296.3: Algorithms in the Real World

Convolutional Coding & Viterbi Decoding

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Today's lecture is based on

A Tutorial on Convolutional Coding with Viterbi Decoding

Chip Fleming
Spectrum Applications

http://home.netcom.com/~chip.f/viterbi/tutorial.html

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And now a word from my father...

"First, computer software and hardware are the most complex and rapidly developing intellectual creations of modem man."

-- p. iii, Internet and Computer Law, P. B. Maggs, J. T. Soma, and J. A. Sprowl, 2001

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Origin of Viterbi Decoding

Andrew J. Viterbi, "Error Bounds for Convolutional Codes and an Asymptotically Optimum Decoding Algorithm," *IEEE Transactions on Information Theory*, Volume IT-13, pp. 260-269, April 1967.

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Viterbi is a founder of Qualcomm.

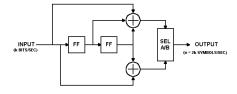
Terminology

- k number of message symbols (as before)
- n number of codeword symbols (as before)
- r rate = k/n
- m number of encoding cycles an input symbol is stored
- K number of input symbols used by encoder to compute each output symbol (decoding time exponentially dependent on K)

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Convolution Encoder output upper input followed by lower input we bit section k = 15, n = 30, $r = \frac{1}{2}$, k = 3, m = 2296.3 Page6

Encoding Example



Both flip flops set to 0 initially.

Input: 010111001010001

Output: 00 11 10 00 01 10 01 11 11 10 00 10 11 00 11

Flush encoder by clocking m = 2 times with 0 inputs.

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Viterbi Decoding Applications

- · decoding trellis-coded modulation in modems
- most common FEC technique used in space communications ($r = \frac{1}{2}$, K = 7)
- usually implemented as serial concatenated block and convolutional coding - first Reed-Solomon, then convolutional
- Turbo codes are a new parallel-concatenated convolutional coding technique

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State Transition and Output Tables

Current State	Next State, if	
	Input = 0:	Input = 1:
00	00	10
01	00	10
10	01	11
11	01	11

	Output Symbols, if	
Current State	Input = 0:	Input = 1:
00	00	11
01	11	00
10	10	01
11	01	10

State transition table

Output table

2^m rows

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State 00

State 01

State 10

On

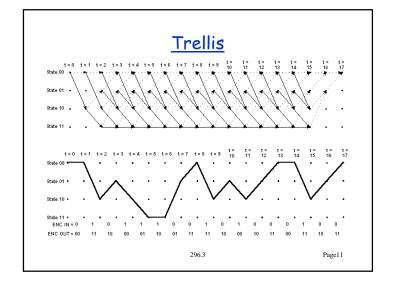
State 11

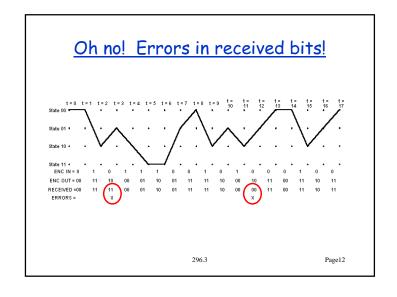
Input symbol is 1

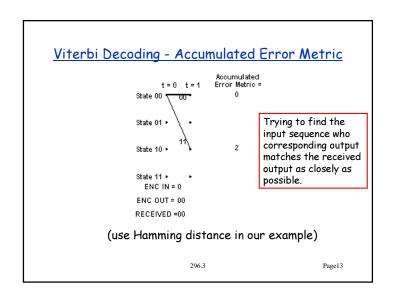
Input symbol is 0

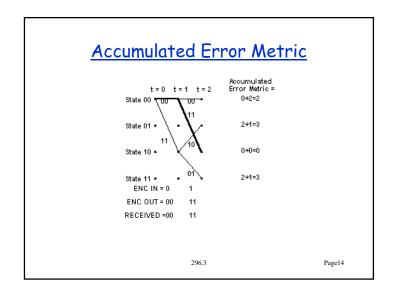
arcs labeled with output symbols

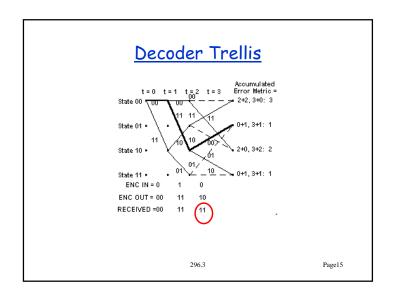
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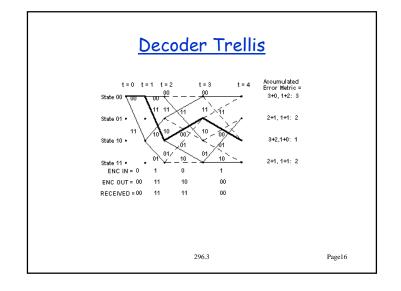


