

## Overview

- Many different ways of implementing the same logical query operator
  - Scan, sort, hash, index
- All with different performance characteristics
- Best choice depends on the situation
  - Implement all alternatives
  - Let the query optimizer choose at run-time

# Notation

- Relations: R, S
- Tuples: r, s
- Number of tuples: |R|, |S|
- Number of disk blocks: *B*(*R*), *B*(*S*)
- Number of memory blocks available: M
- Cost metric
  - Number of I/O's
  - Memory requirement

### Table scan

- Scan table *R* and process the query
  - Selection over *R*
  - Projection of *R* without duplicate elimination
- I/O's: *B*(*R*)
  - Trick for selection:
- Memory requirement: 2 (double buffering)
- Not counting the cost of writing the result out

## Nested-loop join

- $R \triangleright \triangleleft_p S$
- For each block of *R*, and for each *r* in the block: For each block of *S*, and for each *s* in the block: Output *rs* if *p* evaluates to true over *r* and *s* 
  - R is called the outer table; S is called the inner table
- I/O's:  $B(R) + |R| \cdot B(S)$
- Memory requirement: 3 (double buffering)

## Tricks for nested-loop join

• Stop early

- If the key of the inner table is being matched
- May reduce half of the I/O's
- · Block-based nested-loop join
  - Stuff memory with as much of *R* as possible, stream *S* by, and join every *S* tuple with all *R* tuples in memory

- I/O's:  $B(R) + [B(R)/(M-2)] \cdot B(S)$ 

- Or, roughly:  $B(R) \cdot B(S) / M$
- Memory requirement: M (as much as possible)

6

### External merge sort

- Pass 0: read *M* blocks of *R* at a time, sort them, and write out a level-0 run
  - There are  $\left\lceil B(R) / M \right\rceil$  level-0 sorted runs
- Pass *i*: merge (M 1) level-(i-1) runs at a time, and write out a level-*i* run
  - -(M-1) memory blocks for input, 1 to buffer output
  - # of level-*i* runs =  $\lceil$  # of level-(*i*-1) runs / (*M*-1)  $\rceil$

7

• Final pass produces 1 sorted run

Example of external merge sort • Input: 1, 7, 4, 5, 2, 8, 3, 6, 9 • Pass 0  $-1, 7, 4 \rightarrow 1, 4, 7$   $-5, 2, 8 \rightarrow 2, 5, 8$   $-9, 6, 3 \rightarrow 3, 6, 9$ • Pass 1  $-1, 4, 7+2, 5, 8 \rightarrow 1, 2, 4, 5, 7, 8$  -3, 6, 9• Pass 2 (final)  $-1, 2, 4, 5, 7, 8+3, 6, 9 \rightarrow 1, 2, 3, 4, 5, 6, 7, 8, 9$ 

### Performance of external merge sort

- Number of passes:  $\lceil \log_{M-1} \lceil B(R) / M \rceil \rceil + 1$
- I/O's
  - Multiply by  $2 \cdot B(R)$ : each pass reads the entire relation once and writes it once
  - Subtract B(R) for the final pass
  - Roughly, this is O(  $B(R) \cdot \log_M B(R)$  )
- Memory requirement: *M* (as much as possible)

## Tricks for sorting

#### · Double buffering

- Allocate an additional block for each run
- Trade-off: smaller fan-in (more passes)

#### Blocked I/O

- Instead of reading/writing one disk block at time, read/write a bunch ("cluster")
- More sequential I/O's
- Trade-off: larger cluster  $\leftrightarrow$  smaller fan-in (more passes)

#### · Replacement sort

- On average produces level-0 runs that are twice as big
- Use a priority heap: keep outputting as much as possible and making space for input

# Sort-merge join

•  $R \triangleright \triangleleft_{R.A = S.B} S$ 

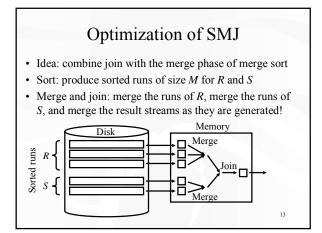
 Sort R and S by their join attributes, and then merge r, s = the first tuples in sorted R and S
 Repeat until one of R and S is exhausted: If r.A > s.B then s = next tuple in S

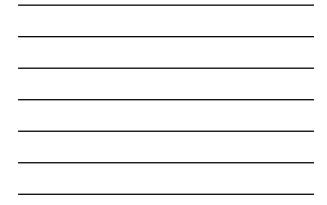
- else if r.A < s.B then r = next tuple in Relse output all matching tuples, and
- r, s = next in R and S

- I/O's: sorting + B(R) + B(S)
  - In most cases (e.g., join of key and foreign key)
  - Worst case is  $B(R) \cdot B(S)$ : everything joins

