

# Artificial Intelligence (CPS 270) : Homework 2

Due October 31, 2006

## 1 Bayes Nets

Consider three binary variables,  $A$ ,  $B$ , and  $C$ . Consider two Bayes net structures: (I)  $A$ , and  $B$  have no parents and have  $C$  as a common child. (II)  $C$  has no parents, but has  $A$  and  $B$  as children.

a) Provide CPTs for both Bayes nets so that case I represents a different distribution than case II. Be sure to justify that the distributions are different in a mathematically rigorous way, e.g., by demonstrating that two atomic events have different probabilities.

b) Provide CPTs for both Bayes nets so that case I and case II represent the same distribution. Be sure to justify your claim that the distributions are the same.

## 2 Bayes Nets II

In the network from Figure 14.2 from the text, compute  $P(\text{MaryCalls})$ .

## 3 Bayes Nets III

In the network from Figure 14.2 from the text, compute  $P(\text{JohnCalls} | \text{MaryCalls} = t)$ .

## 4 Bayes Nets IV

What is the complexity of computing the marginal probability of a node in a Bayes net with  $n$  binary variables and single cycle? Justify your answer by providing a variable elimination ordering and explaining the relationship between the variable elimination ordering and the total time complexity.

## 5 HMMs

Do problem 15.2.

## 6 HMMs II

Do problem 15.4.

## 7 HMMs III

Do problem 15.12. Note: This problem can be done by hand, but it is a bit tedious. You might prefer to write a small program to do this and then submit your program and its output instead of doing the calculations by hand.