CPS 173 - Computational Microeconomics

Programming Assignment 1: linear and mixed integer programming (due 2/3 before class)

Please read the rules for assignments on the course web page. Contact Vince (conitzer@cs.duke.edu) with any questions.

Getting set up. (Please ask questions if you have trouble doing this; don't worry about asking a question that appears dumb. Also, you are welcome to use a different setup if you know how. The point of this exercise is to get everyone comfortable solving linear and (mixed) integer programs.)
You will need to be able to connect to godzilla.acpub.duke.edu using SSH. One way of doing this is to download the program PuTTY (search the Web for "download putty"). Once you have installed this, run it. Under "Host Name" type godzilla.acpub.duke.edu, select SSH, (if you want to, type a name under saved sessions and press "Save",) and press "Open". Use your NetID and password to log in.
Useful commands to try out:

- `pwd`: tells you the directory that you are in

- `ls`: lists the contents of the directory that you are in

- `cd name`: changes to directory "name", if such a directory exists (cd .. brings you up one level)

- `mkdir name`: creates a directory called "name"

- `rmdir name`: removes directory "name"

- `cp name1 name2`: makes a copy of file "name1" and calls it "name2"

- `rm name`: deletes (removes) file "name"

- `wget url`: gets the file at the given url into the current directory. E.g. `wget` http://www.cs.duke.edu/courses/spring10/cps173/class_example.lp

- `logout`: logs you out

Also, pressing the up arrow will take you back to commands you entered earlier. Pressing Tab will try to complete the command you are typing for you.

You probably want to make a directory for the course, e.g.

```
mkdir cps173
cd cps173
```

Now you are in the directory cps173 (use `pwd` to check this). You can make a subdirectory for this homework:

```
mkdir homework1
cd homework1
```

To get all the files relevant to this homework into this directory:

```
wget http://www.cs.duke.edu/courses/spring10/cps173/homework1.tar
tar -xvf homework1.tar
```

(A .tar file is an archive file that contains multiple files, and `tar -xvf` extracts the files.) Use `ls` to check that you have all the files.

To be able to run the GLPK solver, you need to enter the following commands (only the first time):

```
cd ~
wget http://www.cs.duke.edu/courses/spring10/cps173/glpk.conf
cp .cshrc cshrcbackup
cat glpk.conf >> .cshrc
```

After completing the above commands, logout and login again. After this, you will be able to run the GLPK solver.

The command to run the GLPK solver is:

`/afs/acpub/project/cps/bin/glpsol`

If you want to solve an LP/MIP expressed in the standard (CPLEX) LP format, type

`/afs/acpub/project/cps/bin/glpsol --cpxlp`

If you want to solve an LP/MIP expressed using the modeling language, type

`/afs/acpub/project/cps/bin/glpsol --math`

You will also need to specify the file that you want to solve, e.g.

`/afs/acpub/project/cps/bin/glpsol --math cell.mod`

and you will also need to specify a name for a file in which the output will be stored, preceded by -o. So, typing

`/afs/acpub/project/cps/bin/glpsol --math cell.mod -o cell.mod.out`

will instruct the solver to solve the LP/MIP cell.mod, and put the solution in a new file called cell.mod.out.

You will need an editor to read and edit files. One such editor is emacs. For example, typing

```
emacs cell.mod.out
```
will allow you to read the output file.

Inside emacs there are all sorts of commands. You can find emacs commands on the Web, but a few useful ones are:

- Ctrl-x Ctrl-c: exit emacs

- Ctrl-x Ctrl-s: save the file you are editing

- Ctrl-s: search the file for a string (string=sequence of characters)

- Ctrl-r: search the file backwards

- Ctrl-g: if you accidentally typed part of some emacs command and you want to get back to editing, type this

- ESC-%: allows you to replace one string with another throughout the file; for each occurrence it will check with you, press spacebar to confirm the change, n to cancel it

- Ctrl-k: delete a whole line of text

- Ctrl-Shift-_: undo

Try playing around with all of this. In particular, check that you can solve all the example files, and read the solutions. Then, solve the following questions (which refer to the examples from class).

1. (10 points.) Knapsack. Modify[1] the knapsack.lp file (*not* knapsack.mod) so that object B has weight 4.25kg, volume 3.5 liters, sells for \$3.75, and has 4.25 units available. (Do not add integrality constraints, that is, allow the solution to be fractional.) Solve it using `glpsol --cpxlp` and put the output in knapsack.out. Check that the solution makes sense.

2. (30 points.) Hot dogs. Modify the hotdogs.mod file to solve the following instance of the hot-dog problem: you now have 3 hot-dog stands (call the third one s3). The customers are now as follows:

- location: 2, #customers: 5, willing to walk: 2

- location: 5, #customers: 4, willing to walk: 1

- location: 6, #customers: 3, willing to walk: 1

- location: 8, #customers: 5, willing to walk: 1

- location: 9, #customers: 2, willing to walk: 1

---

[1]If you want to keep the original knapsack.lp file, you can do `cp knapsack.lp knapsack.original.lp` first.

- location: 11, #customers: 3, willing to walk: 6

- location: 13, #customers: 4, willing to walk: 1

- location: 15, #customers: 6, willing to walk: 7

Solve using `glpsol --math` and put the output in hotdog.out. Check that the solution makes sense.

3. (60 points.) Paintings. Write an entirely new file painting.mod (just type `emacs painting.mod`), in which you use the modeling language to solve the first (unmodified) painting problem instance from class. As always with the modeling language, you should write the file so that it is possible to modify only the `data` part of the file to solve similar problems. Your file should start with the lines:

```
set PAINTINGS;
set COLORS;
param paint_required{i in PAINTINGS, j in COLORS};
param selling_price{i in PAINTINGS};
param paint_available{j in COLORS};
var reproductions_made{i in PAINTINGS};
```

The rest is up to you to fill in. (You probably want to look at the other .mod files to give you some idea of how to do this.) Solve using `glpsol --math` and put the output in painting.out. Check that you get the right solution.

Instructions for turning in your homework: Download the files that you have modified/created, using webfiles.duke.edu, then email them to conitzer@cs.duke.edu (this time, you are expected to send six files: knapsack.lp, knapsack.out, hotdogs.mod, hotdogs.out, painting.mod, painting.out). Alternatively, you can also e-mail the files directly from `godzilla.acpub.duke.edu` (type `pine` for a simple e-mail program). You are welcome to send Vince e-mail with questions.