	Exar	nple	
$R:$ $\Rightarrow r_1 A = 1$ $\Rightarrow r_2 A = 3$	1	$R \rhd \triangleleft_{R.A = S.B} S:$ $r_1 s_1$ $r_2 s_3$	
$r_{3}A = 3$ $\Rightarrow r_{4}A = 5$ $\Rightarrow r_{5}A = 7$		$r_2 s_4$ $r_3 s_3$ $r_3 s_4$	
$\Rightarrow r_{5.A} = 7$ $\Rightarrow r_{6.A} = 7$ $\Rightarrow r_{7.A} = 8$	<b>-,</b> 55. <b>D</b> 0	$r_{7}s_{5}$	
			12







## Performance of two-pass SMJ

- I/O's:  $3 \cdot (B(R) + B(S))$
- Memory requirement
  - To be able to merge in one pass, we should have enough memory to accommodate one block from each run: M > B(R) / M + B(S) / M

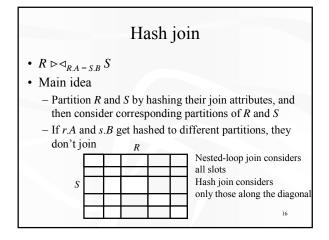
 $-M > \operatorname{sqrt}(B(R) + B(S))$ 

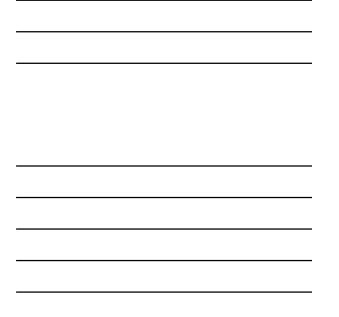
## Other sort-based algorithms

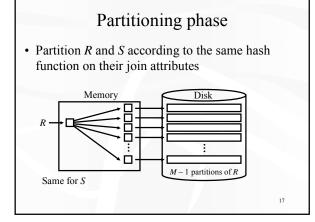
- Union, difference, intersection - More or less like SMJ
- Duplication elimination
- External merge sort
- · Eliminate duplicates in sort and merge · GROUP BY and aggregation
  - External merge sort

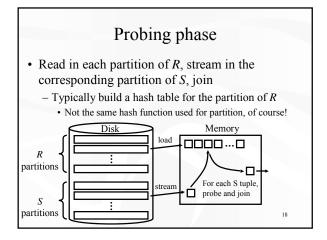
    - · Produce partial aggregate values in each run · Combine partial aggregate values during merge
    - · Partial aggregate values don't always work though

15





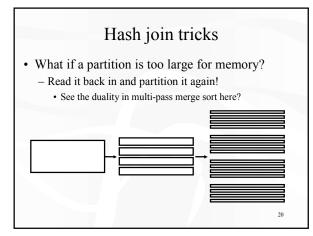


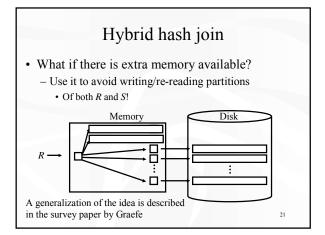




# Performance of hash join

- I/O's:  $3 \cdot (B(R) + B(S))$
- Memory requirement:
  - In the probing phase, we should have enough memory to fit one partition of  $R: M 1 \ge B(R) / (M 1)$
  - $-M > \operatorname{sqrt}(B(R))$
  - We can always pick *R* to be the smaller relation, so:
     *M* > sqrt(min(*B*(*R*), *B*(*S*))





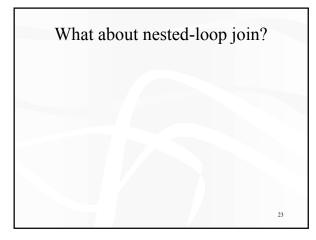


## Hash join versus SMJ

(Assuming two-pass)

• I/O's: same

- · Memory requirement: hash join is lower
  - $\operatorname{sqrt}(\min(B(R), B(S)) < \operatorname{sqrt}(B(R) + B(S))$
- Hash join wins when two relations have very different sizesOther factors
- Other factors
- Hash join performance depends on the quality of the hash
  Might not get evenly sized buckets
- SMJ can be adapted for inequality join predicates
- SMJ wins if R and/or S are already sorted
- SMJ wins if the result needs to be in sorted order



### Other hash-based algorithms

- Union, difference, intersection – More or less like hash join
- Duplicate elimination
  - Check for duplicates within each partition/bucket
- · GROUP BY and aggregation
  - Apply the hash functions to GROUP-BY attributes
  - Tuples in the same group must end up in the same partition/bucket
  - Keep a running aggregate value for each group

24

# Duality of sort and hash

- Divide-and-conquer paradigm
  - Sorting: physical division, logical combination
  - Hashing: logical division, physical combination
- Handling very large inputs
  - Sorting: multi-level merge
  - Hashing: recursive partitioning
- I/O patterns
  - Sorting: sequential write, random read (merge)
  - Hashing: random write, sequential read (partition)