# Query Processing <br> Introduction to Databases <br> CompSci 316 Fall 2016 

## Announcements (Tue., Nov. 15)

- Homework \#3 sample solution posted in Sakai
- Homework \#4 assigned today; due on 12/01
- Project milestone \#2 feedback to be emailed by this weekend


## Overview

- Many different ways of processing the same query
- Scan? Sort? Hash? Use an index?
- All have different performance characteristics and/or make different assumptions about data
- Best choice depends on the situation
- Implement all alternatives
- Let the query optimizer choose at run-time


## Notation

- Relations: $R$, $S$
- Tuples: $r$, $s$
- Number of tuples: $|R|,|S|$
- Number of disk blocks: $B(R), B(S)$
- Number of memory blocks available: $M$
- Cost metric
- Number of I/O's
- Memory requirement


## Scanning-based algorithms

> 0100111101010110101000101010 101010110001010001010100101 D01101010011101011011101000 01010010101101110101000110 10011010100111010110111010 00010100101011011101010001 0101000110100111011010101 ? 10101110101101010011010100 D1010001010100111010101101 0100101101010101101010100 31110101010010101100010110 01000101110101101110101010 1010111001011011010101011 0101000010100100011010100 010110101100101010111010010 D0101000111010010101101011 D1100010101100010100100110 1011010110111010101000101 01110110110101110110101000 21000100100011010100101011 10010010101011101001010100 001110100101011010101010014

## Table scan

- Scan table $R$ and process the query
- Selection over R
- Projection of $R$ without duplicate elimination
- I/O's: $B(R)$
- Trick for selection: stop early if it is a lookup by key
- Memory requirement: 2
- Not counting the cost of writing the result out
- Same for any algorithm!
- Maybe not needed—results may be pipelined into another operator


## Nested-loop join

$R \bowtie_{p} S$

- For each block of $R$, and for each $r$ in the block: For each block of $S$, and for each $s$ in the block: Output $r s$ if $p$ evaluates to true over $r$ and $s$
- $R$ is called the outer table; $S$ is called the inner table
- I/O's: $B(R)+|R| \cdot B(S)$
- Memory requirement: 3

Improvement: block-based nested-loop join

- For each block of $R$, for each block of $S$ :

For each $r$ in the $R$ block, for each $s$ in the $S$ block: ...

- I/O's: $B(R)+B(R) \cdot B(S)$
- Memory requirement: same as before


## More improvements

- Stop early if the key of the inner table is being matched
- Make use of available memory
- Stuff memory with as much of $R$ as possible, stream $S$ by, and join every $S$ tuple with all $R$ tuples in memory
- I/O's: $B(R)+\left\lceil\frac{B(R)}{M-2}\right\rceil \cdot B(S)$
- Or, roughly: $B(R) \cdot B(S) / M$
- Memory requirement: $M$ (as much as possible)
- Which table would you pick as the outer?


## Sorting-based algorithms



## External merge sort

Remember (internal-memory) merge sort?
Problem: sort $R$, but $R$ does not fit in memory

- Pass 0: read $M$ blocks of $R$ at a time, sort them, and write out a level-0 run
- Pass 1: merge ( $M-1$ ) level-0 runs at a time, and write out a level-1 run

- Pass 2: merge ( $M-1$ ) level-1 runs at a time, and write out a level-2 run
- Final pass produces one sorted run


## Toy example

- 3 memory blocks available; each holds one number
- Input: 1, 7, 4, 5, 2, 8, 3, 6, 9
- Pass o
- 1, 7, $4 \rightarrow 1,4,7$
- 5, 2, $8 \rightarrow 2,5,8$
- 9, 6, $3 \rightarrow 3,6,9$
- Pass 1
- 1, 4, $7+2,5,8 \rightarrow 1,2,4,5,7,8$
- 3, 6, 9
- Pass 2 (final)
- $1,2,4,5,7,8+3,6,9 \rightarrow 1,2,3,4,5,6,7,8,9$


## Analysis

- Pass 0: read $M$ blocks of $R$ at a time, sort them, and write out a level-0 run
- There are $\left\lceil\frac{B(R)}{M}\right\rceil$ level-0 sorted runs
- Pass $i$ : merge $(M-1)$ level- $(i-1)$ runs at a time, and write out a level-i run
- ( $M-1$ ) memory blocks for input, 1 to buffer output
- \# of level- $i$ runs $=\left\lceil\frac{\text { \# of level-( } i-1 \text { ) runs }}{M-1}\right\rceil$
- Final pass produces one sorted run


