

CPS 270 Alternative Search Techniques

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Overview

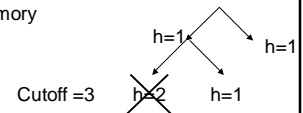
- Memory-bounded Search
- Local Search
- Searching with Incomplete Information

Memory-bounded Search: Why?

- We run out of memory before we run out of time.
- Problem: Need to remember entire search horizon
- Solution: Remember only a partial search horizon
- Issue: Maintaining optimality, completeness
- Issue: How to minimize time penalty

Attempt 1: IDA*

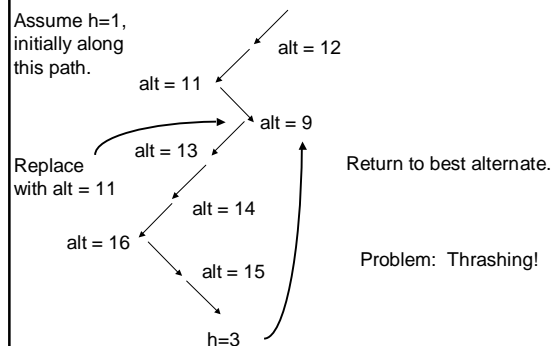
- Iterative deepening A*
- Idea: Like IDDFS, but use the f cost as a cutoff
 - Cutoff all searches with $f > 1$, then $f > 2$, $f > 3$, etc.
 - Motivation: Cut off bad-looking branches early
- Problems:
 - Excessive node regeneration
 - Can still use a lot of memory



Attempt 2: RBFS

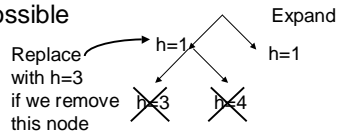
- Recursive best first search
- Objective: Linear space
- Idea: Remember best alternative
- Rewind, try alternatives if “best first” path gets too expensive
- Remember costs on the way back up

RBFS



SMA*

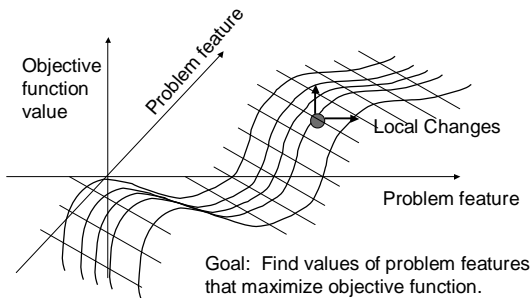
- Idea: Use all of available memory
- Discard the *worst* leaf when memory starts to run out, to make room for new leaves
- Values get backed up to parents
- Optimal if solution fits in memory
- Complete
- Thrashing still possible



Optimization

- Solution is more important than path
- Interested in minimizing or maximizing some function of the problem state
 - Find TSP tour with minimum cost
 - Optimize circuit layout
 - Schedule tasks as tightly as possible
- History of visits not worth the trouble

State Space Landscape



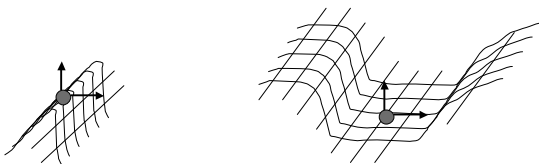
Note: This is conceptual. Often this function is not smooth.

Hill Climbing

- Idea: Try to climb up the state space landscape to find a setting of the problem features with high value.
- Approaches:
 - Steepest ascent
 - Stochastic – pick one of the good ones
 - First choice
- This is a *greedy* procedure

Limitations of Hill Climbing

- Local maxima
- Ridges – direction of ascent is at 45 degree angle to any of the local changes
- Plateaux – flat expanses



Getting Unstuck

- Random restarts
- Simulated annealing
 - Take downhill moves with small probability
 - Probability of moving downhill decreases with
 - Number of iterations
 - Steepness of downhill move
 - If system is “cooled” slowly enough, will find global optimal w.p. 1
 - Motivated by the annealing of metals and glass
 - settle into low energy configuration

Genetic Algorithms

- GAs are hot in some circles
- Biological metaphors to motivate search
- Organism is a word from a finite alphabet (organisms = states)
- Fitness of organism measures its performance on task (fitness = objective)
- Uses multiple organisms (parallel search)
- Uses mutation (random steps)

Crossover

Crossover is a distinguishing feature of GAs:

Randomly select organisms for "reproduction" in accordance with their fitness. More "fit" individuals are more likely to reproduce.

