

CompSci 100e

Program Design and Analysis II

0
100
142
143
432
742
999

February 8, 2011

Prof. Rodger

Announcements

- What is due?
 - Assignment Prestidigitation due today!
 - Apt due Feb 15
 - Markov – out today - Assignment due Feb 17
 - Lab this week also on Markov
 - Exam Feb 22
- Always turn in APTs if you have any green! You can get partial credit.
- Each APT is 10 points. You can do extra APTs to make up the missing points.

Classwork 5

- Redo ClassScores with a Map
- BTW, We are reworking some of the APTs and now to run APT you cannot have in your class `import java.io.*`
 - That means that your Classwork 2 with classscores no longer works on the APT. You have to remove the import and the methods that use it to get it to run

Analysis – Data Structures and Algorithms

- How do we compare two programs?
- Which one will run faster? Can we tell before coding?
- Two ways:
 - Run them and see which is faster – add timings
 - Use mathematics to analyze the algorithm

Quantitative Measurements of Code

- Typically measure running time (memory?)
 - Other things to measure?
- Typically change size of input/problem to validate runtime hypotheses
 - Not the data itself, but the number of data items
 - Size of string vs. number of strings in array?
- Doubling hypothesis: What effect does doubling input size have on running time?
 - Linear: time doubles, quadratic: factor of four, ...

Different measures of complexity

- Worst case
 - Gives a good upper-bound on behavior
 - Never get worse than this
 - Drawbacks?
- Average case
 - What does average mean?
 - Averaged over all inputs? Assuming uniformly distributed random data?
 - Drawbacks?
- Best case
 - Linear search, useful?

Notations for measuring complexity

- O-notation or big-Oh: what does n look like as n approaches infinity?
 - $O(n)$ linear,
 - $O(n^2)$ quadratic
 - $O(n^3)$ cubic
 - $O(\log n)$ logarithmic
 - $O(2^n)$ exponential
- Sedgewick/Wayne uses tilde notation $\sim n^2$ means leading term is n squared

Example

```
for (int k=0; k<n; k++) {  
    for (int j=0; j<n; j++) {  
        count ++;  
    }  
}
```

What is $O()$ worst case?

Example

```
for (int k=1; k<n; k = k * 2) {  
    for (int j=0; j<m; j++) {  
        count ++;  
    }  
}
```

What is $O()$ worst case?

Example

```
for (int k=0; k<n; k++) {  
    for (int j=k; j<n; j++) {  
        count ++;  
    }  
}
```

What is $O()$ worst case?

Big-Oh, O-notation: concepts & caveats

- Count how many times “simple” statements execute
 - In the body of a loop, what matters? (e.g., another loop?)
 - Assume simple statements take a second, cost a penny,...
- In real life: cache behavior, memory behavior, swapping behavior, library gotchas, things we don't understand,...

Simplify

$$O(4n^3 + 100n + 35) =$$

$$O(3n^2 + 4n + 6) =$$

Worst case

- Given an array of integers in sorted order
- What is the worst case big-Oh time for:
 - Insert(x) - insert x in the array (must maintain the sorted property).
 - Delete(x) – remove x from the array
 - Contains(x) - is x in the array, T or F
 - Min(x) – return the minimum value in the array (don't delete it)

Multiplying and adding big-Oh

- Suppose we do a linear search then do another one
 - What is the complexity?
 - If we do 100 linear searches?
 - If we do n searches on a vector of size n?
- Binary search followed by linear search?
 - What are big-Oh complexities? Sum?
 - What about 50 binary searches? What about n searches?
- What is the number of elements in the list (1,2,2,3,3,3); (1,2,2,3,3,3,4,4,4,4)?
 - What about (1,2,2, ..., n,n,...,n)?

Helpful formulae

- We always mean base 2 unless otherwise stated
 - What is $\log(1024)$?
 - $\log(xy) = \log(x^y) = \log(2^n) = 2^{(\log n)}$
- Sums (also, use sigma notation when possible)
 - $1 + 2 + 4 + 8 + \dots + 2^k =$
 - $1 + 2 + 3 + \dots + n =$
 - $a + ar + ar^2 + \dots + ar^{n-1} = a(r^n - 1)/(r-1) = \sum_{i=0}^{n-1} ar^i$

Hashing

- Storage – hash table or hash buckets (implementation could be array, map, tree, or other structure)
- Each data item has a key
- Hash function that maps key to address in the hash table $H(\text{key}) = \text{address}$
- Best if the “key” is near the address
- “collision” if two items map to the same address

Example Hashing

- Duke's ACM Chapter wants to be able to quickly find out info about its members. Also add, delete and update members. Doesn't need members sorted.

267-89-5432 John Smith

703-25-6142 Jack Adams

319-86-2100 Betty Harris

476-82-5142 Rose Black

- Possible Hash Function: $H(\text{ssn}) = \text{last 3 digits}$
- Hash Table size is 1000, range from 0 to 999
- Will there be a collision with data above?

Bucket Hashing

Buckets 0-999 (not all buckets shown)

- Buckets hold a lot of values 0
 - Apply hash function to data. What happens? 100
- $H(267-89-5432) = 432$** 142
John Smith
- $H(703-25-6142) = 142$** 143
Jack Adams
- $H(319-86-2100) = 100$** 432
Betty Harris
- $H(476-82-5142) = 142$** 742
Rose Black
- 999

Hash Functions

- Want hash function with the fewest collisions, data distributed
- Random number Generator with seed
 - $H(\text{key})$ is $\text{random}(\text{key}) * N$
- Shift folding with 100 buckets
 - $H(123-45-6789)$ is $(123 + 45 + 6789) \bmod 100$
- Use ascii code
 - $H(\text{BANKS}) = 66 + 65 + 78 + 75 + 83 = 367$
 - Where $\text{ascii}(B) = 66$, etc.
- Java – `hashCode()`