

Test 1: CPS 100

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Name: _____

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Honor code acknowledgment (signature) _____

	value	grade
Problem 1	18 pts.	
Problem 2	10 pts.	
Problem 3	30 pts.	
Problem 4	12 pts.	
TOTAL:	70 pts.	

This test has 10 pages, be sure your test has them all. Do NOT spend too much time on one question — remember that this class lasts 50 minutes.

In writing code you do not need to worry about specifying the proper `#include` header files. Assume that all the header files we've discussed are included in any code you write.

The declaration for linked list nodes on this test is:

```
struct ListNode
{
    string info;
    ListNode * next;

    ListNode(const string& s, ListNode * ptr)
        : info(s), next(ptr)
    { }
};
```

The declaration for binary search tree nodes on this test is:

```
struct TreeNode
{
    string info;
    TreeNode * left;
    TreeNode * right;

    TreeNode(const string& s, TreeNode * lt, TreeNode * rt)
        : info(s), left(lt), right(rt)
    { }
};
```

PROBLEM 1 : (*Count Chocula (18 points/6 each)*)

Part A

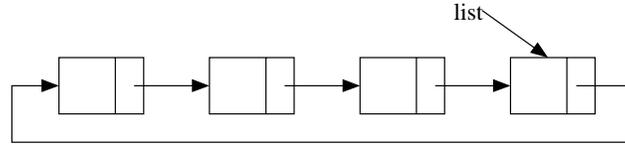
Write function `count` that returns the number of nodes in a NULL-terminated linked list that does not have a header node.

```
int count(ListNode * list)
// pre: list is NULL/0 terminated
// post: return # nodes in list
{

}
}
```

Part B

Write function `circularcount` that returns the number of nodes in a circularly-linked list like the one illustrated below.



```
int circularcount(ListNode * list)
// pre: list is circular
// post: return # nodes in list, list is unchanged
{
```

```
}
```

Part C

Write function `treecount` that returns the number of nodes in a binary tree.

```
int treecount(TreeNode * root)
// pre: root points to a binary tree (or root == NULL)
// post: return # nodes in tree
{
```

```
}
```

PROBLEM 2 : (*Sordid Find (10 points/5 each)*)

Part A

The function `find` below satisfies its postcondition.

```
bool find(ListNode * list, const string& s)
// pre: list has a header node
// post: returns true if s in list, returns false otherwise
{
    list = list->next;    // skip header
    while (list != 0) {
        if (list->info == s) return true;
        list = list->next;
    }
    return false;
}
```

If the list passed to `find` is sorted, the performance of the function can be improved by stopping the search when a value larger than `s` is found (in this case the function can return false without searching the rest of the list). Rewrite the function so that it has this early stopping condition.

```
bool find(ListNode * list, const string& s)
// pre: list has a header node, list is sorted from lowest to highest value
// post: returns true if s in list, returns false otherwise
{

}

}
```

Part B

The original function `find` has a worst-case complexity $O(n)$ for an n -node list. What is the complexity using big-Oh of the new version you wrote for Part A. Justify your answer briefly.

PROBLEM 3 : (*Intersecting interests*)

An `MSApplicant` sub-class named `MSIntersection` computes the intersection of two `Multiset` objects using the code below.

```
void doIntersection (Multiset * lhs, Multiset * rhs, Multiset * result)
// post: *result is intersection of *lhs and *rhs
{
    MSIntersection intersection(lhs, result);
    rhs->applyAll(intersection);
}
```

The intersection of two multisets contains one occurrence of every string that occurs at least once in both multisets.

For example, the intersection of the multisets

```
(["apple", 2], ["kiwi", 6], ["orange", 4], ["cherry", 23])
```

and

```
(["apple", 10], ["banana", 3], ["orange", 12])
```

is the multiset containing (`["apple", 1], ["orange", 1]`), i.e., one occurrence of each value in common to both multisets.

The code for `MSIntersection` is on the last page of the test. You'll be asked to reason about its complexity. The basic algorithm for calculating the intersection as shown in the code above for `doIntersection` when used with `MSIntersection:applyOne` is:

- For each word in multiset `rhs`, see if it occurs in `lhs`
- If the word does occur in `lhs`, add it to the intersection

Part A (4 points)

The call `doIntersect(a,b,result)` will correctly store the intersection of `a` and `b` in `result` regardless of whether `a`, `b`, and `result` are implemented using `LinkedMultisets`, `TableMultisets`, or `TreeMultisets`. In one or two sentences explain why.