Reproduction involves crossover:

Organism 1: 110010010
 Organism 2: 000101110
 Offspring: 110011110

Is this a good idea?

- Has worked well in some examples
- Can be very brittle
 - Representations must be carefully engineered
 - Sensitive to mutation rate
 - Sensitive to details of crossover mechanism
- For the same amount of work stochastic variants of hill climbing often do better
- Hard to analyze; needs more rigorous study

Continuous Spaces

- In continuous spaces, we don't need to "probe" to find the values of local changes
- If we have a closed-form expression for our objective function, we can use the calculus
- Suppose objective function is: $f(x_1, y_1, x_2, y_2, x_3, y_3)$
- Gradient tells us direction and steepness of change

$$\nabla f = \left(\frac{\partial f}{\partial x_1}, \frac{\partial f}{\partial y_1}, \frac{\partial f}{\partial x_2}, \frac{\partial f}{\partial y_2}, \frac{\partial f}{\partial x_3}, \frac{\partial f}{\partial y_3} \right)$$

Following the Gradient



$$\mathbf{x} = (x_1, y_1, x_2, y_2, x_3, y_3)$$

$$\mathbf{x} \leftarrow \mathbf{x} + \alpha \nabla f(\mathbf{x})$$

For sufficiently small step sizes, this will converge to a region around a local optimum.

If gradient is hard to compute:

- Compute empirical gradient
- Compare with classical hill climbing

Accelerating Gradient Ascent

- Many methods for choosing step size
- Newton Raphson method for finding roots:

$$x \leftarrow x - g(x) / g'(x)$$

- Application to gradient ascent:

$$\mathbf{x} \leftarrow \mathbf{x} - \nabla f(\mathbf{x}) H_f^{-1}(\mathbf{x})$$

What's a Hessian?

$$H_f = \begin{pmatrix} \frac{\partial^2 f}{\partial x_1^2} & \cdots & \frac{\partial^2 f}{\partial x_1 \partial x_n} \\ \vdots & \ddots & \vdots \\ \frac{\partial^2 f}{\partial x_n \partial x_1} & \cdots & \frac{\partial^2 f}{\partial x_n^2} \end{pmatrix}$$

Constrained Optimization

- Don't forget about the easier cases
 - If the objective function is linear, things are easier
 - If linear constraints, solve as a linear program:
 - Maximize: $f(\mathbf{x})$
 - Subject to: $\mathbf{Ax} \leq \mathbf{b}$
 - Can be done in polynomial time
 - Can solve some quadratic programs in poly time

Searching with Partial Information

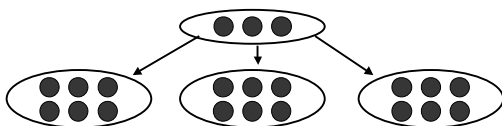
- Multiple state problems
 - Several possible initial states
- Contingency problems
 - Several possible outcomes for each action
- Exploration problems
 - Outcomes of actions not known *a priori*, must be discovered by trying them

Example

- In some situations, initial state may not be detectable
 - Suppose sensors for a nuclear reactor fail
 - Need *safe* shutdown sequence despite ignorance of some aspects of state
- This complicates search *enormously*
- In the worst case, contingent solution could cover the entire state space

State Sets

- Idea:
 - Maintain a set of candidate states
 - Each search node represents a set of states
 - Can be hard to manage if state sets get large



Searching in Unknown Environments

- What if we don't know the consequences of actions before we try them?
- Often called on-line search
- Goal: Minimize competitive ratio
 - Actual distance/distance traveled if model known
 - Problematic if actions are irreversible
 - Problematic if links can have unbounded cost

Conclusions

- There are search algorithms for almost every situation
- Many problems can be formulated as search
- While search is a very general method, it can sometimes outperform special-purpose methods