

CompSci 516  
Database Systems

Lecture 4  
SQL

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# Announcements

- Lab-1 makeup instructions sent on piazza
  - Please respond by 3 pm today if you have missed the lab
- Let me know if you are still not on piazza
- HW1 will be posted after the class
  - On sakai (data is already there)
  - Deadlines in stages
  - First deadline on 09/17

# Today's topic

- Finish SQL
- RC
- Next week:
  - Tuesday: Guest Lecture by Junyang Gao: RA
  - Thursday: Lab on RA

Acknowledgement:

The following slides have been created adapting the instructor material of the [RG] book provided by the authors

Dr. Ramakrishnan and Dr. Gehrke.

# Nulls and Views in SQL

# Null Values

- Field values in a tuple are sometimes
  - **unknown**, e.g., a rating has not been assigned, or
  - **inapplicable**, e.g., no spouse's name
  - SQL provides a special value **null** for such situations.

# Standard Boolean 2-valued logic

- True = 1, False = 0
- Suppose  $X = 5$ 
  - $(X < 100) \text{ AND } (X \geq 1)$  is  $T \wedge T = T$
  - $(X > 100) \text{ OR } (X \geq 1)$  is  $F \vee T = T$
  - $(X > 100) \text{ AND } (X \geq 1)$  is  $F \wedge T = F$
  - $\text{NOT}(X = 5)$  is  $\neg T = F$
- Intuitively,
  - $T = 1, F = 0$
  - For  $V1, V2 \in \{1, 0\}$
  - $V1 \wedge V2 = \text{MIN}(V1, V2)$
  - $V1 \vee V2 = \text{MAX}(V1, V2)$
  - $\neg(V1) = 1 - V1$

# 2-valued logic does not work for nulls

- Suppose rating = null, X = 5
- Is rating > 8 true or false?
- What about **AND**, **OR** and **NOT** connectives?
  - (rating > 8) AND (X = 5)?
- What if we have such a condition in the WHERE clause?

# 3-Valued Logic For Null

- TRUE (= 1), FALSE (= 0), UNKNOWN (= 0.5)
  - unknown is treated as 0.5
- Now you can apply rules from 2-valued logic!
  - For  $V1, V2 \in \{1, 0, 0.5\}$
  - $V1 \wedge V2 = \text{MIN}(V1, V2)$
  - $V1 \vee V2 = \text{MAX}(V1, V2)$
  - $\neg(V1) = 1 - V1$
- Therefore,
  - NOT UNKNOWN = UNKNOWN
  - UNKNOWN OR TRUE = TRUE
  - UNKNOWN AND TRUE = UNKNOWN
  - UNKNOWN AND FALSE = FALSE
  - UNKNOWN OR FALSE = UNKNOWN



# New issues for Null

- The presence of **null** complicates many issues. E.g.:
  - Special operators needed to check if value **IS/IS NOT NULL**
  - Be careful!
  - “WHERE X = NULL” does not work!
  - Need to write “WHERE X IS NULL”
- Meaning of constructs must be defined carefully
  - e.g., **WHERE clause eliminates rows that don't evaluate to true**
  - So not only FALSE, but UNKNOWNs are eliminated too
  - **very important to remember!**
- But NULL allows new operators (e.g. **outer joins**)
- Can force “no nulls” while creating a table
  - **sname char(20) NOT NULL**
  - **primary key is always not null**

# Aggregates with NULL

sid	sname	rating	age
22	dustin	7	45
31	lubber	8	55
58	rusty	10	35

R1

- What do you get for
- `SELECT count(*) from R1?`
- `SELECT count(rating) from R1?`

# Aggregates with NULL

sid	sname	rating	age
22	dustin	7	45
31	lubber	8	55
58	rusty	10	35

R1

- What do you get for
- `SELECT count(*) from R1?`
- `SELECT count(rating) from R1?`
- **Ans: 3 for both**

# Aggregates with NULL

sid	sname	rating	age
22	dustin	7	45
31	lubber	8	55
58	rusty	10	35

R1

sid	sname	rating	age
22	dustin	7	45
31	lubber	null	55
58	rusty	10	35

R2

- What do you get for
  - SELECT count(\*) from R1?
  - SELECT count(rating) from R1?
  - **Ans: 3 for both**
- 
- What do you get for
  - SELECT count(\*) from R2?
  - SELECT count(rating) from R2?

