

Lab 6: Bit-Coin Puzzles and Cryptographic Hash

Monday, October 22

CompSci 531, Fall 2018

Credits: Some slides taken from Bruce Maggs' CompSci 590 course in Spring 2018. Those slides are themselves based in part on Based on a Bitcoin Tutorial presentation by Joseph Bonneau, from Princeton University.

Outline

- Bitcoin and cryptocurrencies at a High Level
- Preview: Public Key Cryptography
- Review: Cryptographic Hash Functions as Proof of Work
- How bitcoin works

Bitcoin Value

Market Price (USD)

source: blockchain.info



Bitcoin and Cryptocurrencies



- Bitcoin isn't a single thing. It is a currency, a payment system, a lot of cryptographic algorithms, and software implementations.
- The goal of bitcoin is to enable “trustless” payments with low transaction costs in an “anonymous” distributed network.
- What does that mean?

A Brief History of Currency

- Two people might want to *trade* with one another.



- In which case we don't need currency.

A Brief History of Currency

- But in reality, the situation is more complicated. What if you want something someone else has, but don't have anything to trade that they want?
- Idea: a universal good, that exists in limited quantities, that can be traded for anything. Currency!
- Originally gold or silver. Today, things are a little different.

Online Purchase

amazon



Trusted Parties



VISA



Cryptocurrency Problem

- How do we accomplish the following transaction:
 - Without any trusted parties (cryptography), and
 - Without any “hard money” being moved around, while still guaranteeing that only amazon has the money afterward? (Cryptographic hash as proof of work and the blockchain).



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Preview: Public Key Cryptography

- In class tomorrow, you will dive into how to design and analyze these algorithms. For our purposes today, we just need to know what they do and guarantee.
- We want to be able to send secure message (encryption), and to be able to prove that the person who claims to have sent a message really sent it (digital signature).
- The challenge for public key cryptography is how to do this *without* having to exchange a secret key beforehand (that would be *private* key cryptography).

Preview: Public Key Cryptography

- Alice and Bob have public keys P_A , P_B and private keys S_A , S_B , which you should think of as 4,000 bits.
- *Everyone* knows the public keys (just post them “in the clear”), but only Alice knows S_A , and only Bob knows S_B . Let M be a message that Alice wants to send to Bob. She encrypts M with Bob’s public key, and then Bob decrypts with his private key.
- We want two functions, both of which are easy to compute:
 - $\text{Encrypt}(M, P)$
 - $\text{Decrypt}(M, S)$
- Such that $\text{Decrypt}(\text{Encrypt}(M, P_B), S_B) == M$

