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## Announcements

- Lecture notes
- "Notes" version (incomplete) available in the morning on the day of lecture
- "Slides" version (complete) available after the lecture
- We are working on installing IBM DB2!
- Help needed
- Good learning experience
- Reminder: check CourseInfo for announcements!


## Relational data model

- A database is a collection of relations (or tables)
- Each relation has a list of attributes (or columns)
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- Set-valued attributes not allowed
- Each attribute has a domain (or type) $\qquad$
- Each relation contains a set of tuples (or rows)
- Duplicates not allowed
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- Simplicity is a virtue!
$\qquad$
Student

| SID | name | age | GPA |
| :---: | :---: | :---: | :---: |
| 142 | Bart | 10 | 2.3 |
| 123 | Milhouse | 10 | 3.1 |
| 857 | Lisa | 8 | 4.3 |
| 456 | Ralph | 8 | 2.3 |
| $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |

Course

| CID | title |
| :---: | :---: |
| CPS 216 | Advanced Database Systems |
| CPS 130 | Analysis of Algorithms |
| CPS 214 | Computer Networks |
| $\ldots$ | $\ldots$ |

Enroll
Ordering of rows doesn't matter (even though the output is always in some order)

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## Schema versus instance

- Schema(metadata)
- Specification of how data is to be structured logically
- Defined at set-up
- Rarely changes
- Instance
- Content
- Changes rapidly, but always conforms to the schema
- Compare to types and variables in a programming language


## Example

- Schema
- Student (SID integer, name string, age integer, GPA float)
- Course (CID string, title string)
- Enroll (SID integer, CID integer)
- Instance
- \{ (142, Bart, 10, 2.3 ), ( 123, Milhouse, 10, 3.1 ), ...\}
- \{ (CPS 216, Advanced Database Systems ), ...\}
- $\{(142$, CPS 216), (142, CPS 214$), \ldots\}$

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## Selection

- Input: a table $R$
- Notation: $\sigma_{p}(R)$
$-p$ is called a selection condition/predicate
- Purpose: filter rows according to some criteria $\qquad$
- Output: same columns as $R$, but only rows of $R$ that satisfy $p$ $\qquad$
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## More on selection

- Selection predicate in general can include any
$\qquad$ column of R, constants, comparisons such as $=, \leq$, etc., and Boolean connectives $\wedge, \vee$, and $\neg$
- Example: straight A students under 18 or over 21
- But you must be able to evaluate the predicate over a single row $\qquad$
- Example: student with the highest GPA?


## Projection

- Input: a table $R$
- Notation: $\pi_{L}(R)$
- $L$ is a list of columns in $R$
- Purpose: select columns to output $\qquad$
- Output: same rows, but only the columns in $L$


## Projection example

- IDs and names of all students
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## Cross product

- Input: two tables $R$ and $S$
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- Notation: $R \times S$ $\qquad$
- Purpose: pairs rows from two tables
- Output: for each row $r$ in $R$ and each row $s$ in $S$, $\qquad$ output a row $r s$ (concatenation of $r$ and $s$ )
$\qquad$



## Derived operator: join

- Input: two tables $R$ and $S$
$\qquad$
- Notation: $R \triangleright \triangleleft_{p} S$
$-p$ is called a join condition/predicate
- Purpose: related rows from two tables according to some criteria
- Output: for each row $r$ in $R$ and each row $s$ in $S$, output a row $r s$ (concatenation of $r$ and $s$ ) if $r$ and $s$ satisfy $p$
- Shorthand for


## Join example

- Info about students, plus CIDs of their courses

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## Derived operator: natural join

- Input: two tables $R$ and $S$
- Notation: $R \triangleright \triangleleft S$
- Purpose: related rows from two tables, and
- Enforce equality on all common attributes $\qquad$
- Eliminate one copy of common attributes
- Shorthand for
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## Union

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- Input: two tables $R$ and $S$ $\qquad$
- Notation: $R \cup S$
$-R$ and $S$ must have identical schema
- Output: $\qquad$
- Has the same schema as $R$ and $S$
- Contains all rows in $R$ and all rows in $S$, with $\qquad$ duplicates eliminated
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## Difference

- Input: two tables $R$ and $S$
- Notation: $R-S$
$-R$ and $S$ must have identical schema
- Output: $\qquad$
- Has the same schema as $R$ and $S$
- Contains all rows in $R$ that are not found in $S$
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## Derived operator: intersection

- Input: two tables $R$ and $S$
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- Notation: $R \cap S$
- $R$ and $S$ must have identical schema
- Output:
- Has the same schema as $R$ and $S$
- Contains all rows that are in both $R$ and $S$
- Shorthand for
- Also equivalent to


## Renaming

- Input: a table R
- Notation: $\rho_{S}(R)$, or $\rho_{S\left(A_{1}, A_{2}, \ldots\right)}(R)$
- Purpose: rename a table and/or its columns
- Output: a renamed table with the same rows as R $\qquad$
- Used to
- Avoid confusion caused by identical column names
$\qquad$
- Create identical columns names for natural joins
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| Summary of core operators |
| :--- |
| - Selection: $\sigma_{p}(R)$ |
| - Projection: $\pi_{L}(R)$ |
| - Cross product: $R \times S$ |
| - Union: $R \cup S$ |
| - Difference: $R-S$ |
| - Renaming: $\rho_{S\left(A_{1}, A_{2}, \ldots\right)}(R)$ |
| $\quad$ - Doesn't really add to expressive power |
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## Summary of derived operators

- Join: $R \triangleright \triangleleft_{p} S$
- Natural join: $R \triangleright \triangleleft S$
- Intersection: $R \cap S$
- Many more
- Semi-join, anti-semi-join, quotient, ...
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| Classification of relational operators |  |
| Monotone $\checkmark$ Non-monotone $\mathbf{x}$ |  |
| - Selection: $\sigma_{p}(R)$ | $\checkmark$ |
| - Projection: $\pi_{L}(R)$ | $\checkmark$ |
| - Cross product: $R \times S$ | $\checkmark$ |
| - Union: $R \cup S$ | $\checkmark$ |
| - Difference: $R-S$ | $\mathbf{x}$ (Not with respect to $S$ ) |
|  |  |

Why is "-" needed for highest GPA?

- Composition of monotone operators produces a monotone query
- Old output rows remain "correct" when more rows are added to the input
- Highest-GPA query is?

Why do we need core operator X ?

- Difference
- Cross product
- Union
- Selection? Projection?

Why is r.a. a good query language?

- Declarative?
- Yes, compared to older languages like CODASYL
- But operators are inherently procedural
- Simple
- A small set of core operators whose semantics are easy to grasp
- Complete?
- With respect to what?



## Turing machine?

- Relational algebra has no recursion
- Why not recursion?
- Optimization becomes undecidable
- You can always implement it at the application level
- Recursion is added to SQL nonetheless


## Next time

- How to design a relational database (and the theory behind it)
- No required reading, but for new comers to the $\qquad$ field, reading related sections in a textbook is recommended $\qquad$
- See Tentative Syllabus on course Web page

