

# Query Optimization

Introduction to Databases

CompSci 316 Spring 2019



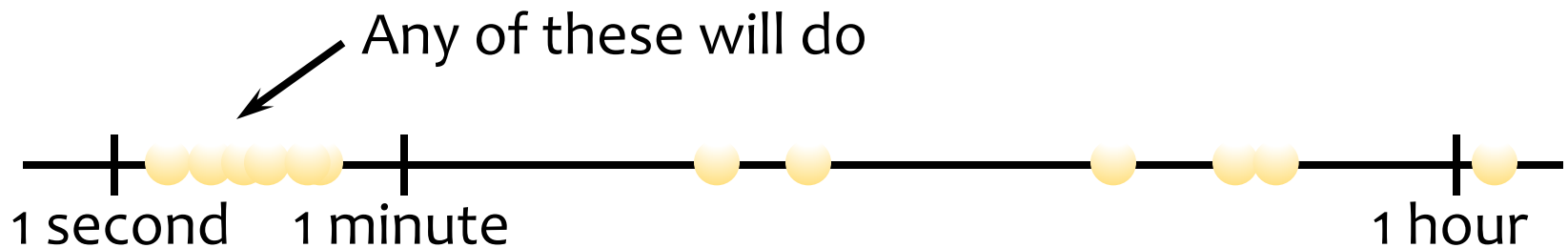
**DUKE**  
COMPUTER SCIENCE

# Announcements (Thu., Apr. 9)

- Friday 04/12: HW4-problem 1 due (gradiance)
- Monday 04/15: Hw4-problem 3 due (gradescope)

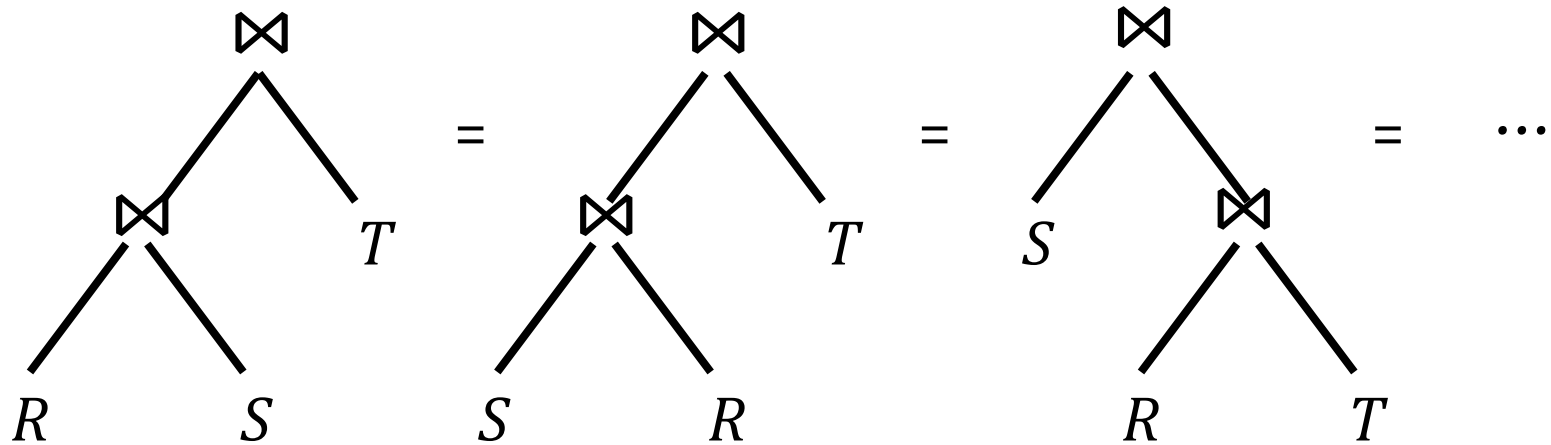
# Query optimization

- One logical plan → “best” physical plan
- Questions
  - How to enumerate possible plans
  - How to estimate costs
  - How to pick the “best” one
- Often the goal is not getting the optimum plan, but instead avoiding the horrible ones



# Plan enumeration in relational algebra

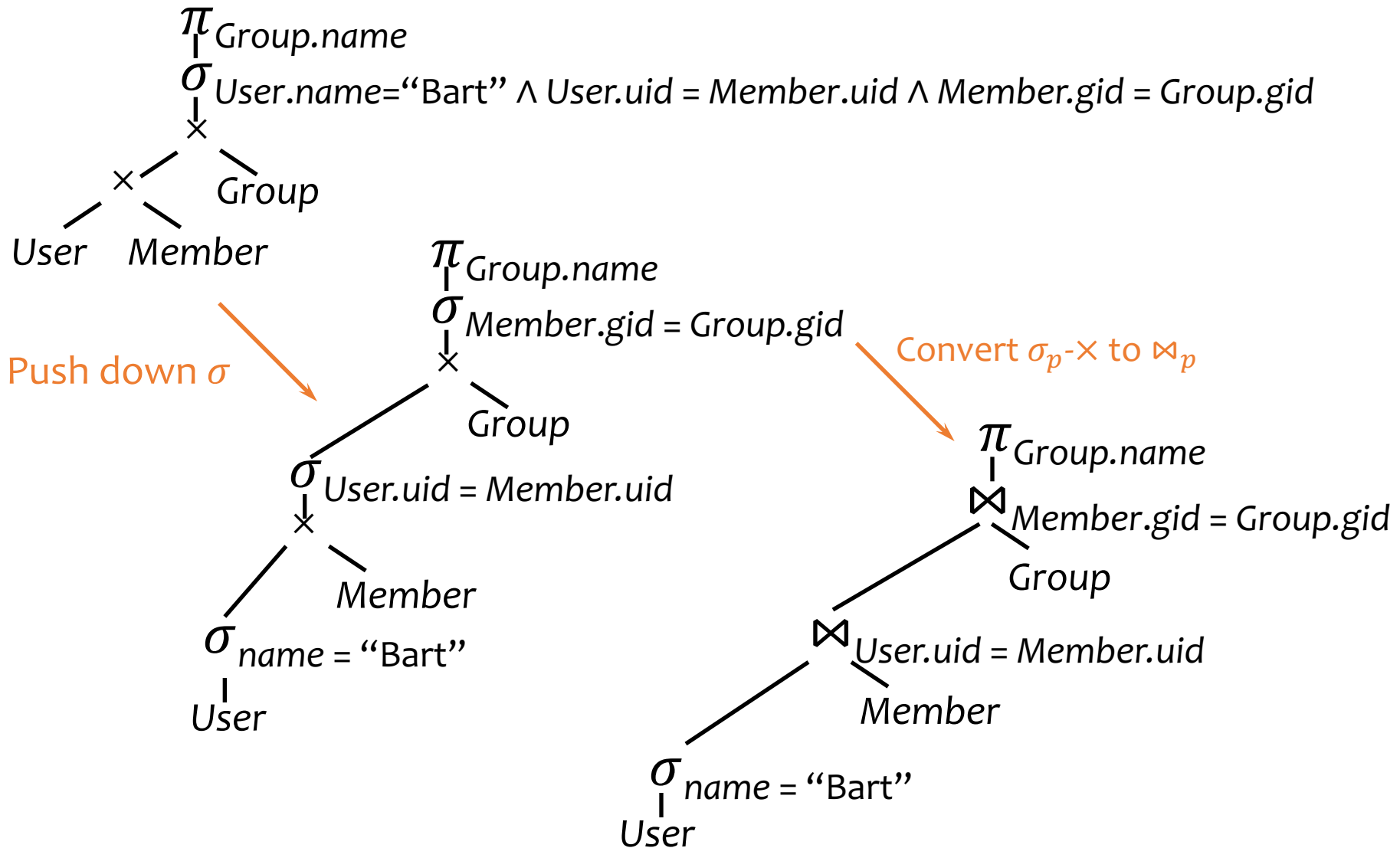
- Apply relational algebra equivalences
  - ☞ Join reordering:  $\bowtie$  and  $\ltimes$  are associative and commutative (except column ordering, but that is unimportant)



# More relational algebra equivalences

- Convert  $\sigma_p$ - $\times$  to/from  $\bowtie_p$ :  $\sigma_p(R \times S) = R \bowtie_p S$
- Merge/split  $\sigma$ 's:  $\sigma_{p_1}(\sigma_{p_2} R) = \sigma_{p_1 \wedge p_2} R$
- Merge/split  $\pi$ 's:  $\pi_{L_1}(\pi_{L_2} R) = \pi_{L_1} R$ , where  $L_1 \subseteq L_2$
- Push down/pull up  $\sigma$ :  
 $\sigma_{p \wedge p_r \wedge p_s}(R \bowtie_{p'} S) = (\sigma_{p_r} R) \bowtie_{p \wedge p'} (\sigma_{p_s} S)$ , where
  - $p_r$  is a predicate involving only  $R$  columns
  - $p_s$  is a predicate involving only  $S$  columns
  - $p$  and  $p'$  are predicates involving both  $R$  and  $S$  columns
- Push down  $\pi$ :  $\pi_L(\sigma_p R) = \pi_L(\sigma_p(\pi_{L \cup L'} R))$ , where
  - $L'$  is the set of columns referenced by  $p$  that are not in  $L$
- Many more (seemingly trivial) equivalences...
  - Can be systematically used to transform a plan to new ones

# Relational query rewrite example



# Heuristics-based query optimization

- Start with a logical plan
- Push selections/projections down as much as possible
  - Why? Reduce the size of intermediate results
  - Why not? May be expensive; maybe joins filter better
- Join smaller relations first, and avoid cross product
  - Why? Reduce the size of intermediate results
  - Why not? Size depends on join selectivity too
- Convert the transformed logical plan to a physical plan (by choosing appropriate physical operators)

# SQL query rewrite

- More complicated—subqueries and views divide a query into nested “blocks”
  - Processing each block separately forces particular join methods and join order
  - Even if the plan is optimal for each block, it may not be optimal for the entire query
- Unnest query: convert subqueries/views to joins
- ☞ We can just deal with select-project-join queries
  - Where the clean rules of relational algebra apply



# SQL query rewrite example

- `SELECT name`  
`FROM User`  
`WHERE uid = ANY (SELECT uid FROM Member);`
- `SELECT name`  
`FROM User, Member`  
`WHERE User.uid = Member.uid;`
  - Wrong—consider two Bart's, each joining two groups
- `SELECT name`  
`FROM (SELECT DISTINCT User.uid, name`  
`FROM User, Member`  
`WHERE User.uid = Member.uid);`
  - Right—assuming User.uid is a key

# Dealing with correlated subqueries

- `SELECT gid FROM Group  
WHERE name LIKE 'Springfield%'  
AND min_size > (SELECT COUNT(*) FROM Member  
WHERE Member.gid = Group.gid);`
- `SELECT gid  
FROM Group, (SELECT gid, COUNT(*) AS cnt  
FROM Member GROUP BY gid) t  
WHERE t.gid = Group.gid AND min_size > t.cnt  
AND name LIKE 'Springfield%';`
  - New subquery is inefficient (it computes the size for every group)
  - Suppose a group is empty?