Part B (6 points)

What is the big-Oh complexity of calculating the intersection of two `LinkedMultiset` objects `a` and `b` where `a` has `N` elements and `b` has `N` elements, and `result` is an initially empty `LinkedMultiset` object using the following call.

```
doIntersection(a,b,result);
```

Express your answer in terms of `N` and justify your answer briefly. Recall that `count` is an $O(n)$ operation for an `n`-element `LinkedMultiset` and that `add` is an $O(1)$ or constant-time operation.

Part C (6 points)

What is the complexity using big-Oh of the `doIntersection` call

```
doIntersection(a,b,result);
```

if all multisets are implemented as `TreeMultiset` objects, `a` and `b` both contain `N` elements, and `result` is initially empty. Recall that the `TreeMultiset` class uses a binary search tree so that `count` and `add` are both $O(\log n)$ operations for an `n`-element `TreeMultiset`. Justify your answer briefly.

Part D (8 points)

Suppose multisets **a** and **b** have N and M elements, respectively. Consider the following calculation for storing the intersection of **a** and **b** in **result**.

```
if (a->size() < b->size()) {
    doIntersection(a,b,result)
}
else {
    doIntersection(b,a,result)
}
```

Explain why this method makes an enormous difference when `TreeMultiset` objects are used but very little difference when `LinkedMultiset` objects are used. For full credit you should analyze the complexity of the code when the sizes of **a** and **b** differ by many orders of magnitude, e.g., the sizes are 2^{10} and 2^{20} .

Part E (6 points)

For this part, assume the definition of intersection changes so that the result set contains $\min(x,y)$ occurrences of strings that occur x times in one set and y times in another and `min` is a function that returns the minimum of its two integer arguments.

For example, the intersection of the multisets

```
(["apple", 2], ["kiwi", 6], ["orange", 4], ["cherry", 23])
```

and

```
(["apple", 10], ["banana", 3], ["orange", 12])
```

is the multiset containing `(["apple", 2], ["orange", 4])`,

Rewrite `MSIntersection::applyOne` so that it works with this definition (see the code page for `MSIntersection`).

```
void MSIntersection::applyOne(const string& s, int count)
{
```

```
}
```

PROBLEM 4 : (*Least Common Denominator (12 points)*)

This problem involves creating a new sorted linked list from two sorted linked lists. The new linked list contains those elements in common to both sorted linked lists. For example, for the two lists ("bat", "cat", "hat", "sat", "vat") and ("cat", "fat", "hat", "pat", "sat") the list returned should be ("cat", "hat", "sat"). Assume that each list being processed has no duplicate elements, i.e., a list like ("mat", "rat", "rat") won't be processed since it has a duplicate/repeated element.

Write the function *common* whose header is shown below so that it runs in $O(n)$ time when both lists *a* and *b* have *n* nodes.

The idea is to traverse both lists adding nodes to the end of *result* when appropriate. The function is started for you, you should maintain the invariant noted in the comment. *All lists have header nodes.*

```
ListNode * common(ListNode * a, ListNode * b)
// pre: a and b are sorted, both have header nodes,
// post: return sorted list with header node containing
//       values in common to a and b
{
    a = a->next;        // skip header nodes in both a and b
    b = b->next;

    ListNode * result = new ListNode("",0); // return this list
    ListNode * tail = result;

    // invariant: result list is sorted, tail points to its last node

    return result;
}
```

Multisets have the following interface:

```
class Multiset
{
public:

    virtual ~Multiset() {}          // multisets are deleted properly

    virtual bool add(const string& word)          = 0; // add word to multiset
    virtual int  count(const string& word) const = 0; // # times word occurs
    virtual int  size()                          const = 0; // # elements in multiset
    virtual void applyAll(MSApplicant& applicant) const = 0;
};
```

MSApplicants have the following interface:

```
class MSApplicant
{
public:

    virtual ~Multiset() {}
    virtual void applyOne(const string& word, int count) = 0;
};
```

The declaration/definition of MSIntersection follow.

```
class MSIntersection : public MSApplicant
{
public:

    MSIntersection (Multiset * lhs, Multiset * result)
        : myLHS(lhs), myResult(result)
    {}

    virtual void applyOne (const string& word, int count)
    {
        if (myLHS->count(word) != 0) {
            myResult->add(word);
        }
    }

private:

    Multiset * myLHS;
    Multiset * myResult;
};
```