Working of RSA

Alice

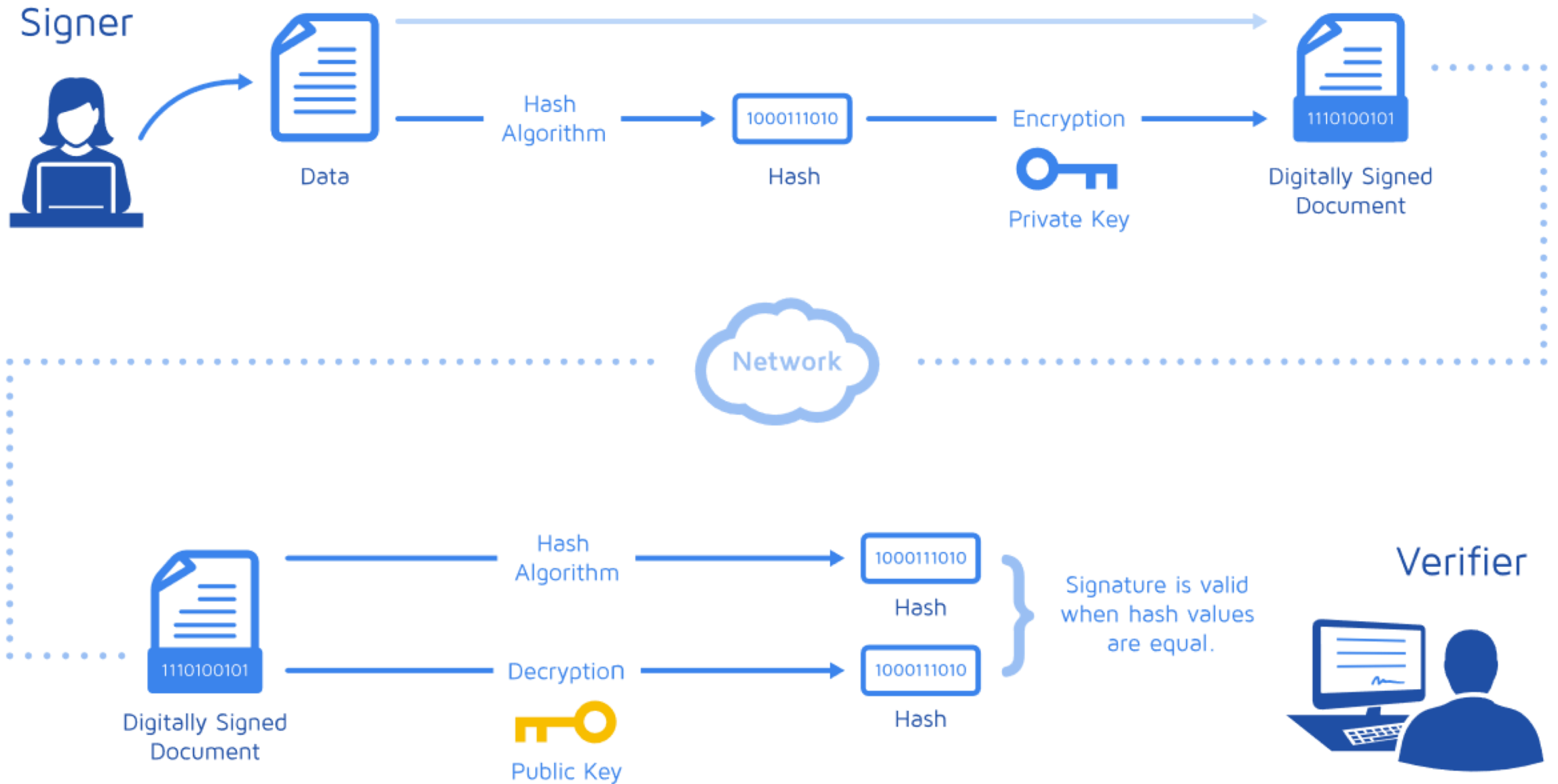


Bob



Preview: Public Key Cryptography

- We can use the same basic idea for a *digital signature* scheme. Here, if Alice wants to prove to Bob that *she* sent the message, she can sign it using her private key, and he can verify with her public key.
- We want two functions, both of which are easy to compute:
 - $\text{Sign}(M, S)$
 - $\text{Verify}(M, P)$
- Such that $\text{Verify}(\text{Sign}(M, S_A), P_A) == M$



Preview: Public Key Cryptography

- The crucial property for security is that while Encrypt/Decrypt and Sign/Verify are all highly efficient functions, computing their *inverses*, is computationally challenging (in RSA, it requires you to factor large numbers).
- These schemes will allow us to perform bitcoin transactions in a decentralized way, without the need for so many trusted entities.

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Cryptographic Hash Functions

A related idea we need is that of a cryptographic hash function, that is, a hash function that has the following properties:

1. Deterministic (same message always gives the same hash)
2. Efficient (computationally)
3. Extremely difficult to reverse engineer the input from the output.
4. Small change to input → large change in output
5. Extremely difficult to find two input with the same output.

Proof of Work

- The idea of proof of work was introduced in the 90's, originally with anti-spam applications.
- In order to allow a transaction to go through, you give give a cryptographic puzzle consisting of some input x and a cryptographic hash function $h()$. To solve the puzzle, one must find a number called a *nonce*, such that $h(x+nonce) == 0$.
- The properties of a cryptographic hash function ensure that (practically speaking), the only way to find such a nonce is brute force search.