# “Magic” decorrelation

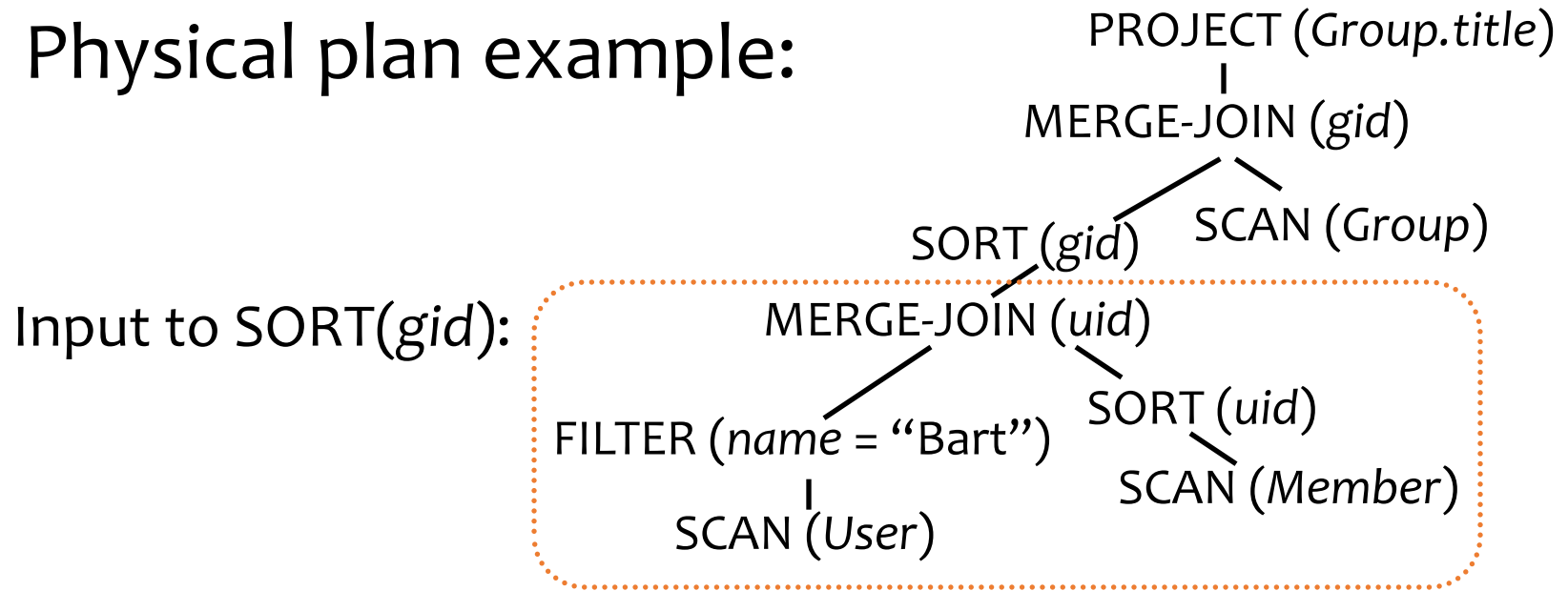
- `SELECT gid FROM Group`  
`WHERE name LIKE 'Springfield%'`  
`AND min_size > (SELECT COUNT(*) FROM Member`  
`WHERE Member.gid = Group.gid);`
- `WITH Supp_Group AS` *Process the outer query without the subquery*  
`(SELECT * FROM Group WHERE name LIKE 'Springfield%'),`  
  
`Magic AS` *Collect bindings*  
`(SELECT DISTINCT gid FROM Supp_Group),`  
  
`DS AS` *Evaluate the subquery with bindings*  
`((SELECT Group.gid, COUNT(*) AS cnt`  
`FROM Magic, Member WHERE Magic.gid = Member.gid`  
`GROUP BY Member.gid) UNION`  
`(SELECT gid, 0 AS cnt`  
`FROM Magic WHERE gid NOT IN (SELECT gid FROM Member)))`  
  
`SELECT Supp_Group.gid FROM Supp_Group, DS`  
`WHERE Supp_Group.gid = DS.gid`  
`AND min_size > DS.cnt;` *Finally, refine the outer query*

# Heuristics- vs. cost-based optimization

- **Heuristics-based optimization**
  - Apply heuristics to rewrite plans into cheaper ones
- **Cost-based optimization**
  - **Rewrite** logical plan to combine “blocks” as much as possible
  - **Optimize** query block by block
    - Enumerate logical plans (already covered)
    - Estimate the cost of plans
    - Pick a plan with acceptable cost
  - Focus: select-project-join blocks

# Cost estimation

Physical plan example:



- We have: cost estimation for each operator
  - Example: SORT(*gid*) takes  $O(B(\text{input}) \times \log_M B(\text{input}))$ 
    - But what is  $B(\text{input})$ ?
- We need: **size of intermediate results**

# Cardinality estimation



# Selections with equality predicates

- $Q: \sigma_{A=v} R$
- Suppose the following information is available
  - Size of  $R$ :  $|R|$
  - Number of distinct  $A$  values in  $R$ :  $|\pi_A R|$
- Assumptions
  - Values of  $A$  are uniformly distributed in  $R$
  - Values of  $v$  in  $Q$  are uniformly distributed over all  $R.A$  values
- $|Q| \approx |R| / |\pi_A R|$ 
  - Selectivity factor of  $(A = v)$  is  $1 / |\pi_A R|$

# Conjunctive predicates

- $Q: \sigma_{A=u \wedge B=v} R$
- Additional assumptions
  - $(A = u)$  and  $(B = v)$  are independent
    - Counterexample: major and advisor
  - No “over”-selection
    - Counterexample:  $A$  is the key
- $|Q| \approx \frac{|R|}{|\pi_A R| \cdot |\pi_B R|}$ 
  - Reduce total size by all selectivity factors



# Negated and disjunctive predicates

- $Q: \sigma_{A \neq v} R$ 
  - $|Q| \approx |R| \cdot \left(1 - \frac{1}{|\pi_A R|}\right)$ 
    - Selectivity factor of  $\neg p$  is  $(1 - \text{selectivity factor of } p)$
- $Q: \sigma_{A=u \vee B=v} R$ 
  - $|Q| \approx |R| \cdot \left(\frac{1}{|\pi_A R|} + \frac{1}{|\pi_B R|}\right)?$ 
    - No! Tuples satisfying  $(A = u)$  and  $(B = v)$  are counted twice
  - $|Q| \approx |R| \cdot \left(\frac{1}{|\pi_A R|} + \frac{1}{|\pi_B R|} - \frac{1}{|\pi_A R| |\pi_B R|}\right)$ 
    - Inclusion-exclusion principle

# Range predicates

- $Q: \sigma_{A > v} R$
- Not enough information!
  - Just pick, say,  $|Q| \approx |R| \cdot 1/3$
- With more information
  - Largest R.A value:  $\text{high}(R.A)$
  - Smallest R.A value:  $\text{low}(R.A)$
  - $|Q| \approx |R| \cdot \frac{\text{high}(R.A) - v}{\text{high}(R.A) - \text{low}(R.A)}$
  - In practice: sometimes the **second** highest and lowest are used instead
    - The highest and the lowest are often used by inexperienced database designer to represent invalid values!

# Two-way equi-join

- $Q: R(A, B) \bowtie S(A, C)$
- Assumption: **containment of value sets**
  - Every tuple in the “smaller” relation (one with fewer distinct values for the join attribute) joins with some tuple in the other relation
  - That is, if  $|\pi_A R| \leq |\pi_A S|$  then  $\pi_A R \subseteq \pi_A S$
  - Certainly not true in general
  - But holds in the common case of foreign key joins
- $|Q| \approx \frac{|R| \cdot |S|}{\max(|\pi_A R|, |\pi_A S|)}$ 
  - Selectivity factor of  $R.A = S.A$  is  $1 / \max(|\pi_A R|, |\pi_A S|)$

# Multiway equi-join

- $Q: R(A, B) \bowtie S(B, C) \bowtie T(C, D)$
- What is the number of distinct  $C$  values in the join of  $R$  and  $S$ ?
- Assumption: **preservation of value sets**
  - A non-join attribute does not lose values from its set of possible values
  - That is, if  $A$  is in  $R$  but not  $S$ , then  $\pi_A(R \bowtie S) = \pi_A R$
  - Certainly not true in general
  - But holds in the common case of foreign key joins (for value sets from the referencing table)

# Multiway equi-join (cont'd)

- $Q: R(A, B) \bowtie S(B, C) \bowtie T(C, D)$
- Start with the product of relation sizes
  - $|R| \cdot |S| \cdot |T|$
- Reduce the total size by the selectivity factor of each join predicate
  - $R.B = S.B: \frac{1}{\max(|\pi_B R|, |\pi_B S|)}$
  - $S.C = T.C: \frac{1}{\max(|\pi_C S|, |\pi_C T|)}$
  - $|Q| \approx \frac{|R| \cdot |S| \cdot |T|}{\max(|\pi_B R|, |\pi_B S|) \cdot \max(|\pi_C S|, |\pi_C T|)}$

# Cost estimation: summary

- Using similar ideas, we can estimate the size of projection, duplicate elimination, union, difference, aggregation (with grouping)
- Lots of assumptions and very rough estimation
  - Accurate estimate is not needed
  - Maybe okay if we overestimate or underestimate consistently
  - May lead to very nasty optimizer “hints”

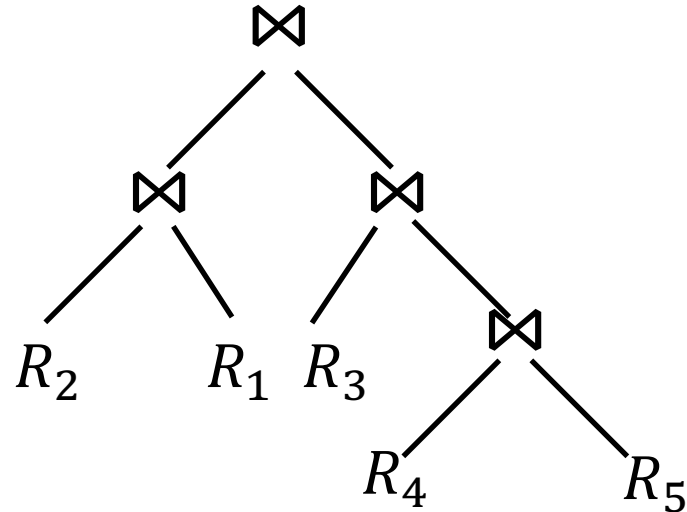
```
SELECT * FROM User WHERE pop > 0.9;  
SELECT * FROM User WHERE pop > 0.9 AND pop > 0.9;
```
- Not covered: better estimation using histograms

# Search strategy



# Search space

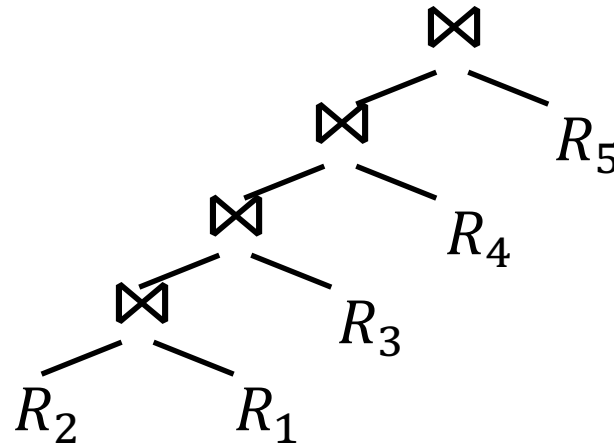
- Huge!
- “Bushy” plan example:



- Just considering different join orders, there are  $\frac{(2n-2)!}{(n-1)!}$  bushy plans for  $R_1 \bowtie \dots \bowtie R_n$ 
  - 30240 for  $n = 6$
- And there are more if we consider:
  - Multiway joins
  - Different join methods
  - Placement of selection and projection operators



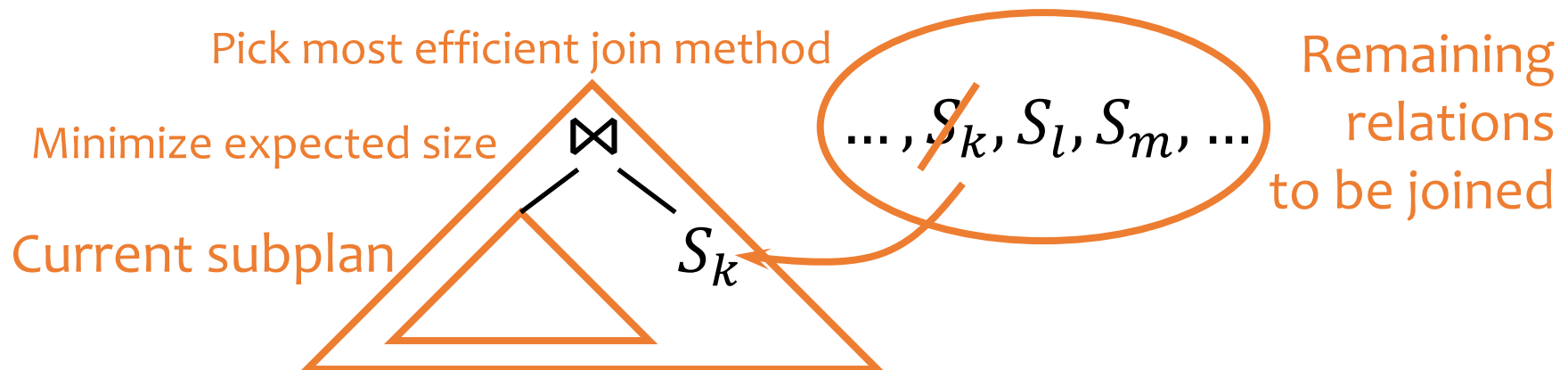
# Left-deep plans



- Heuristic: consider only “**left-deep**” plans, in which only the left child can be a join
  - Tend to be better than plans of other shapes, because many join algorithms scan inner (right) relation multiple times—you will not want it to be a complex subtree
- How many left-deep plans are there for  $R_1 \bowtie \dots \bowtie R_n$ ?
  - Significantly fewer, but still lots— **$n!$**  (720 for  $n = 6$ )