## Performance of external merge sort

- Number of passes: $\left\lceil\log _{M-1}\left\lceil\frac{B(R)}{M}\right\rceil\right\rceil+1$
- I/O's
- Multiply by $2 \cdot B(R)$ : each pass reads the entire relation once and writes it once
- Subtract $B(R)$ for the final pass
- Roughly, this is $O\left(B(R) \times \log _{M} B(R)\right)$
- Memory requirement: $M$ (as much as possible)


## Some tricks for sorting

- Double buffering
- Allocate an additional block for each run
- Overlap I/O with processing
- Trade-off: smaller fan-in (more passes)
- Blocked I/O
- Instead of reading/writing one disk block at time, read/write a bunch ("cluster")
- More sequential I/O’s
- Trade-off: larger cluster $\rightarrow$ smaller fan-in (more passes)


## Sort-merge join

## $R \bowtie_{R . A=S . B} S$

- Sort $R$ and $S$ by their join attributes; then merge $r, s=$ the first tuples in sorted $R$ and $S$
Repeat until one of $R$ and $S$ is exhausted:
If $r . A>s . B$ then $s=$ next tuple in $S$
else if $r . A<s . B$ then $r=$ next tuple in $R$ else output all matching tuples, and $r, s=$ next in $R$ and $S$
- I/O's: sorting $+2 B(R)+2 B(S)$
- In most cases (e.g., join of key and foreign key)
- Worst case is $B(R) \cdot B(S)$ : everything joins


## Example of merge join

$$
\begin{array}{llc}
R: & S: & R \bowtie_{R \cdot A=S \cdot B} S: \\
r_{1} \cdot A=1 & \Rightarrow s_{1} \cdot B=1 & r_{1} s_{1} \\
r_{2} \cdot A=3 & \Rightarrow s_{2} \cdot B=2 & r_{2} s_{3} \\
r_{3} \cdot A=3 & \Rightarrow s_{3} \cdot B=3 & r_{2} s_{4} \\
r_{4} \cdot A=5 & s_{4} \cdot B=3 & r_{3} s_{3} \\
r_{5} \cdot A=7 & \Rightarrow s_{5} \cdot B=8 & r_{3} s_{4} \\
r_{6} \cdot A=7 & & r_{7} s_{5}
\end{array}
$$

## Optimization of SMJ

- Idea: combine join with the (last) merge phase of merge sort
- Sort: produce sorted runs for $R$ and $S$ such that there are fewer than $M$ of them total
- Merge and join: merge the runs of $R$, merge the runs of $S$, and merge-join the result streams as they are generated!



## Performance of SMJ

- If SMJ completes in two passes:
- I/O's: $3 \cdot(B(R)+B(S))$
- Memory requirement
- We must have enough memory to accommodate one block from each run: $M>\frac{B(R)}{M}+\frac{B(S)}{M}$
- $M>\sqrt{B(R)+B(S)}$
- If SMJ cannot complete in two passes:
- Repeatedly merge to reduce the number of runs as necessary before final merge and join


## Other sort-based algorithms

- Union (set), difference, intersection
- More or less like SMJ
- Duplication elimination
- External merge sort
- Eliminate duplicates in sort and merge
- Grouping and aggregation
- External merge sort, by group-by columns
- Trick: produce "partial" aggregate values in each run, and combine them during merge
- This trick doesn't always work though
- Examples: SUM (DISTINCT ...) , MEDIAN (...)


## Hashing-based algorithms



## Hash join

$R \bowtie_{R . A=S . B} S$

- Main idea
- Partition $R$ and $S$ by hashing their join attributes, and then consider corresponding partitions of $R$ and $S$
- If $r . A$ and $s . B$ get hashed to different partitions, they don't join


Nested-loop join considers all slots

Hash join considers only those along the diagonal!

## Partitioning phase

- Partition $R$ and $S$ according to the same hash function on their join attributes



## Probing phase

- Read in each partition of $R$, stream in the corresponding partition of $S$, join
- Typically build a hash table for the partition of $R$
- Not the same hash function used for partition, of course!