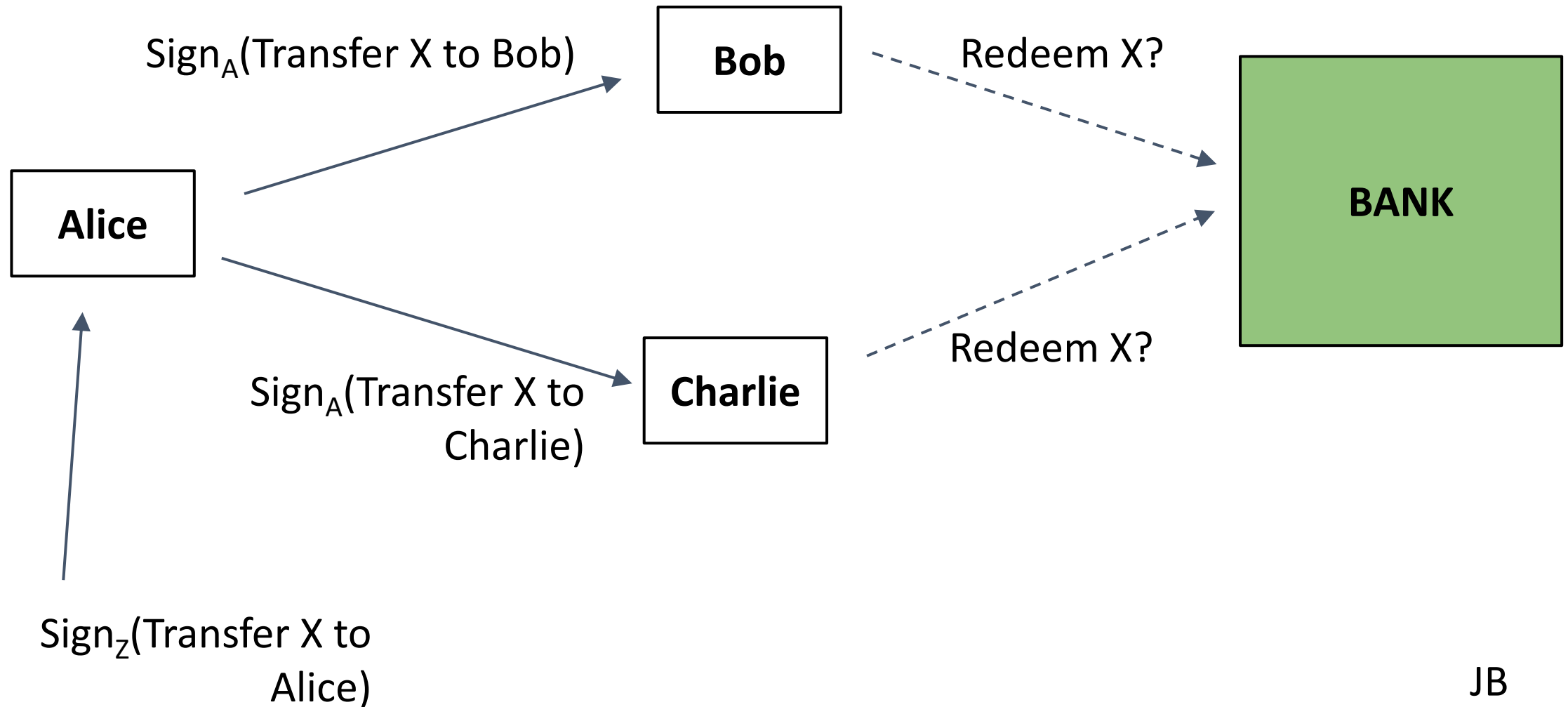
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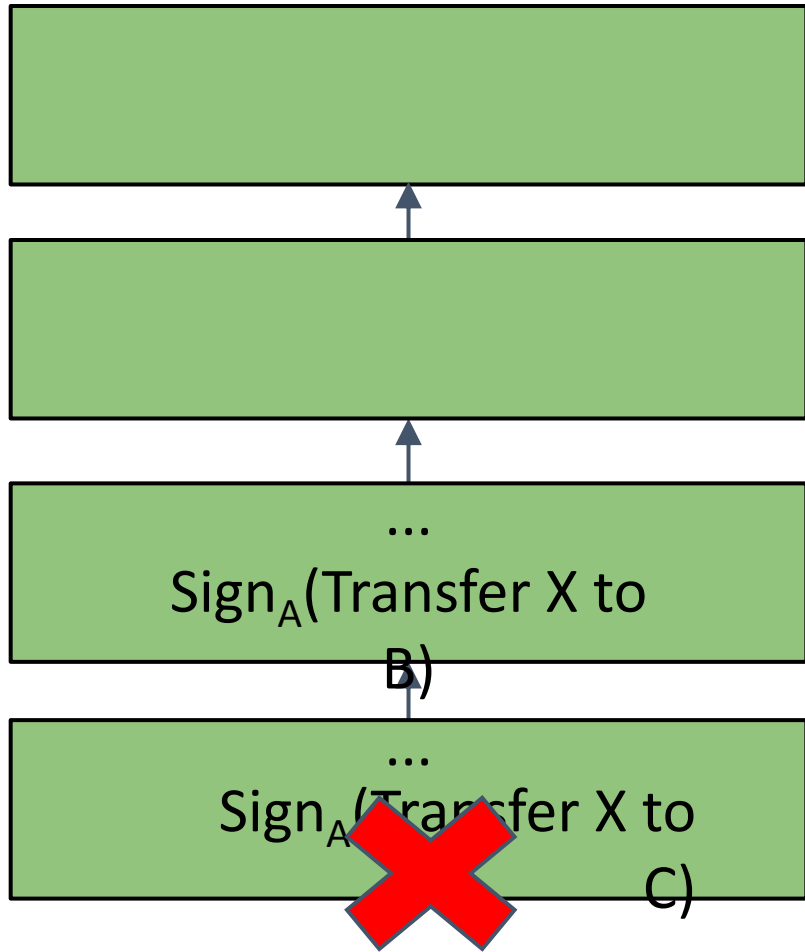
How bitcoin works (roughly)