# A greedy algorithm

- $S_1, \dots, S_n$ 
  - Say selections have been pushed down; i.e.,  $S_i = \sigma_p(R_i)$
- Start with the pair  $S_i, S_j$  with the smallest estimated size for  $S_i \bowtie S_j$
- Repeat until no relation is left:  
Pick  $S_k$  from the remaining relations such that the join of  $S_k$  and the current result yields an intermediate result of the smallest size



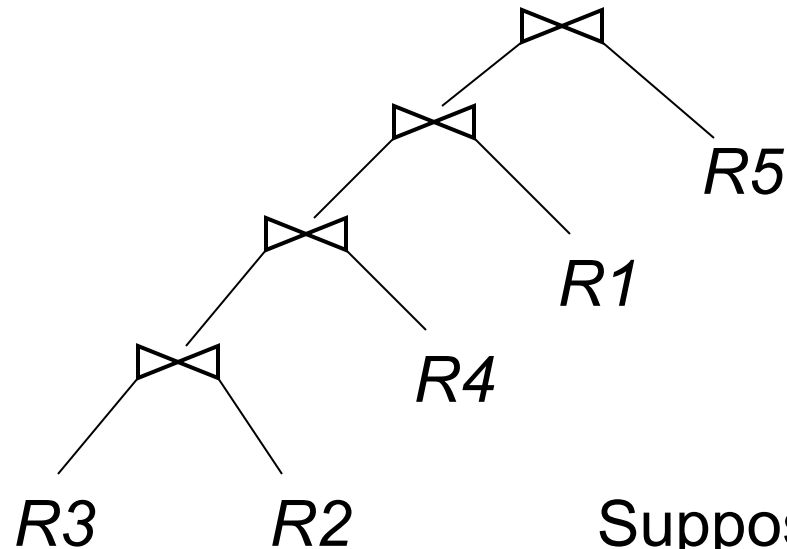
# Selinger's algorithm: A dynamic programming approach

Optimal for “whole” made up from  
optimal for “parts”

# Principle of Optimality

Query:  $R1 \bowtie R2 \bowtie R3 \bowtie R4 \bowtie R5$

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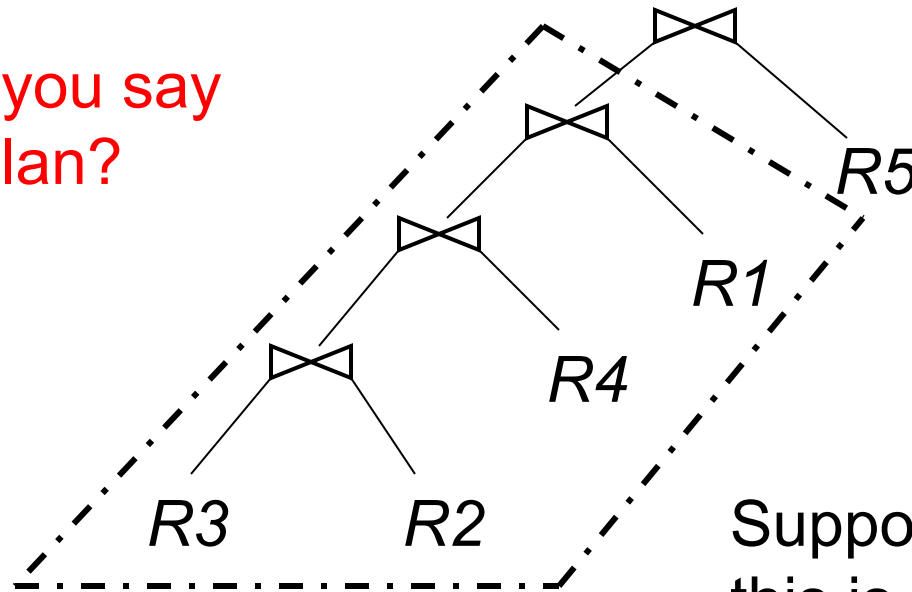
Suppose,  
this is an Optimal Plan  
for joining  $R1 \dots R5$ :

# Principle of Optimality

Query:  $R1 \bowtie R2 \bowtie R3 \bowtie R4 \bowtie R5$

---

Then, what can you say  
about this sub-plan?



This has to be the  
optimal plan for joining  $R3, R2, R4, R1$

Suppose,  
this is an Optimal Plan  
for joining  $R1...R5$ :

# Principle of Optimality

Query:  $R1 \bowtie R2 \bowtie R3 \bowtie R4 \bowtie R5$

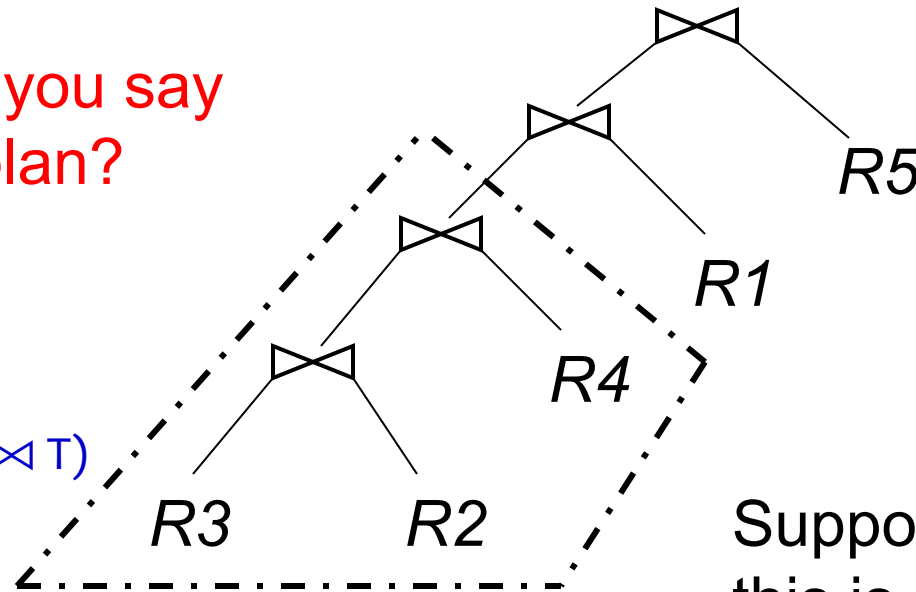
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Then, what can you say  
about this sub-plan?

We are using the  
associativity and  
commutativity of joins

$$(R \bowtie S) \bowtie T = R \bowtie (S \bowtie T)$$

$$R \bowtie S = S \bowtie R$$



This has to be the  
optimal plan for joining  $R3, R2, R4$

Suppose,  
this is an Optimal Plan  
for joining  $R1...R5$ :

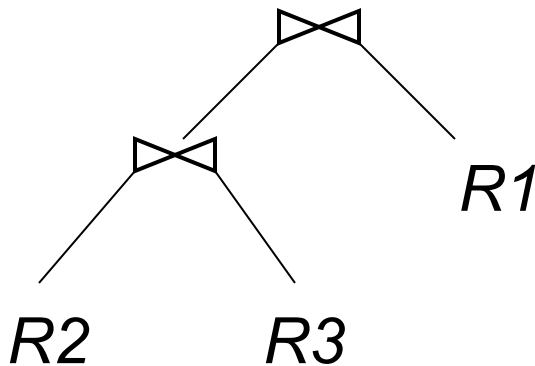
# Exploiting Principle of Optimality

Query:  $R1 \bowtie R2 \bowtie \dots \bowtie Rn$

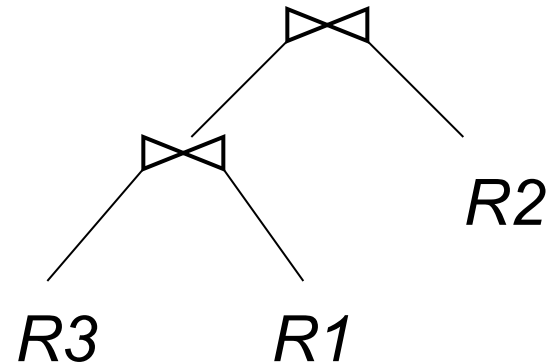
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Both are giving the same result

$R2 \bowtie R3 \bowtie R1 = R3 \bowtie R1 \bowtie R2$



Optimal  
for joining  $R1, R2, R3$



Sub-Optimal  
for joining  $R1, R2, R3$

# Selinger Algorithm:

$\text{OPT} ( \{ R1, R2, R3 \} ):$

Min

$\text{OPT} ( \{ R1, R2 \} ) + \text{cost-to-join} ( \{ R1, R2 \}, \{ R3 \} )$

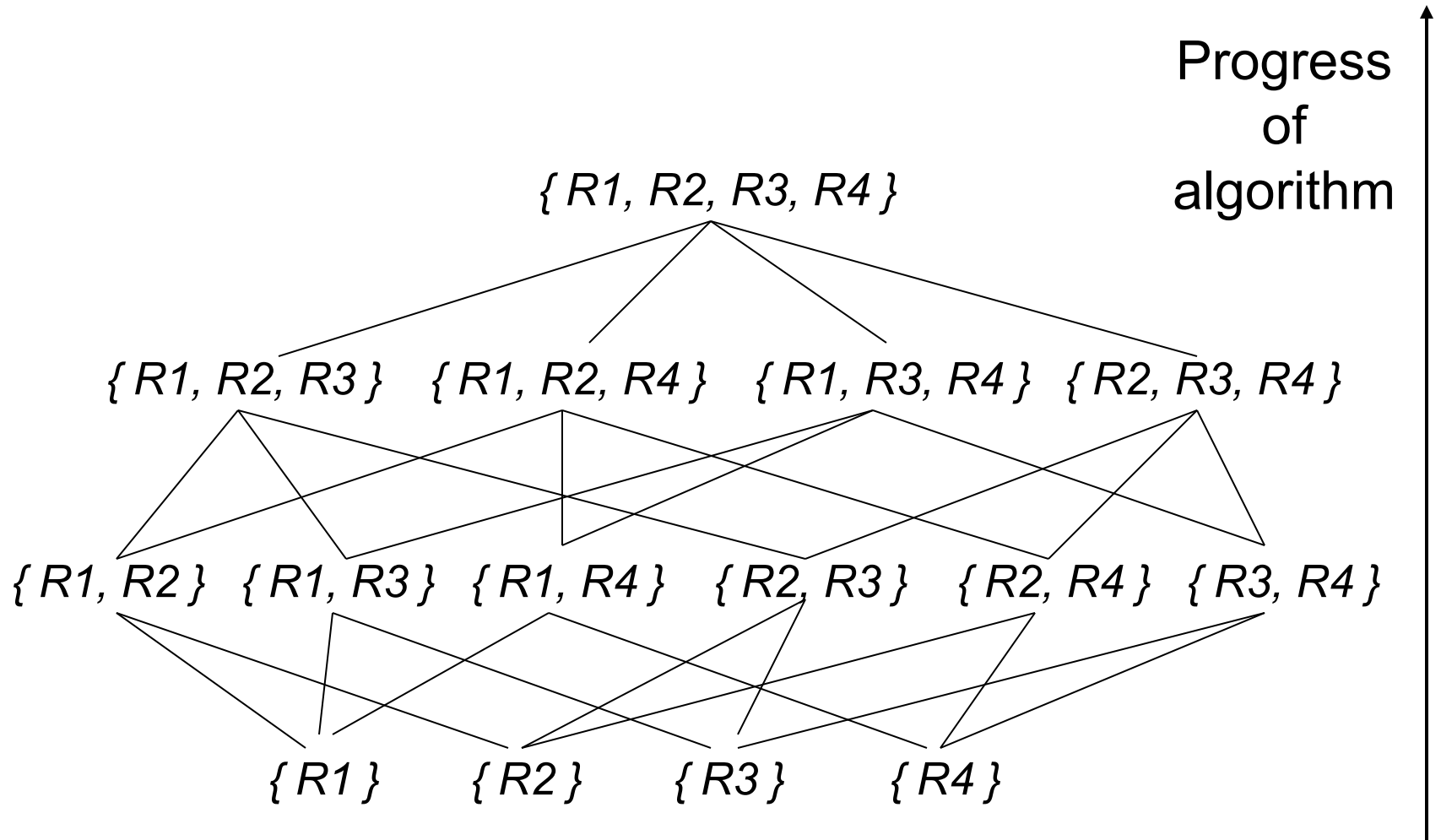
$\text{OPT} ( \{ R2, R3 \} ) + \text{cost-to-join} ( \{ R2, R3 \}, \{ R1 \} )$