## Performance of (two-pass) hash join

- If hash join completes in two passes:
- I/O's: $3 \cdot(B(R)+B(S))$
- Memory requirement:
- In the probing phase, we should have enough memory to fit one partition of $R$ : $M-1>\frac{B(R)}{M-1}$
- $M>\sqrt{B(R)}+1$
- We can always pick $R$ to be the smaller relation, so:

$$
M>\sqrt{\min (B(R), B(S))}+1
$$

## Generalizing for larger inputs

-What if a partition is too large for memory?

- Read it back in and partition it again!
- See the duality in multi-pass merge sort here?



## Hash join versus SMJ

(Assuming two-pass)

- I/O’s: same
- Memory requirement: hash join is lower
- $\sqrt{\min (B(R), B(S))}+1<\sqrt{B(R)+B(S)}$
- Hash join wins when two relations have very different sizes
- Other factors
- Hash join performance depends on the quality of the hash
- Might not get evenly sized buckets
- SMJ can be adapted for inequality join predicates
- SMJ wins if $R$ and/or $S$ are already sorted
- SMJ wins if the result needs to be in sorted order


## What about nested-loop join?

- May be best if many tuples join
- Example: non-equality joins that are not very selective
- Necessary for black-box predicates
- Example: WHERE user_defined_pred(R.A, S.B)


## Other hash-based algorithms

- Union (set), difference, intersection
- More or less like hash join
- Duplicate elimination
- Check for duplicates within each partition/bucket
- Grouping and aggregation
- Apply the hash functions to the group-by columns
- Tuples in the same group must end up in the same partition/bucket
- Keep a running aggregate value for each group
- May not always work


## Duality of sort and hash

- Divide-and-conquer paradigm
- Sorting: physical division, logical combination
- Hashing: logical division, physical combination
- Handling very large inputs
- Sorting: multi-level merge
- Hashing: recursive partitioning
- I/O patterns
- Sorting: sequential write, random read (merge)
- Hashing: random write, sequential read (partition)


## Index-based algorithms



## Selection using index

- Equality predicate: $\sigma_{A=v}(R)$
- Use an ISAM, $\mathrm{B}^{+}$-tree, or hash index on $R(A)$
- Range predicate: $\sigma_{A>v}(R)$
- Use an ordered index (e.g., ISAM or $\mathrm{B}^{+}$-tree) on $R(A)$
- Hash index is not applicable
- Indexes other than those on $R(A)$ may be useful
- Example: $\mathrm{B}^{+}$-tree index on $R(A, B)$
- How about $\mathrm{B}^{+}$-tree index on $R(B, A)$ ?


## Index versus table scan

Situations where index clearly wins:

- Index-only queries which do not require retrieving actual tuples
- Example: $\pi_{A}\left(\sigma_{A>v}(R)\right)$
- Primary index clustered according to search key
- One lookup leads to all result tuples in their entirety


## Index versus table scan (cont'd)

BUT(!):

- Consider $\sigma_{A>v}(R)$ and a secondary, non-clustered index on $R(A)$
- Need to follow pointers to get the actual result tuples
- Say that $20 \%$ of $R$ satisfies $A>v$
- Could happen even for equality predicates
- I/O's for index-based selection: lookup $+20 \%|R|$
- I/O's for scan-based selection: $B(R)$
- Table scan wins if a block contains more than 5 tuples!


## Index nested-loop join

## $R \bowtie_{R . A=S . B} S$

- Idea: use a value of $R$. $A$ to probe the index on $S(B)$
- For each block of $R$, and for each $r$ in the block:

Use the index on $S(B)$ to retrieve $s$ with $s . B=r . A$ Output $r s$

- I/O's: $B(R)+|R| \cdot($ index lookup)
- Typically, the cost of an index lookup is 2-4 I/O's
- Beats other join methods if $|R|$ is not too big
- Better pick $R$ to be the smaller relation
- Memory requirement: 3


## Zig-zag join using ordered indexes

## $R \bowtie_{R . A=S . B} S$

- Idea: use the ordering provided by the indexes on $R(A)$ and $S(B)$ to eliminate the sorting step of sort-merge join
- Use the larger key to probe the other index
- Possibly skipping many keys that don't match



## Summary of techniques

- Scan
- Selection, duplicate-preserving projection, nested-loop join
- Sort
- External merge sort, sort-merge join, union (set), difference, intersection, duplicate elimination, grouping and aggregation
- Hash
- Hash join, union (set), difference, intersection, duplicate elimination, grouping and aggregation
- Index
- Selection, index nested-loop join, zig-zag join