- The generation/amount of currency is limited by the ability to (approximately) compute the inverse of hash functions as proof of work.
- Once you have a bitcoin, you can send bitcoins to someone in a transaction by digitally signing.
- But wait, what *is* a bitcoin really? And why can't I just tell multiple people that I'm sending them bitcoin at the same time?

Double spending: why ecash is hard



Solution: Maintain a global public append-only log



The block chain – a public ledger of all transactions.

(In Bitcoin, the log is extended in increments of blocks, each of which may contain thousands of transactions.)

Spending a Bitcoin

- A transaction is of the form “send these Bitcoins from address Y to address Z”
- Specific Bitcoins are described as outputs of previous transactions.
- The transaction is signed with the private key of address Y and broadcast, along with the public key of Y, to the payment network
- A transaction might also include a transaction fee.

Bitcoin mining

- Approximately every ten minutes, one lucky Bitcoin miner earns a reward for extending the block chain by one block.
- Mining reward: 12.5 Bitcoin
- Mining is the only mechanism for creating new bitcoins. The total number of Bitcoins will never exceed 21M. (Bitcoins in circulation: <https://blockchain.info/charts/total-bitcoins>)
- The rewarded miner also receives all (optional) transaction fees in the block.

How is a new block created?

- A Bitcoin miner creates a block by
 - (1) Gathering a set of pending transactions, prioritizing those with transaction fees
 - (2) Verifying the transactions
 - (3) Gives the reward and transaction fees to himself/herself
 - (4) Solving a hashing problem

How is a transaction verified?

- “send these Bitcoins from address Y to address Z”
- The miner first checks the signature using the public key for address Y.
 - compute hash of public key for Y, which should be Y
 - check signature of transaction using public key for Y
- Then the miner checks the public ledger to verify that Y hasn't already sent these Bitcoins to someone else.

The Hashing Problem

- To extend the blockchain, a miner creates a new block, which has a block header. The block header contains:
 - (1) block version number
 - (2) SHA-256 hash of previous block header
 - (3) SHA-256 hash of new transactions to include in the blockchain, including creation of reward bitcoins (e.g., 12.5 new BTC)
 - (4) current target / difficulty
 - (5) timestamp
 - (6) nonce
- Block is valid if $\text{SHA-256}(\text{SHA-256}(\text{header}))$ leads in enough zeros, as determined by current difficulty. Miner has to find the right nonce by trial and error!
- Difficulty chosen so that the time until the first miner wins is about ten minutes, on average.

bmm

Target and Difficulty

- A miner can win if his/her hash value is below the current 256-bit target, i.e., the hash value has enough leading zeros.
- Probability that a given nonce will produce a winning hash value is $\text{target} / 2^{256}$
- $\text{difficulty} = \text{difficulty_1_target} / \text{target}$, where $\text{difficulty_1_target} = 2^{224}$
- Expected time (in seconds) to mine a block = $2^{256} / (\text{target} * \text{hashrate})$
- $= \text{difficulty} * 2^{32} / \text{hashrate}$
- Difficulty was 440,779,902,286 on March 3, 2017.
- Difficulty is adjusted every 2016 blocks. If a new block is added in ten minutes, 2016 blocks are added in exactly two weeks.

Conclusion

- Bitcoin is a complicated system of currency, payment, algorithms, and software. There are abundant technical, legal, and ethical dilemmas.
- But it fundamentally rests on the power of public key cryptography and cryptographic hashing.