# Aggregates with NULL

sid	sname	rating	age
22	dustin	7	45
31	lubber	8	55
58	rusty	10	35

R1

sid	sname	rating	age
22	dustin	7	45
31	lubber	null	55
58	rusty	10	35

R2

- What do you get for
- SELECT count(\*) from R1?
- SELECT count(rating) from R1?
- **Ans: 3 for both**

- What do you get for
- SELECT count(\*) from R2?
- SELECT count(rating) from R2?
- **Ans: First 3, then 2**

# Aggregates with NULL

- COUNT, SUM, AVG, MIN, MAX (with or without DISTINCT)
  - Discards null values first
  - Then applies the aggregate
  - Except count(\*)
- If only applied to null values, the result is null

sid	sname	rating	age
22	dustin	7	45
31	lubber	null	55
58	rusty	10	35

R2

- SELECT sum(rating) from R2?
- **Ans: 17**

sid	sname	rating	age
22	dustin	null	45
31	lubber	null	55
58	rusty	null	35

R3

- SELECT sum(rating) from R3?
- **Ans: null**

# Creating Relations in SQL

- Creates the “Students” relation
  - the type (domain) of each field is specified
  - enforced by the DBMS whenever tuples are added or modified
- As another example, the “Enrolled” table holds information about courses that students take

```
CREATE TABLE Students
(sid CHAR(20),
 name CHAR(20),
 login CHAR(10),
 age INTEGER,
 gpa REAL)
```

```
CREATE TABLE Enrolled
(sid CHAR(20),
 cid CHAR(20),
 grade CHAR(2))
```

sid	name	login	age	gpa
53666	Jones	jones@cs	18	3.4
53688	Smith	smith@eecs	18	3.2
53650	Smith	smith@math	19	3.8

Students

sid	cid	grade
53831	Carnatic101	C
53831	Reggae203	B
53650	Topology112	A
53666	History105	B

Enrolled

# Destroying and Altering Relations

`DROP TABLE Students`

- Destroys the relation Students
  - The schema information *and* the tuples are deleted.

`ALTER TABLE Students`

`ADD COLUMN firstYear: integer`

- The schema of Students is altered by adding a new field; every tuple in the current instance is extended with a **NULL** value in the new field.



# Adding and Deleting Tuples

- Can insert a single tuple using:

```
INSERT INTO Students (sid, name, login, age, gpa)
VALUES (53688, 'Smith', 'smith@ee', 18, 3.2)
```

- Can delete all tuples satisfying some condition (e.g., name = Smith):

```
DELETE
FROM Students S
WHERE S.name = 'Smith'
```

# Integrity Constraints (ICs)

- **IC:** condition that must be true for **any** instance of the database
  - e.g., **domain constraints**
  - ICs are specified when schema is defined
  - ICs are checked when relations are modified
- A **legal** instance of a relation is one that satisfies all specified ICs
  - **DBMS will not allow illegal instances**
- If the DBMS checks ICs, stored data is more faithful to real-world meaning
  - Avoids data entry errors, too!

# Keys in a Database

- Key / Candidate Key
- Primary Key
- Super Key
- Foreign Key
  
- Primary key attributes are underlined in a schema
  - Person(pid, address, name)
  - Person2(address, name, age, job)

# Primary Key Constraints

- A set of fields is a **key** for a relation if :
  1. No two distinct tuples can have same values in all key fields, and
  2. This is not true for any subset of the key
- Part 2 false? A **superkey**
- If there are  $> 1$  keys for a relation, one of the keys is chosen (by DBA = DB admin) to be the **primary key**
  - E.g., sid is a key for Students
  - The set {sid, gpa} is a superkey.
- Any possible benefit to refer to a tuple using primary key (than any key)?

