Indexing

Introduction to Databases
CompSci 316 Fall 2014
Announcements (Tue., Nov. 11)

• Project milestone #2 due Thursday
• Homework #3 sample solution posted on Sakai
• Homework #4 assigned today; due in two weeks
What are indexes for?

• Given a value, locate the record(s) with this value
  SELECT * FROM R WHERE $A = value$;
  SELECT * FROM R, S WHERE $R.A = S.B$;

• Find data by other search criteria, e.g.
  • Range search
    SELECT * FROM R WHERE $A > value$;
  • Keyword search
Dense and sparse indexes

- **Dense**: one index entry for each search key value
  - One entry may “point” to multiple records (e.g., two users named Jessica)
- **Sparse**: one index entry for each block
  - Records must be clustered according to the search key

Sparse index on *uid*

| 123 | Milhouse | 10 | 0.2 |
| 142 | Bart     | 10 | 0.9 |
| 279 | Jessica  | 10 | 0.9 |
| 345 | Martin   | 8  | 2.3 |

Dense index on *name*

| 456 | Ralph    | 8  | 0.3 |
| 512 | Nelson   | 10 | 0.4 |
| 679 | Sherri   | 10 | 0.6 |
| 697 | Terri    | 10 | 0.6 |
| 857 | Lisa     | 8  | 0.7 |
| 912 | Windel   | 8  | 0.5 |
| 997 | Jessica  | 8  | 0.5 |
Dense versus sparse indexes

- **Index size**
  - Sparse index is smaller

- **Requirement on records**
  - Records must be clustered for sparse index

- **Lookup**
  - Sparse index is smaller and may fit in memory
  - Dense index can directly tell if a record exists

- **Update**
  - Easier for sparse index
Primary and secondary indexes

• Primary index
  • Created for the primary key of a table
  • Records are usually clustered by the primary key
  • Can be sparse

• Secondary index
  • Usually dense

• SQL
  • PRIMARY KEY declaration automatically creates a primary index, UNIQUE key automatically creates a secondary index
  • Additional secondary index can be created on non-key attribute(s): 
    CREATE INDEX UserPopIndex ON User(pop);
• What if an index is still too big?
  • Put a another (sparse) index on top of that!

ISAM (Index Sequential Access Method), more or less

Example: look up 197
Updates with ISAM

Example: insert 107
Example: delete 129

- Overflow chains and empty data blocks degrade performance
  - Worst case: most records go into one long chain, so lookups require scanning all data!
B$^+$-tree

- A hierarchy of nodes with intervals
- Balanced (more or less): good performance guarantee
- Disk-based: one node per block; large fan-out

Max fan-out: 4
Sample B⁺-tree nodes

Max fan-out: 4

Non-leaf

- to keys
  - 100 ≤ k

Leaf

- to keys
  - 100 ≤ k < 120
  - 120 ≤ k < 150
  - 150 ≤ k < 180
  - 180 ≤ k

- to next leaf node in sequence

- to records with these k values;
  or, store records directly in leaves
B⁺-tree balancing properties

- Height constraint: all leaves at the same lowest level
- Fan-out constraint: all nodes at least half full (except root)

<table>
<thead>
<tr>
<th></th>
<th>Max # pointers</th>
<th>Max # keys</th>
<th>Min # active pointers</th>
<th>Min # keys</th>
</tr>
</thead>
<tbody>
<tr>
<td>Non-leaf</td>
<td>$f$</td>
<td>$f - 1$</td>
<td>$\lceil f/2 \rceil$</td>
<td>$\lceil f/2 \rceil - 1$</td>
</tr>
<tr>
<td>Root</td>
<td>$f$</td>
<td>$f - 1$</td>
<td>2</td>
<td>1</td>
</tr>
<tr>
<td>Leaf</td>
<td>$f$</td>
<td>$f - 1$</td>
<td>$\lfloor f/2 \rfloor$</td>
<td>$\lfloor f/2 \rfloor$</td>
</tr>
</tbody>
</table>
Lookups

- `SELECT * FROM R WHERE k = 179;`
- `SELECT * FROM R WHERE k = 32;`
Range query

- \texttt{SELECT * FROM R WHERE} \( k > 32 \) \texttt{AND} \( k < 179 \);

Max fan-out: 4

Look up 32...

And follow next-leaf pointers until you hit upper bound
Insertion

• Insert a record with search key value 32

Look up where the inserted key should go...

And insert it right there
Another insertion example

- Insert a record with search key value 152

Oops, node is already full!
Node splitting

Max fan-out: 4

Need to add to parent node a pointer to the newly created node

Oops, that node becomes full!
More node splitting

- In the worst case, node splitting can “propagate” all the way up to the root of the tree (not illustrated here)
  - Splitting the root introduces a new root of fan-out 2 and causes the tree to grow “up” by one level

Max fan-out: 4

Need to add to parent node a pointer to the newly created node
Deletion

• Delete a record with search key value 130

Look up the key to be deleted...

And delete it

Oops, node is too empty!

If a sibling has more than enough keys, steal one!
Stealing from a sibling

Remember to fix the key in the least common ancestor of the affected nodes.
Another deletion example

• Delete a record with search key value 179

Max fan-out: 4

Cannot steal from siblings
Then coalesce (merge) with a sibling!
Coalescing

• Deletion can “propagate” all the way up to the root of the tree (not illustrated here)
  • When the root becomes empty, the tree “shrinks” by one level

Remember to delete the appropriate key from parent

Max fan-out: 4
Performance analysis

• How many I/O’s are required for each operation?
  • \( h \), the height of the tree (more or less)
  • Plus one or two to manipulate actual records
  • Plus \( O(h) \) for reorganization (rare if \( f \) is large)
  • Minus one if we cache the root in memory

• How big is \( h \)?
  • Roughly \( \log_{\text{fan-out}} N \), where \( N \) is the number of records
  • \( B^+ \)-tree properties guarantee that fan-out is least \( f / 2 \) for all non-root nodes
  • Fan-out is typically large (in hundreds)—many keys and pointers can fit into one block
  • A 4-level \( B^+ \)-tree is enough for “typical” tables
B⁺-tree in practice

• Complex reorganization for deletion often is not implemented (e.g., Oracle)
  • Leave nodes less than half full and periodically reorganize

• Most commercial DBMS use B⁺-tree instead of hashing-based indexes because B⁺-tree handles range queries
The Halloween Problem

• Story from the early days of System R...

```sql
UPDATE Payroll
SET salary = salary * 1.1
WHERE salary >= 100000;
```

• There is a B^+-tree index on Payroll(salary)
• The update never stopped (why?)

• Solutions?
B\textsuperscript{+}-tree versus ISAM

- ISAM is more static; B\textsuperscript{+}-tree is more dynamic
- ISAM can be more compact (at least initially)
  - Fewer levels and I/O’s than B\textsuperscript{+}-tree
- Overtime, ISAM may not be balanced
  - Cannot provide guaranteed performance as B\textsuperscript{+}-tree does
B⁺-tree versus B-tree

• B-tree: why not store records (or record pointers) in non-leaf nodes?
  • These records can be accessed with fewer I/O’s
• Problems?
Beyond ISAM, B-, and $B^+$-trees

• Other tree-based indexes: R-trees and variants, GiST, etc.
  • How about binary tree?

• Hashing-based indexes: extensible hashing, linear hashing, etc.

• Text indexes: inverted-list index, suffix arrays, etc.

• Other tricks: bitmap index, bit-sliced index, etc.