$\text{OPT} ( \{ R1, R3 \} ) + \text{cost-to-join} ( \{ R1, R3 \}, \{ R2 \} )$



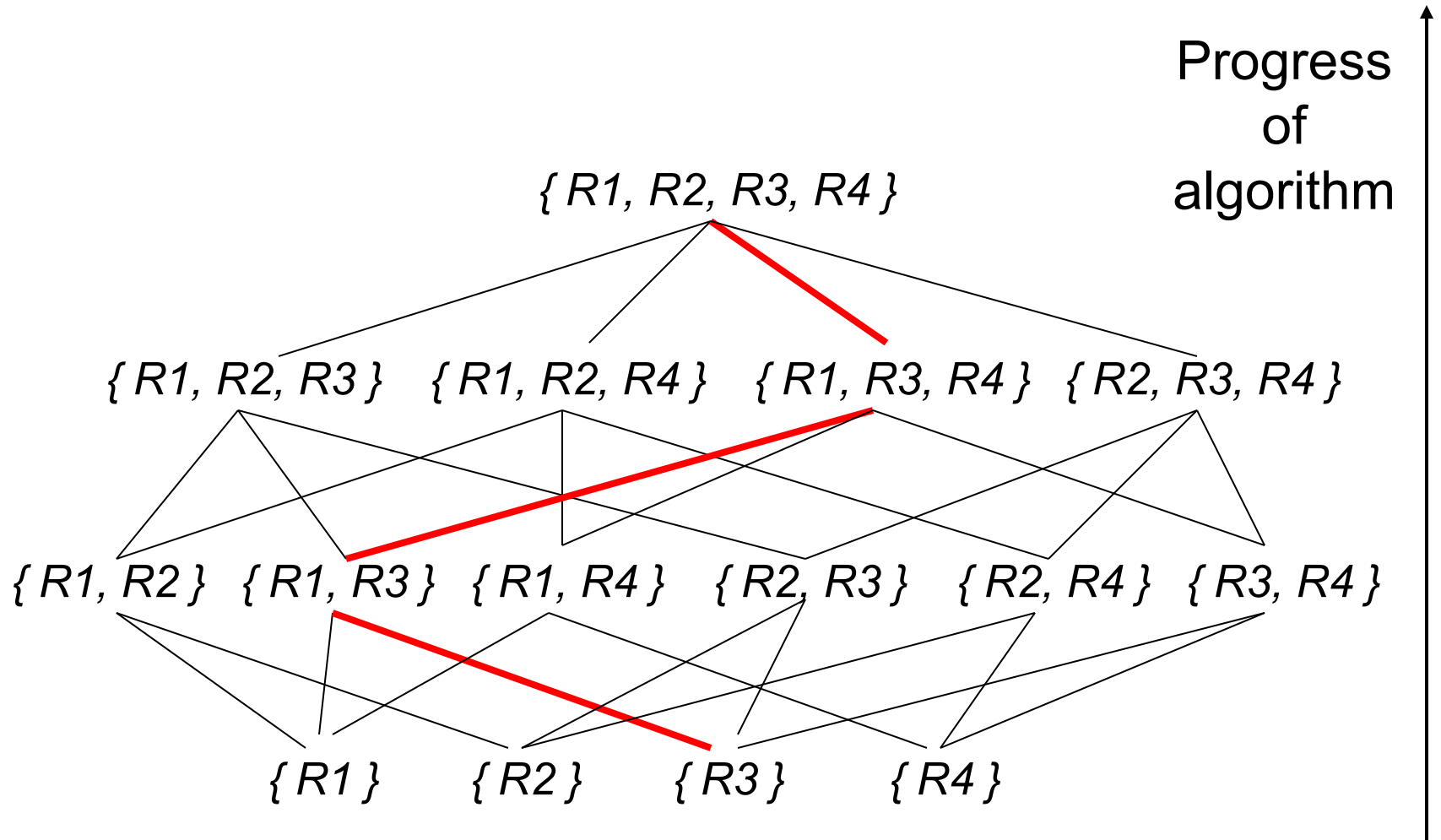
# Selinger Algorithm:

Query:  $R1 \bowtie R2 \bowtie R3 \bowtie R4$



# Selinger Algorithm:

Query:  $R1 \bowtie R2 \bowtie R3 \bowtie R4$

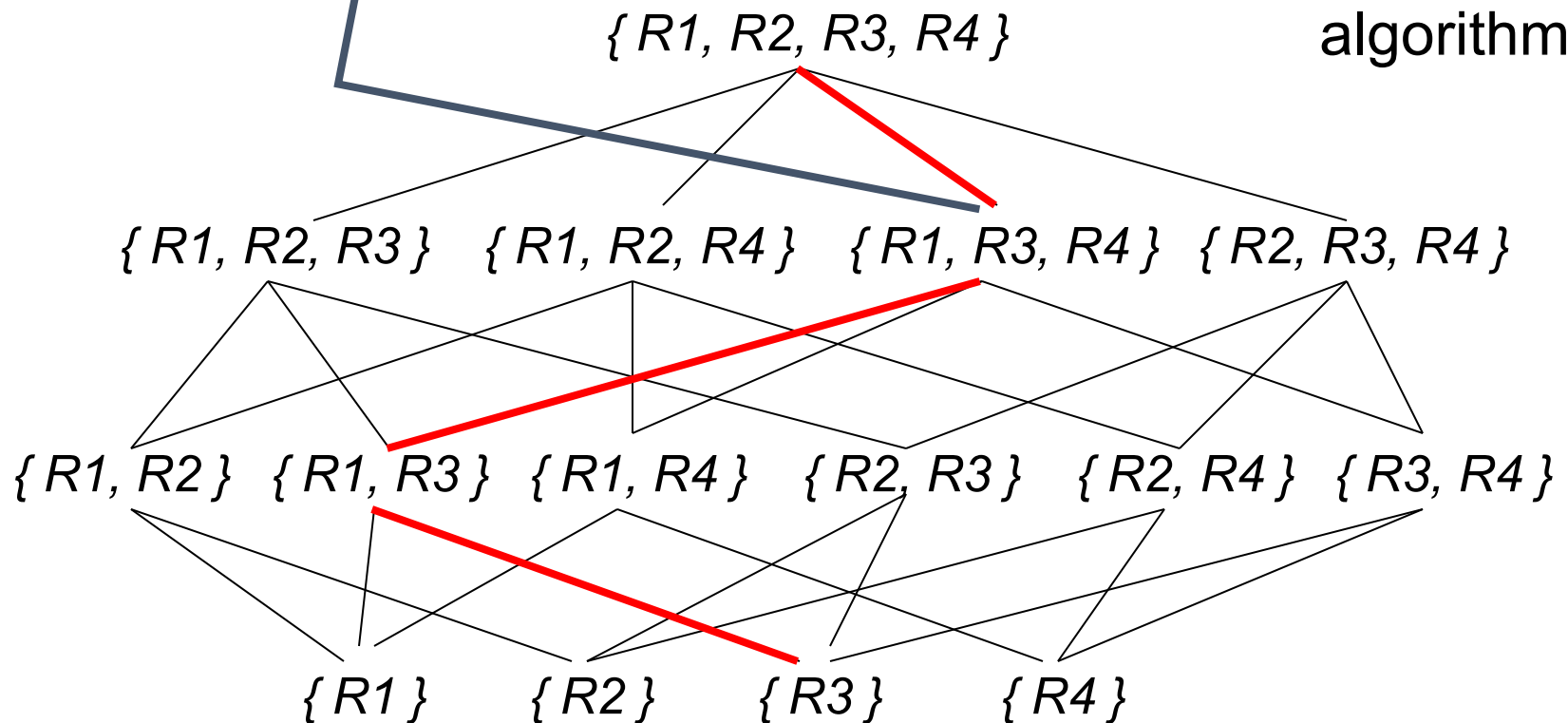


# Selinger Algorithm:

Query:  $R1 \bowtie R2 \bowtie R3 \bowtie R4$

e.g. All possible permutations of  $R1, R3, R4$   
have been considered  
after  $\text{OPT}(\{R1, R3, R4\})$  has been computed

Progress  
of  
algorithm



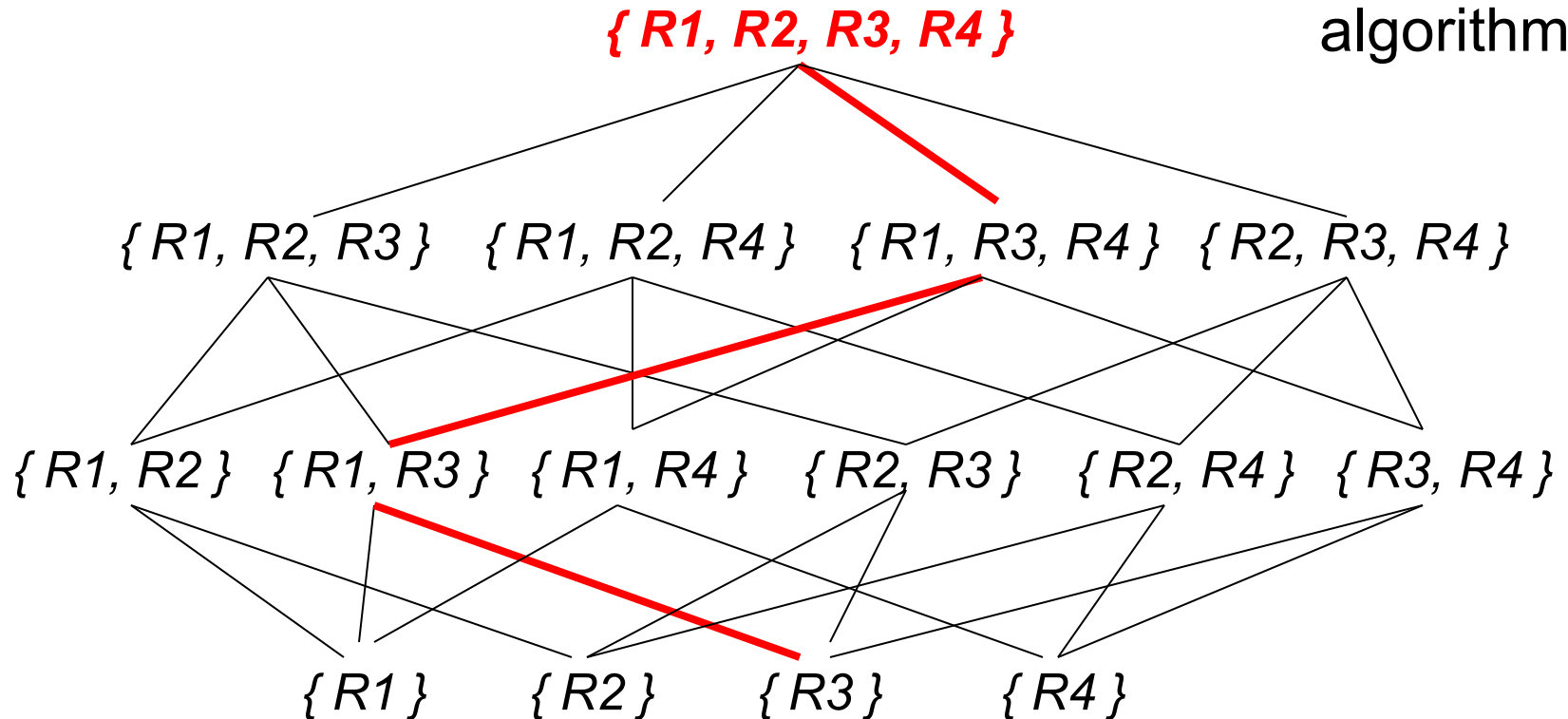
# Selinger Algorithm:

Query:  $R1 \bowtie R2 \bowtie R3 \bowtie R4$

Q. How to optimally compute join of  $\{R1, R2, R3, R4\}$ ?

Ans: First optimally join  $\{R1, R3, R4\}$  then join with  $R2$  as inner.