# Primary and Candidate Keys in SQL

- Possibly many **candidate keys**

- specified using **UNIQUE**

- one of which is chosen as the primary key.

- “For a given student and course, there is a single grade.”

```
CREATE TABLE Enrolled  
(sid CHAR(20)  
  cid CHAR(20),  
  grade CHAR(2),  
  PRIMARY KEY (???)
```

# Primary and Candidate Keys in SQL

- Possibly many **candidate keys**

- specified using **UNIQUE**

- one of which is chosen as the primary key.

- “For a given student and course, there is a single grade.”

```
CREATE TABLE Enrolled
(sid CHAR(20)
 cid CHAR(20),
 grade CHAR(2),
 PRIMARY KEY (sid, cid) )
```

# Primary and Candidate Keys in SQL

- Possibly many **candidate keys**

- specified using **UNIQUE**
- one of which is chosen as the primary key.

- “For a given student and course, there is a single grade.”

- **vs.**

- “Students can take only one course, and receive a single grade for that course; further, no two students in a course receive the same grade.”

```
CREATE TABLE Enrolled
(sid CHAR(20)
 cid CHAR(20),
 grade CHAR(2),
 PRIMARY KEY (sid, cid) )
```

```
CREATE TABLE Enrolled
(sid CHAR(20)
 cid CHAR(20),
 grade CHAR(2),
 PRIMARY KEY ???,
 UNIQUE ??? )
```

# Primary and Candidate Keys in SQL

- Possibly many **candidate keys**

- specified using **UNIQUE**
- one of which is chosen as the primary key.

- “For a given student and course, there is a single grade.”

- **vs.**

- “Students can take only one course, and receive a single grade for that course; further, no two students in a course receive the same grade.”

```
CREATE TABLE Enrolled
(sid CHAR(20)
 cid CHAR(20),
 grade CHAR(2),
 PRIMARY KEY (sid,cid) )
```

```
CREATE TABLE Enrolled
(sid CHAR(20)
 cid CHAR(20),
 grade CHAR(2),
 PRIMARY KEY sid,
 UNIQUE (cid, grade))
```



# Primary and Candidate Keys in SQL

- Possibly many **candidate keys**

- specified using **UNIQUE**
- one of which is chosen as the primary key.

- “For a given student and course, there is a single grade.”

- **vs.**

- “Students can take only one course, and receive a single grade for that course; further, no two students in a course receive the same grade.”

- **Used carelessly, an IC can prevent the storage of database instances that arise in practice!**

```
CREATE TABLE Enrolled
(sid CHAR(20)
 cid CHAR(20),
 grade CHAR(2),
 PRIMARY KEY (sid,cid) )
```

```
CREATE TABLE Enrolled
(sid CHAR(20)
 cid CHAR(20),
 grade CHAR(2),
 PRIMARY KEY sid,
 UNIQUE (cid, grade))
```

# Foreign Keys, Referential Integrity

- **Foreign key** : Set of fields in one relation that is used to `refer` to a tuple in another relation
  - Must correspond to primary key of the second relation
  - Like a `logical pointer`
- E.g. **sid** is a foreign key referring to **Students**:
  - Enrolled(**sid**: string, cid: string, grade: string)
  - If all foreign key constraints are enforced, **referential integrity** is achieved
  - i.e., no dangling references

# Foreign Keys in SQL

- Only students listed in the Students relation should be allowed to enroll for courses

```
CREATE TABLE Enrolled
(sid CHAR(20), cid CHAR(20), grade CHAR(2),
PRIMARY KEY (sid,cid),
FOREIGN KEY (sid) REFERENCES Students )
```