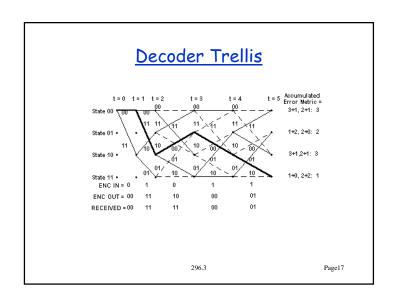


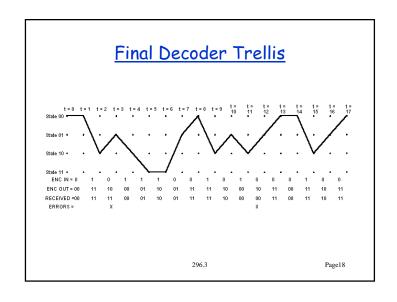


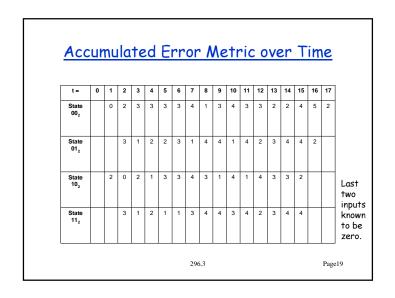


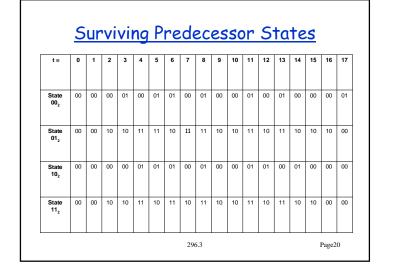


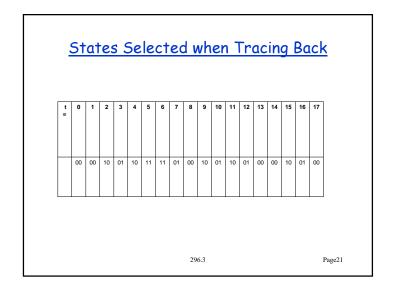


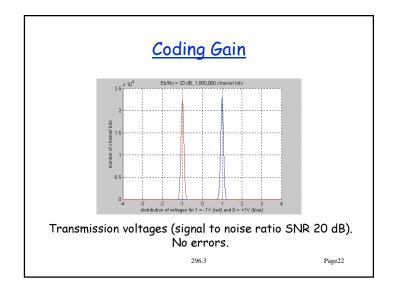


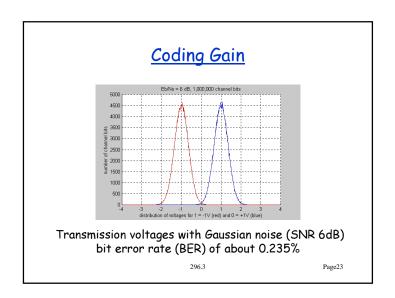


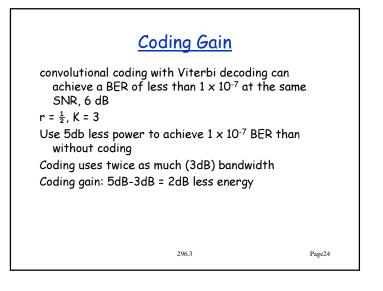












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- S. B. Wicker, Error Control Systems for Digital Communication and Storage . Englewood Cliffs, NJ: Prentice Hall, 1995.

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More References (from Fleming)

Some Papers about Convolutional Coding with Viterbi Decoding

For those interested in VLSI implementations of the Viterbi algorithm, I recommend the

- following paper and the papers to which it refers (and so on): Lin, Ming-Bo, "New Path History Management Circuits for Viterbi Decoders," *IEEE Transactions on Communications*, vol. 48, October, 2000, pp. 1605-1608. Other papers are:
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