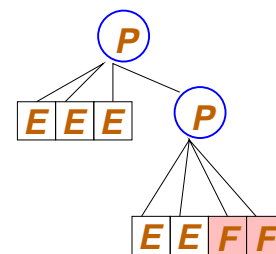
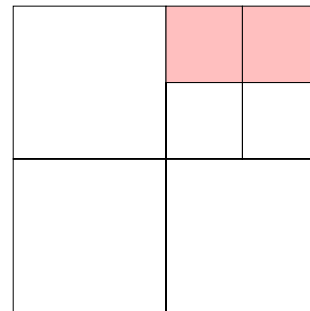
*Object S*



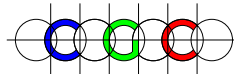
*Object T*



*Union (S, T)*

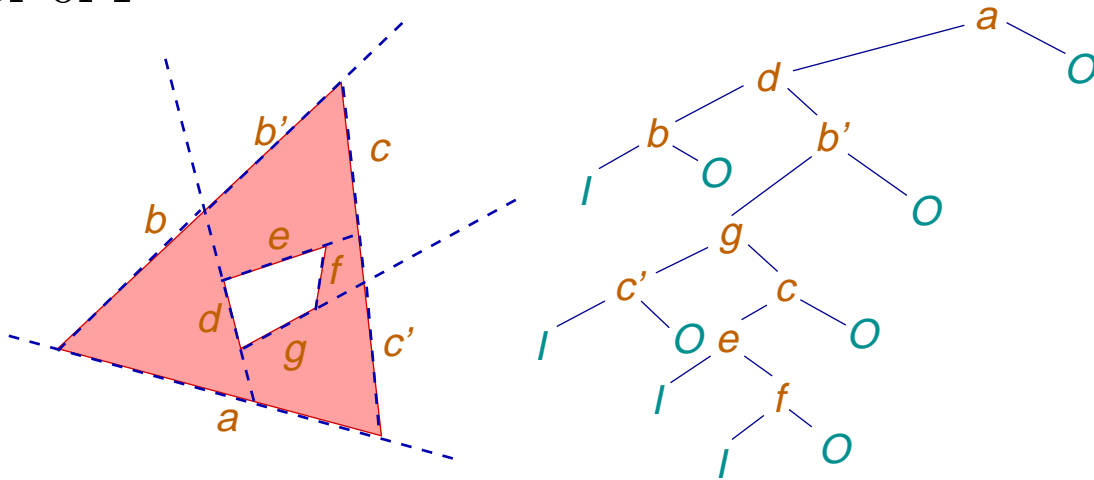


*Intersection (S, T)*



## Binary Space Partiton (BSP) Trees

$P$ : Polyhedron; Normal of each face point to exterior of  $P$



- ★ Each interior node  $v$  is associated with a plane  $\pi_v$  (containing a face of  $P$ ) and convex polytope  $Q_v$ .
  - $\pi_v^+$ : outside halfspace bounded by  $\pi_v$ .
  - $\pi_v^-$ : inside halfspace bounded by  $\pi_v$ .
- ★ The left child  $w$  of  $v$  is associated with  $Q_v \cap \pi^-$ .
- ★ If  $Q_w$  is monochromatic,  $w$  is a leaf.
- ★ The right child  $x$  of  $v$  is associated with  $Q_v \cap \pi^+$ .
- ★ If  $Q_z$  is monochromatic,  $w$  is a leaf.