Enrolled

sid	cid	grade
53666	Carnatic101	C
53666	Reggae203	B
53650	Topology112	A
53666	History105	B

Students

sid	name	login	age	gpa
53666	Jones	jones@cs	18	3.4
53688	Smith	smith@eecs	18	3.2
53650	Smith	smith@math	19	3.8

# Enforcing Referential Integrity

- Consider Students and Enrolled
  - sid in Enrolled is a foreign key that references Students.
- What should be done if an Enrolled tuple with a non-existent student id is inserted?
  - Reject it!
- What should be done if a Students tuple is **deleted**?
  - Three semantics allowed by SQL
    1. Also delete all Enrolled tuples that refer to it (cascade delete)
    2. Disallow deletion of a Students tuple that is referred to
    3. Set sid in Enrolled tuples that refer to it to a default sid
    4. (in addition in SQL): Set sid in Enrolled tuples that refer to it to a special value **null**, denoting `unknown` or `inapplicable`
- Similar if primary key of Students tuple is **updated**

# Referential Integrity in SQL

- SQL/92 and SQL:1999 support all 4 options on deletes and updates.
  - Default is **NO ACTION** (delete/update is rejected)
  - **CASCADE** (also delete all tuples that refer to deleted tuple)
  - **SET NULL / SET DEFAULT** (sets foreign key value of referencing tuple)

```
CREATE TABLE Enrolled
(sid CHAR(20) DEFAULT '000',
cid CHAR(20),
grade CHAR(2),
PRIMARY KEY (sid,cid),
FOREIGN KEY (sid)
REFERENCES Students
ON DELETE CASCADE
ON UPDATE SET DEFAULT )
```

# Where do ICs Come From?

- ICs are based upon the semantics of the real-world enterprise that is being described in the database relations
- Can we infer ICs from an instance?
  - We can check a database instance to see if an IC is violated, but we can **NEVER** infer that an IC is true by looking at an instance.
  - An IC is a statement about **all possible instances!**
  - From example, we know name is not a key, but the assertion that sid is a key is given to us.

# Example Instances

- What does the key (sid, bid, day) in Reserves mean?
- If the key for the Reserves relation contained only the attributes (sid, bid), how would the semantics differ?

Sailor

<u>sid</u>	sname	rating	age
22	dustin	7	45
31	lubber	8	55
58	rusty	10	35

Reserves

<u>sid</u>	<u>bid</u>	<u>day</u>
22	101	10/10/96
58	103	11/12/96

# Views

Students(sid, name)  
Enrolled(sid, cid, grade)

- A **view** is just a relation, but we store a **definition**, rather than a set of tuples

```
CREATE VIEW YoungActiveStudents (name, grade)
  AS SELECT S.name, E.grade
  FROM Students S, Enrolled E
  WHERE S.sid = E.sid and S.age<21
```

- Views can be dropped using the **DROP VIEW** command
- **Views and Security:** Views can be used to present necessary information (or a summary), while hiding details in underlying relation(s)
  - the above view hides courses “cid” from E



# Can create a new table from a query on other tables too

SELECT... INTO.... FROM.... WHERE

```
SELECT S.name, E.grade  
INTO YoungActiveStudents  
FROM Students S, Enrolled E  
WHERE S.sid = E.sid and S.age<21
```

# “WITH” clause – very useful!

- You will find “WITH” clause very useful!

```
WITH Temp1 AS  
    (SELECT ..... ..),  
    Temp2 AS  
    (SELECT ..... ..)  
SELECT X, Y  
FROM TEMP1, TEMP2  
WHERE....
```