Progress  
of  
algorithm



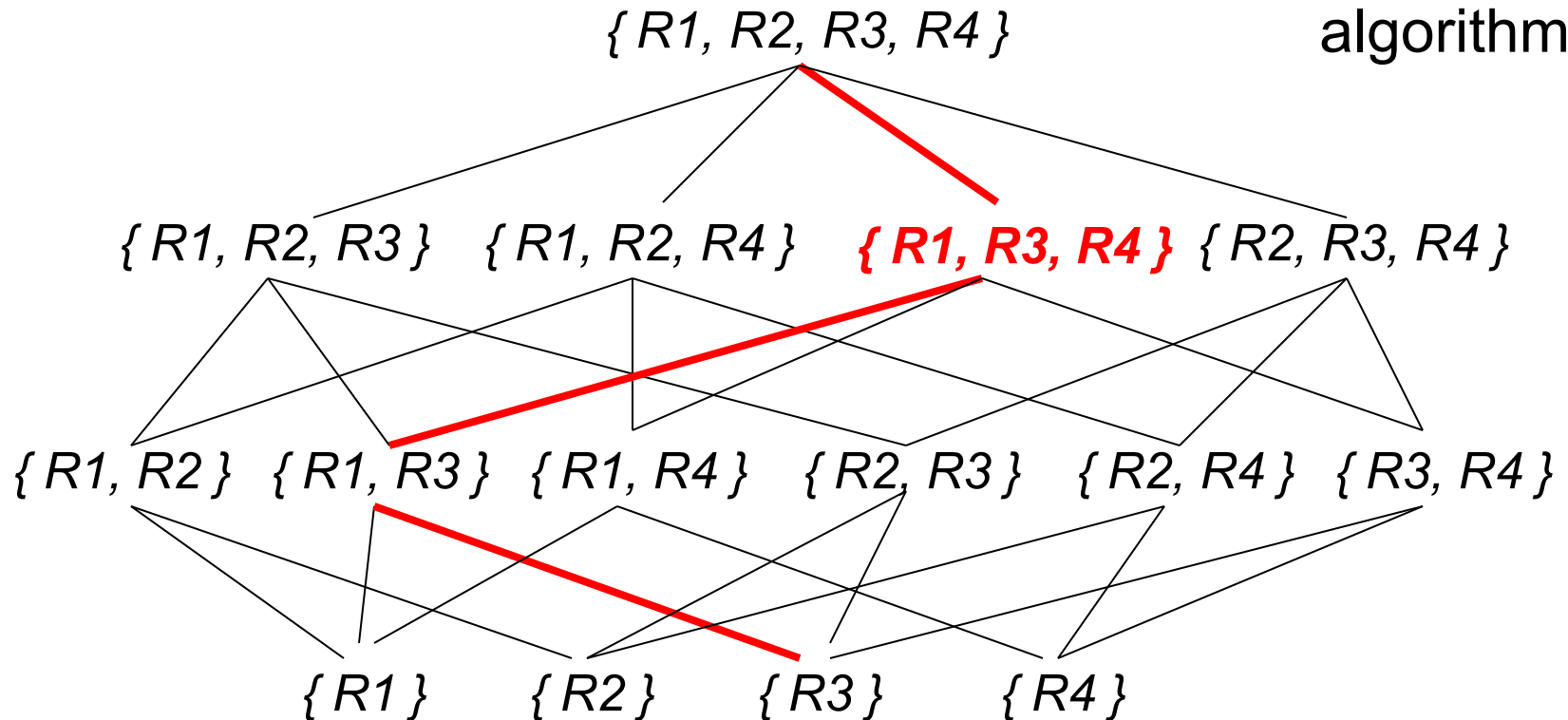
# Selinger Algorithm:

Query:  $R1 \bowtie R2 \bowtie R3 \bowtie R4$

Q. How to optimally compute join of  $\{R1, R3, R4\}$ ?

Ans: First optimally join  $\{R1, R3\}$ , then join with  $R4$  as inner.

Progress  
of  
algorithm



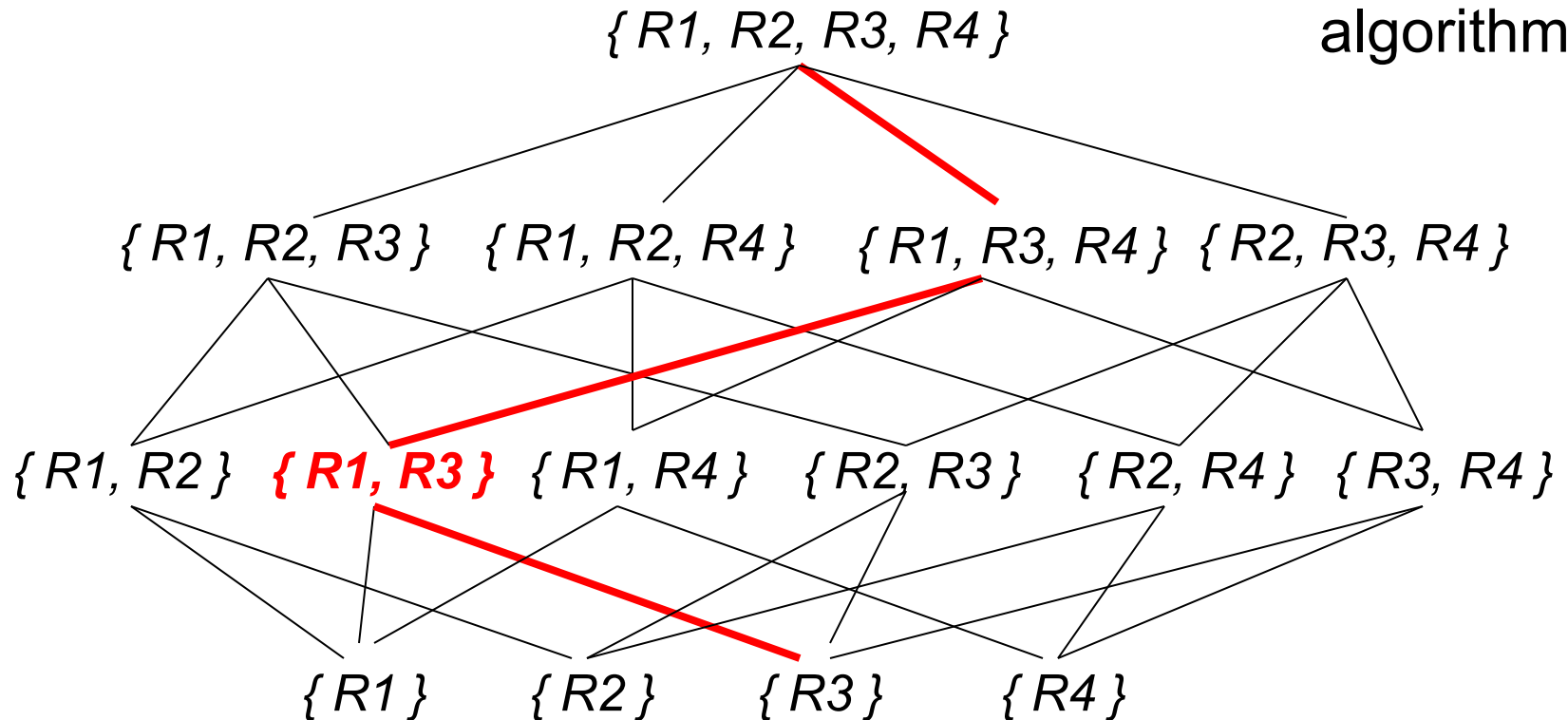
# Selinger Algorithm:

Query:  $R1 \bowtie R2 \bowtie R3 \bowtie R4$

Q. How to optimally compute join of  $\{R1, R3\}$ ?

Ans: First optimally join  $\{R3\}$ , then join with  $R1$  as inner.

Progress  
of  
algorithm



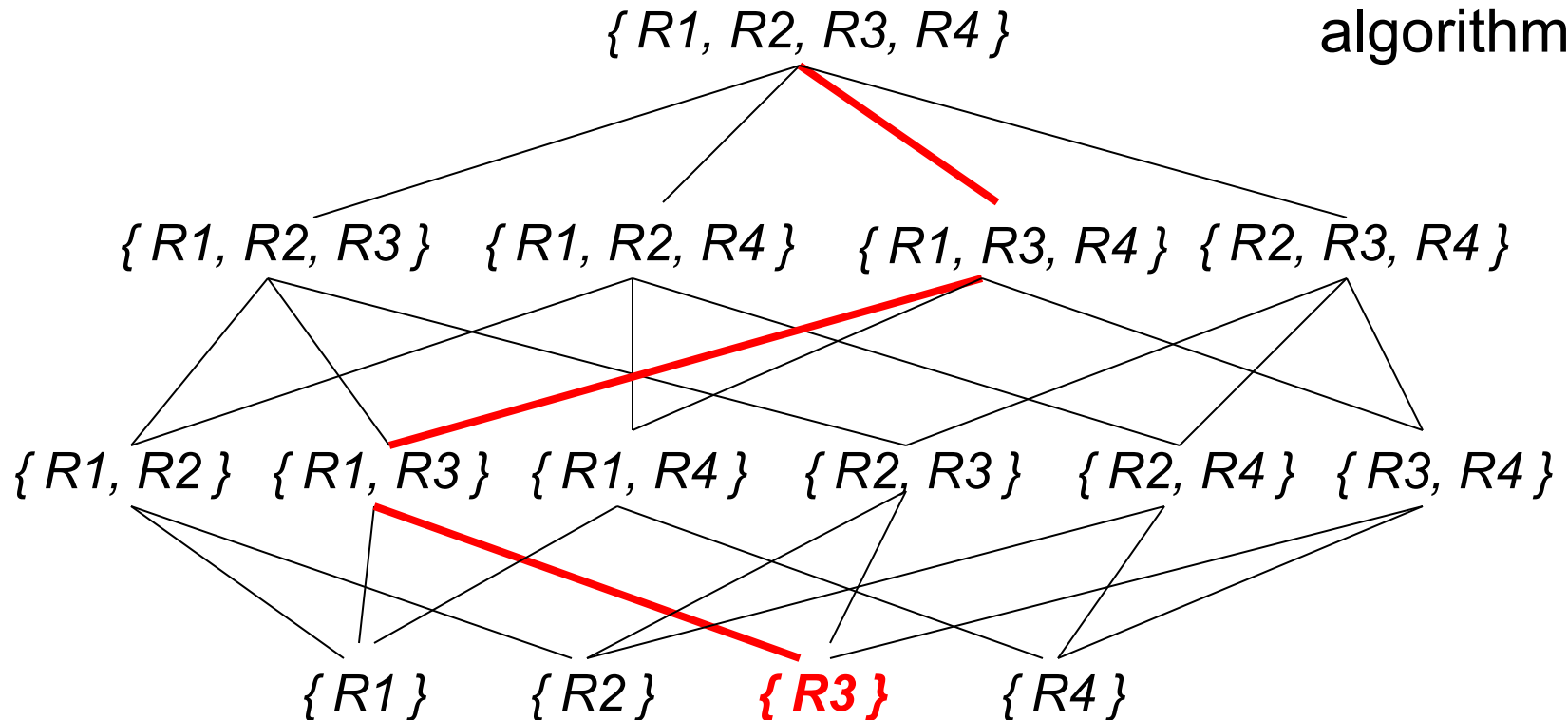
# Selinger Algorithm:

Query:  $R1 \bowtie R2 \bowtie R3 \bowtie R4$

Q. How to optimally compute join of  $\{R3\}$ ?

Ans: Single relation – so **optimally scan  $R3$** .

Progress  
of  
algorithm

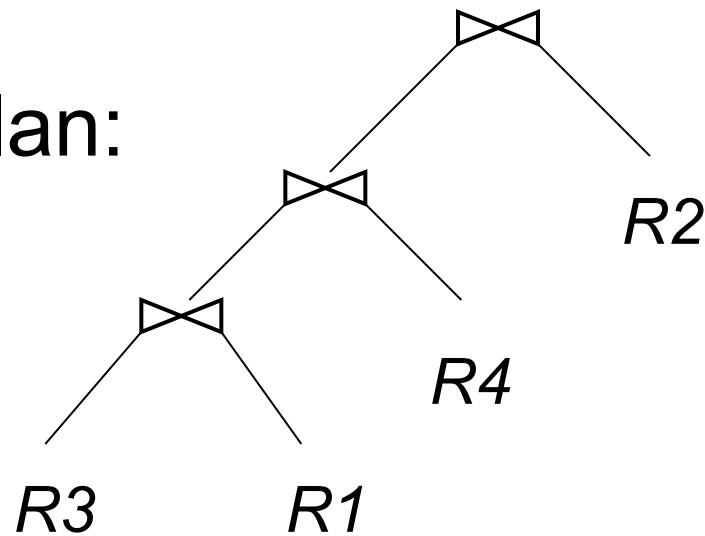


# Selinger Algorithm:

Query:  $R1 \bowtie R2 \bowtie R3 \bowtie R4$

---

Final optimal plan:



NOTE : There is a one-one correspondence between the permutation (R3, R1, R4, R2) and the above left deep plan



# The need for “interesting order”

- Optimal plan may not have an optimal sub-plan in practice!
- Example:  $R(A, B) \bowtie S(A, C) \bowtie T(A, D)$
- Best plan for  $R \bowtie S$ : hash join (beats sort-merge join)
- Best overall plan: sort-merge join  $R$  and  $S$ , and then sort-merge join with  $T$ 
  - Subplan of the optimal plan is not optimal!
- Why?
  - The result of the sort-merge join of  $R$  and  $S$  is sorted on  $A$
  - This is an **interesting order** that can be exploited by later processing (e.g., join, dup elimination, GROUP BY, ORDER BY, etc.)!

# Dealing with interesting orders

When picking the best plan

- Comparing their costs is not enough
  - Plans are not totally ordered by cost anymore
- Comparing interesting orders is also needed
  - Plans are now partially ordered
  - Plan  $X$  is better than plan  $Y$  if
    - Cost of  $X$  is lower than  $Y$ , and
    - Interesting orders produced by  $X$  “subsume” those produced by  $Y$
- Need to keep a **set** of optimal plans for joining every combination of  $k$  tables
  - At most one for each interesting order

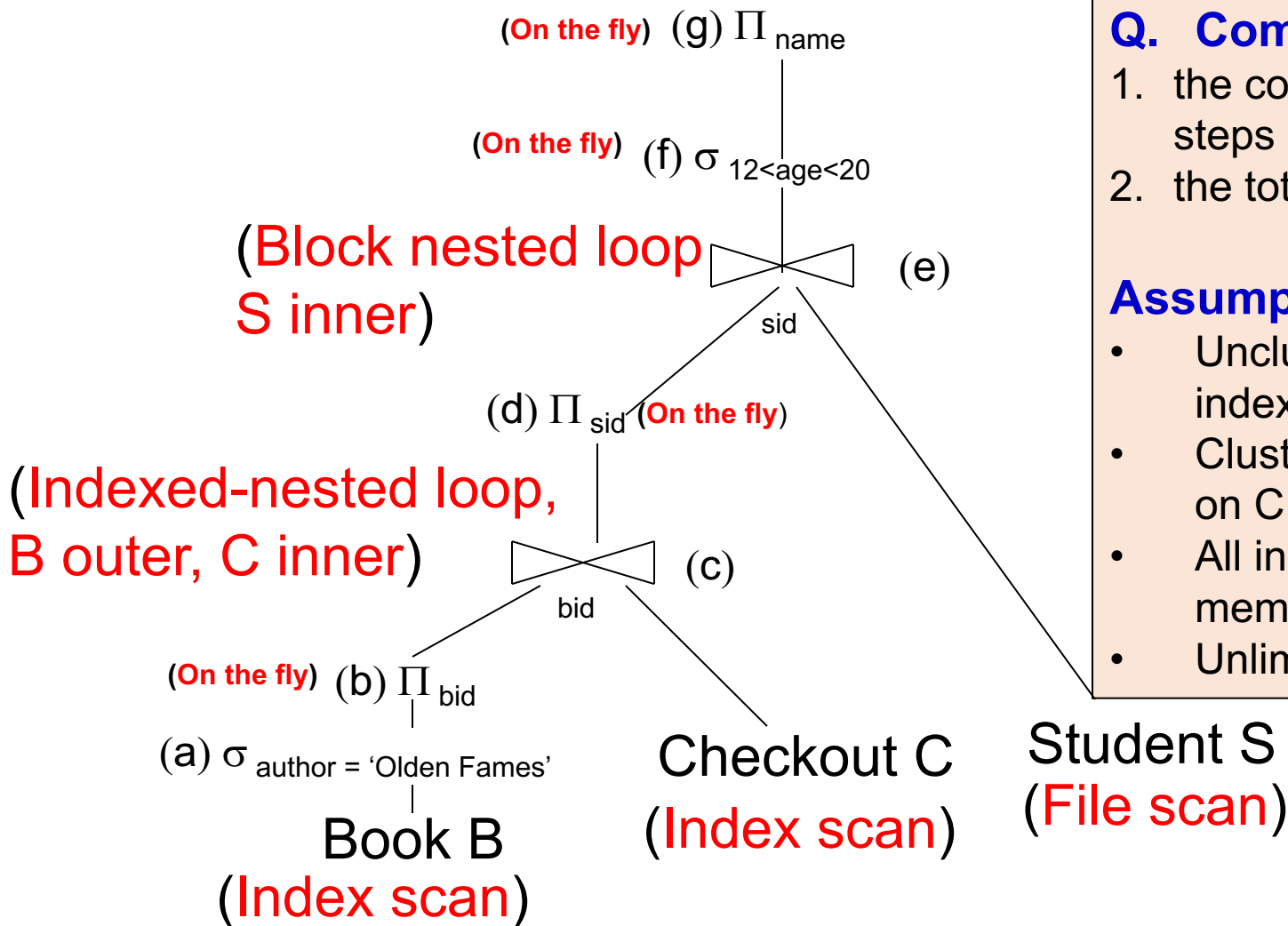
# Summary

- Relational algebra equivalence
- SQL rewrite tricks
- Heuristics-based optimization
- Cost-based optimization
  - Need statistics to estimate sizes of intermediate results
  - Greedy approach
  - Dynamic programming approach

Practice problem:  
Estimating the cost of the entire plan

S( <u>sid</u> ,name,age,addr)	no. of tuples	no. of pages	V(B,author) = 500
B( <u>bid</u> ,title,author)	T(S)=10,000	B(S)=1,000	7 <= age <= 24
C( <u>sid</u> , <u>bid</u> ,date)	T(B)=50,000	B(B)=5,000	V(B,author) = 500
	T(C)=300,000	B(C)=15,000	7 <= age <= 24

# Physical Query Plan



## Q. Compute

1. the cost and cardinality in steps (a) to (g)
2. the total cost

## Assumptions (given):

- Unclustered B+tree index on B.author
- Clustered B+tree index on C.bid
- All index pages are in memory
- Unlimited memory

S(sid,name,age,addr)

T(S)=10,000

B(S)=1,000

V(B,author) = 500

B(bid,title,author): Un. B+ on author

T(B)=50,000

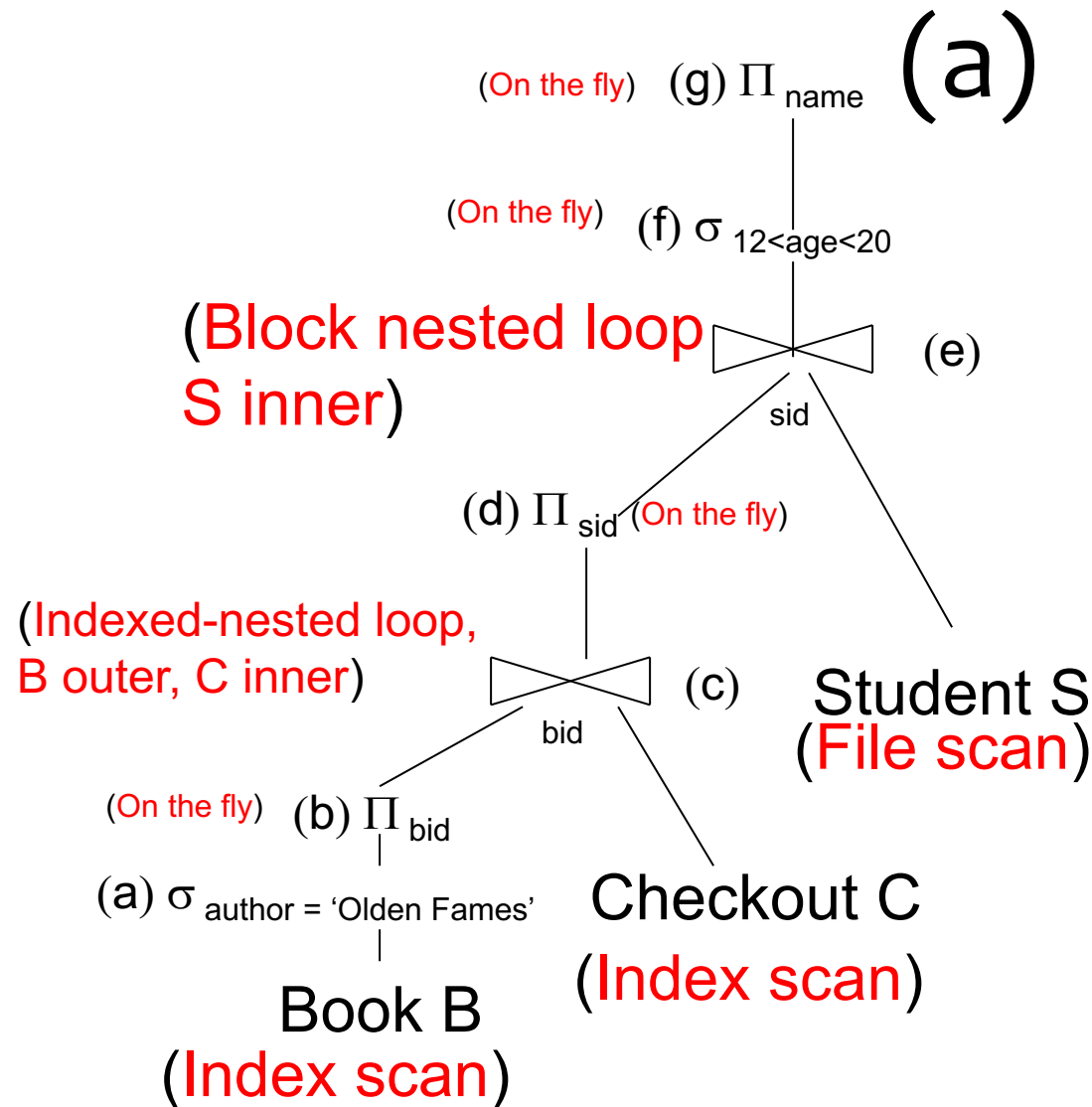
B(B)=5,000

7 <= age <= 24

C(sid,bid,date): Cl. B+ on bid

T(C)=300,000

B(C)=15,000



**Cost =**

$T(B) / V(B, \text{author})$

= 50,000/500

= 100 (unclustered)

**Cardinality =**

100

S(sid,name,age,addr)

T(S)=10,000

B(S)=1,000

B(bid,title,author): Un. B+ on author

T(B)=50,000

B(B)=5,000

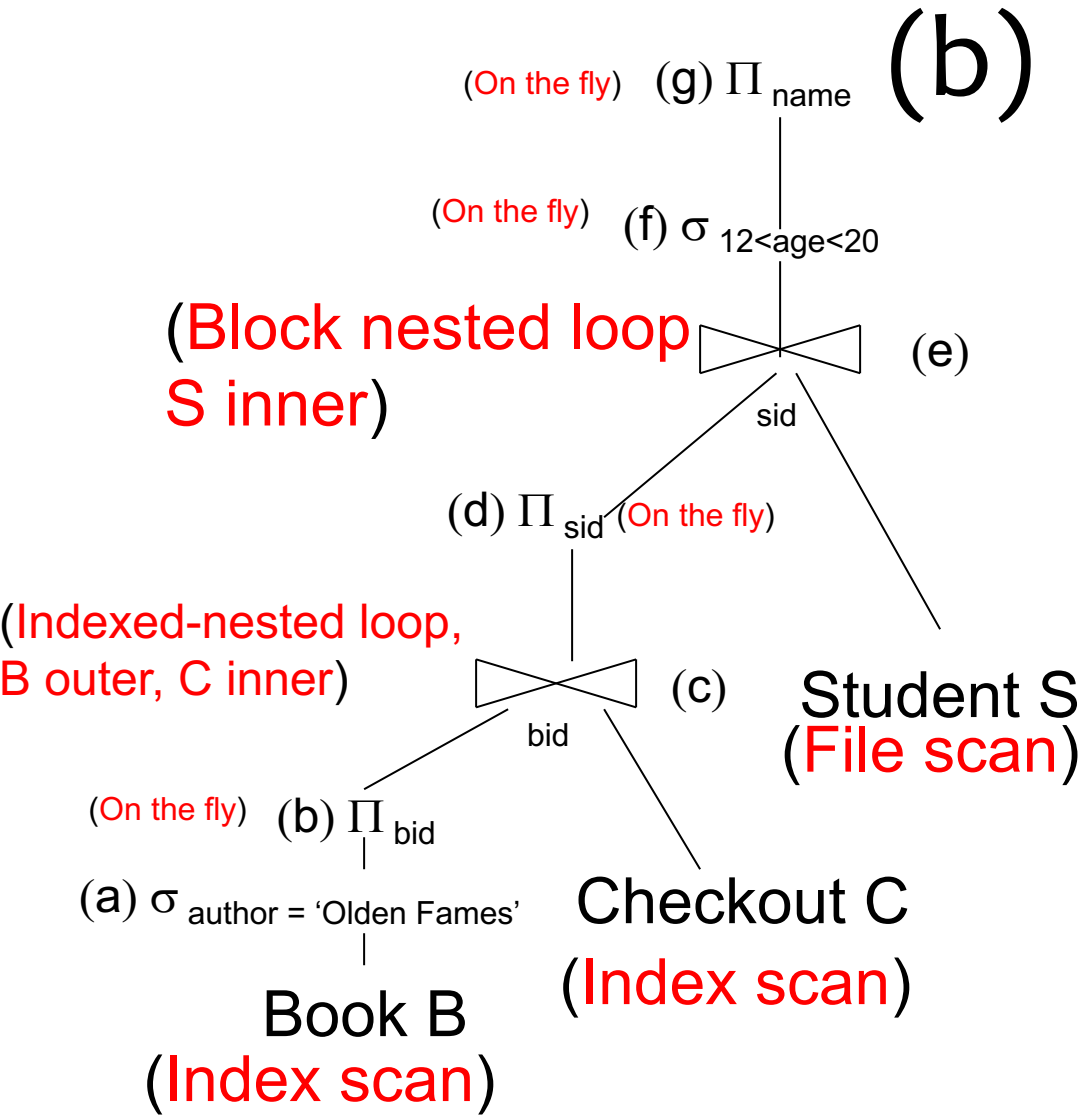
C(sid,bid,date): Cl. B+ on bid

T(C)=300,000

B(C)=15,000

V(B,author) = 500

7 <= age <= 24



Cost =

0 (on the fly)

Cardinality =

100

S(sid,name,age,addr)

T(S)=10,000

B(S)=1,000

V(B,author) = 500

B(bid,title,author): Un. B+ on author

T(B)=50,000

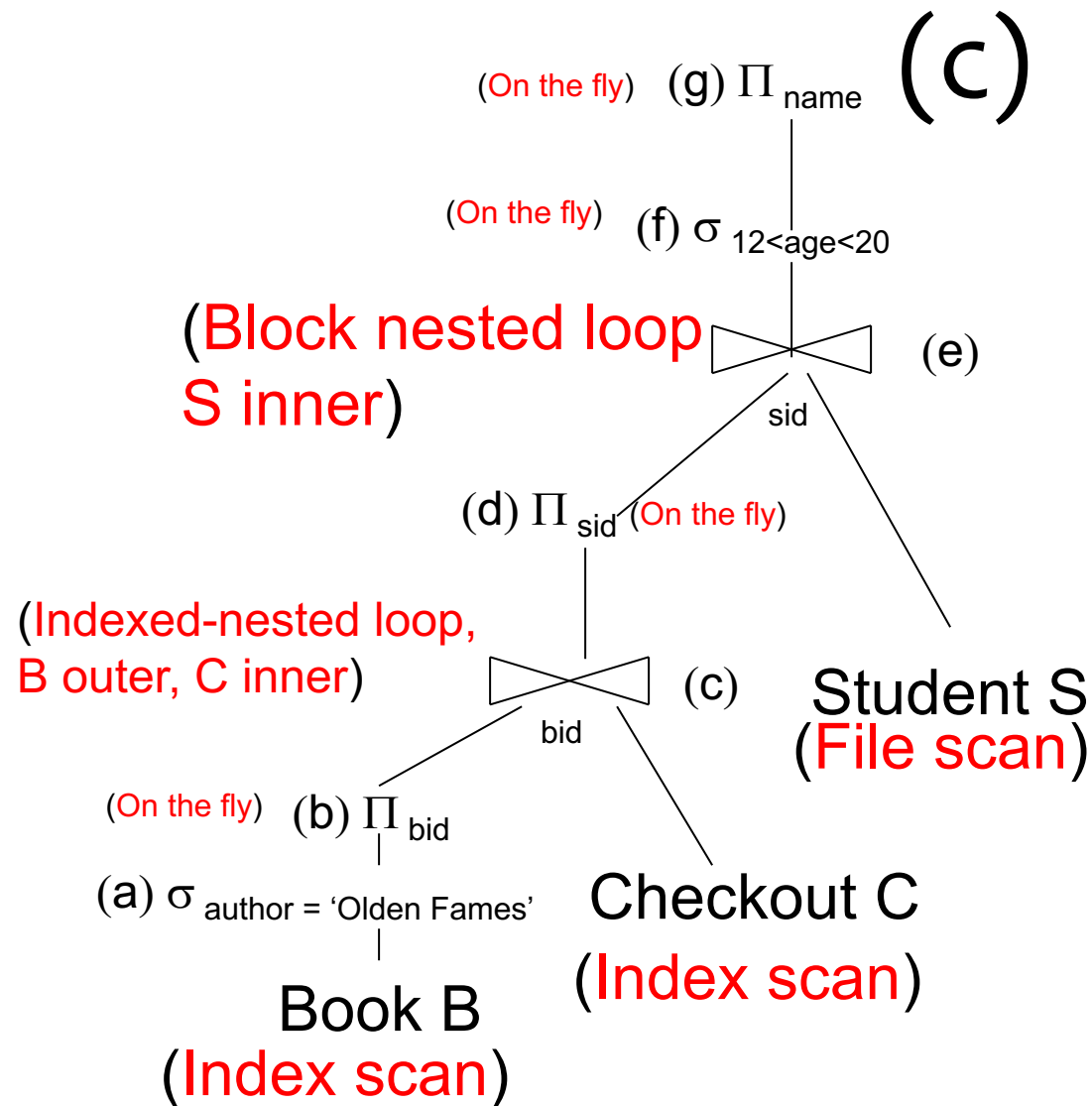
B(B)=5,000

7 <= age <= 24

C(sid,bid,date): Cl. B+ on bid

T(C)=300,000

B(C)=15,000



- one index lookup per outer B tuple
- 1 book has  $T(C)/T(B) = 6$  checkouts (uniformity)
- # C tuples per page =  $T(C)/B(C) = 20$
- 6 tuples fit in at most 2 consecutive pages (clustered) could assume 1 page as well

**Cost** <=

$$100 * 2 = 200$$

**Cardinality** =

$$100 * 6 = 600$$

$$= 100 * T(C) / \text{MAX}(100, V(C, \text{bid}))$$

assuming

$$V(C, \text{bid}) = V(B, \text{bid}) = T(B) = 50,000$$



S(sid,name,age,addr)

T(S)=10,000

B(bid,title,author): Un. B+ on author

T(B)=50,000

C(sid,bid,date): Cl. B+ on bid

T(C)=300,000

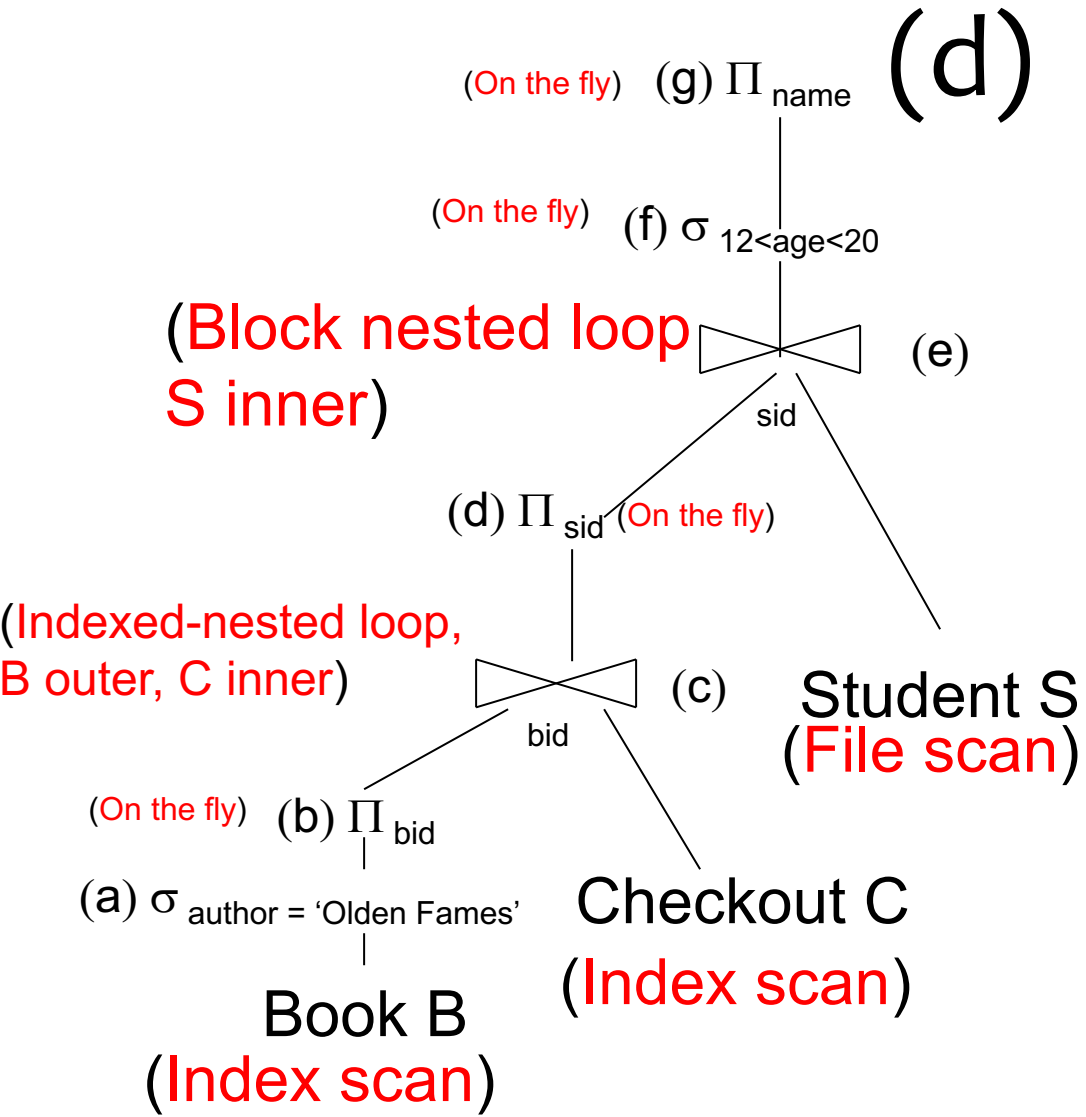
B(S)=1,000

B(B)=5,000

B(C)=15,000

V(B,author) = 500

7 <= age <= 24



Cost =

0 (on the fly)

Cardinality =

600

S(sid,name,age,addr)

T(S)=10,000

B(S)=1,000

B(bid,title,author): Un. B+ on author

T(B)=50,000

B(B)=5,000

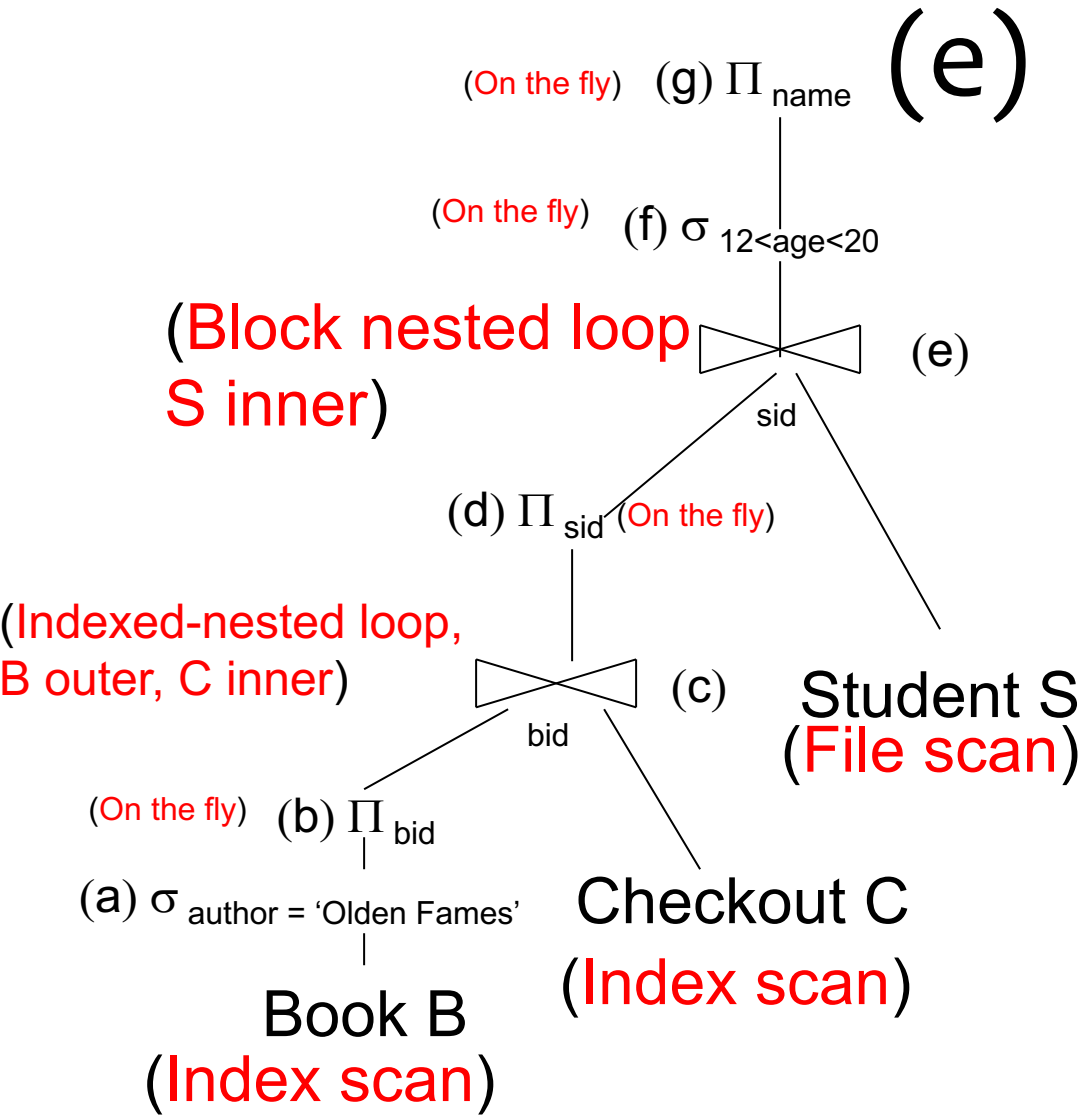
V(B,author) = 500

7 <= age <= 24

C(sid,bid,date): Cl. B+ on bid

T(C)=300,000

B(C)=15,000



Outer relation is already in (unlimited) memory need to scan S relation

Cost =

$B(S) = 1000$

Cardinality =

600

(one student per checkout)

S(sid,name,age,addr)

T(S)=10,000

B(S)=1,000

B(bid,title,author): Un. B+ on author

T(B)=50,000

B(B)=5,000

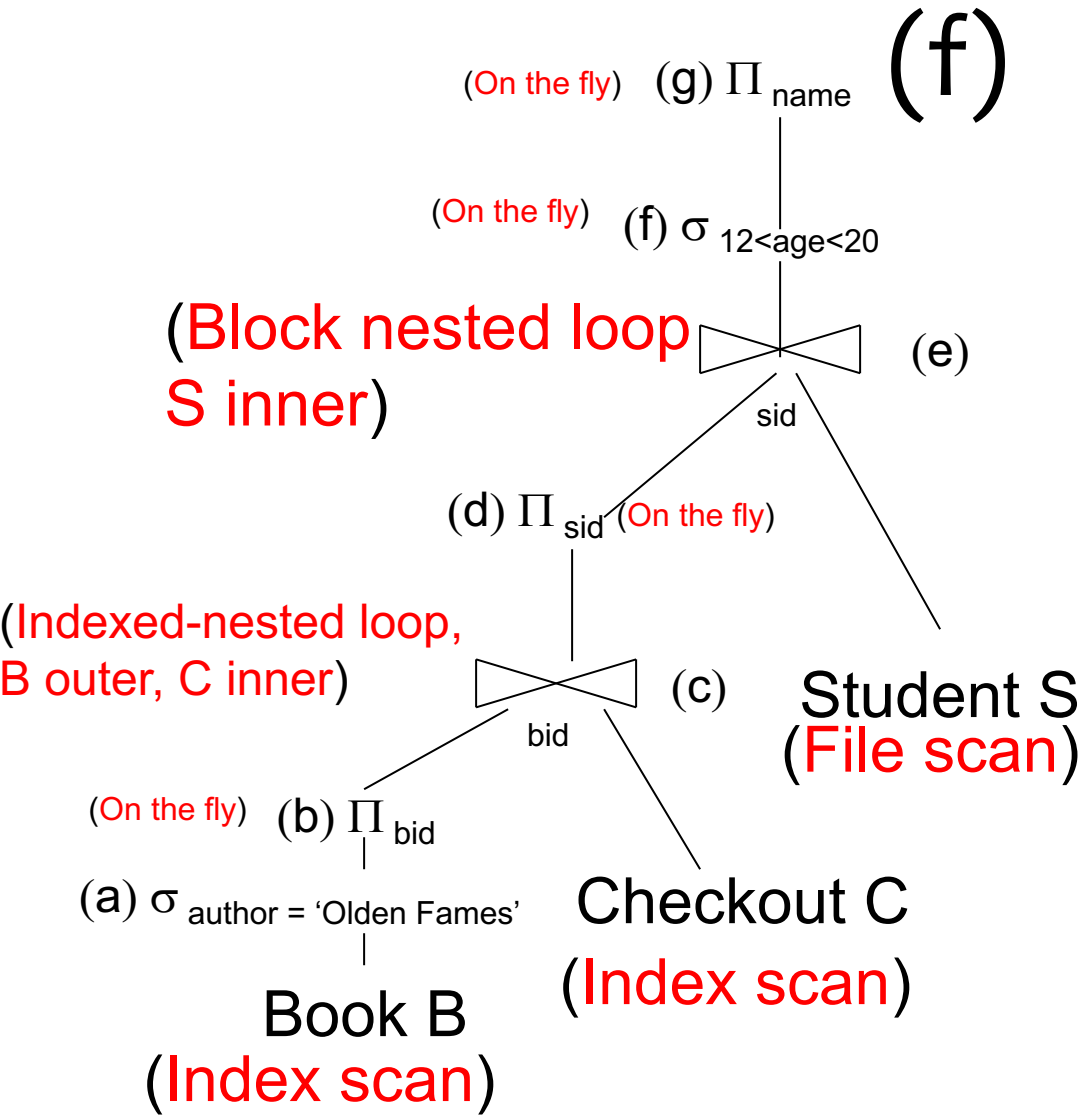
V(B,author) = 500

C(sid,bid,date): Cl. B+ on bid

T(C)=300,000

B(C)=15,000

7 <= age <= 24



Cost =

0 (on the fly)

Cardinality =

600 \* 7/18 = 234 (approx)

S(sid,name,age,addr)

T(S)=10,000

B(S)=1,000

B(bid,title,author): Un. B+ on author

T(B)=50,000

B(B)=5,000

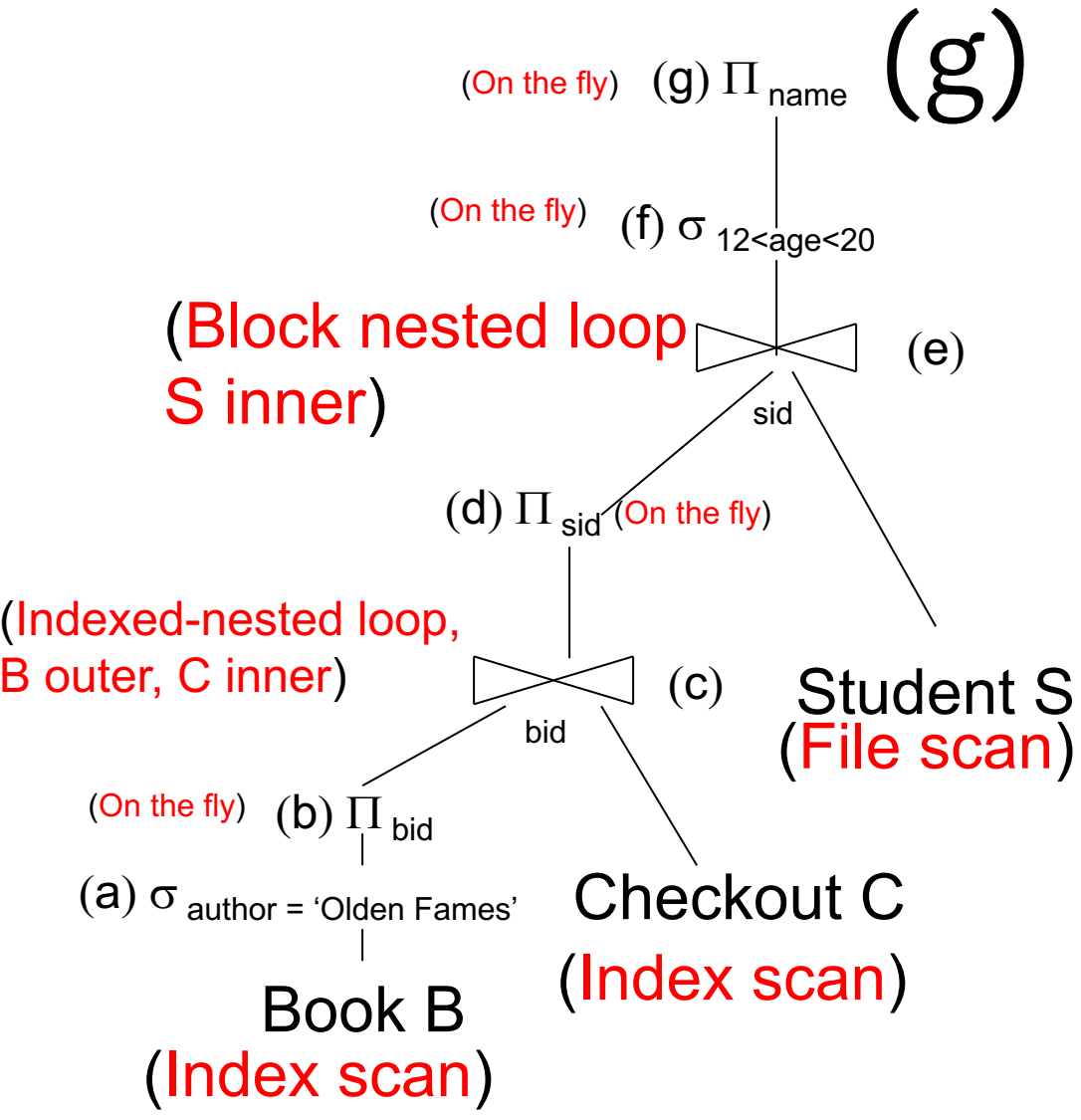
V(B,author) = 500

7 <= age <= 24

C(sid,bid,date): Cl. B+ on bid

T(C)=300,000

B(C)=15,000



Cost =

0 (on the fly)

Cardinality =

234

S(sid,name,age,addr)

T(S)=10,000

B(S)=1,000

B(bid,title,author): Un. B+ on author

T(B)=50,000

B(B)=5,000

C(sid,bid,date): Cl. B+ on bid

T(C)=300,000

B(C)=15,000

V(B,author) = 500

7 <= age <= 24