- Can simplify complex nested queries

# Overview: General Constraints

- Useful when more general ICs than keys are involved
- There are also **ASSERTIONS** to specify constraints that span across multiple tables
- There are **TRIGGERS** too : procedure that starts automatically if specified changes occur to the DBMS

```
CREATE TABLE Sailors
  ( sid INTEGER,
    sname CHAR(10),
    rating INTEGER,
    age REAL,
    PRIMARY KEY (sid),
    CHECK ( rating >= 1
           AND rating <= 10 )
```

```
CREATE TABLE Reserves
  ( sname CHAR(10),
    bid INTEGER,
    day DATE,
    PRIMARY KEY (bid,day),
    CONSTRAINT noInterlakeRes
    CHECK ( `Interlake' <>
           ( SELECT B.bname
             FROM Boats B
             WHERE B.bid=bid)))
```

# Summary: SQL

- SQL has a huge number of constructs and possibilities
  - You need to learn and practice it on your own
- Can limit answers using “LIMIT” or “TOP” clauses
  - e.g. to output TOP 20 results according to an aggregate
  - also can sort using ASC or DESC keywords
- We learnt
  - Creating/modifying relations
  - Specifying integrity constraints
  - Key/candidate key, superkey, primary key, foreign key
  - Conceptual evaluation of SQL queries
  - Joins
  - Group bys and aggregates
  - Nested queries
  - NULLs
  - Views

# Relational Query Languages

# Relational Query Languages

- **Query languages:** Allow manipulation and retrieval of data from a database
- Relational model supports simple, powerful QLs:
  - Strong formal foundation based on logic
  - Allows for much optimization
- Query Languages **!=** programming languages
  - QLs not intended to be used for complex calculations
  - QLs support easy, efficient access to large data sets

# Formal Relational Query Languages

- Two “mathematical” Query Languages form the basis for “real” languages (e.g. SQL), and for implementation:
  - **Relational Calculus**: Lets users describe what they want, rather than how to compute it (**Non-operational, declarative, or procedural**)
  - **Relational Algebra**: More **operational**, very useful for representing execution plans
- **Note: Declarative (RC, SQL) vs. Operational (RA)**

# Relational Calculus (RC)

Please see updated Lecture notes  
in Lecture 7



# Relational Algebra (RA)

# Relational Algebra

- Takes one or more relations as input, and produces a relation as output
  - operator
  - operand
  - semantic
  - so an algebra!
- Since each operation returns a relation, **operations can be composed**
  - Algebra is “closed”

# Relational Algebra

- Basic operations:
  - Selection ( $\sigma$ ) Selects a subset of rows from relation
  - Projection ( $\pi$ ) Deletes unwanted columns from relation.
  - Cross-product ( $\times$ ) Allows us to combine two relations.
  - Set-difference ( $-$ ) Tuples in reln. 1, but not in reln. 2.
  - Union ( $\cup$ ) Tuples in reln. 1 or in reln. 2.
- Additional operations:
  - Intersection ( $\cap$ )
  - join  $\bowtie$
  - division ( $\div$ )
  - renaming ( $\rho$ )
  - Not essential, but (very) useful.

# Example Schema and Instances

Sailors(sid, sname, rating, age)

Boats(bid, bname, color)

Reserves(sid, bid, day)

*S1*

<u>sid</u>	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

*S2*

<u>sid</u>	sname	rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

*R1*

<u>sid</u>	<u>bid</u>	<u>day</u>
22	101	10/10/96
58	103	11/12/96

# Projection

S2

<u>sid</u>	sname	rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

- Deletes attributes that are not in projection list.
- Schema** of result contains exactly the fields in the projection list, with the same names that they had in the (only) input relation.
- Projection operator has to **eliminate duplicates** (Why)
  - Note: real systems typically don't do duplicate elimination unless the user explicitly asks for it (performance)

sname	rating
yuppy	9
lubber	8
guppy	5
rusty	10

$\pi_{sname, rating}(S2)$

age
35.0
55.5

$\pi_{age}(S2)$

# Selection

- Selects rows that satisfy **selection condition**

- No duplicates in result.  
Why?

- Schema of result identical to schema of (only) input relation

S2

<u>sid</u>	sname	rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

sid	sname	rating	age
28	yuppy	9	35.0
58	rusty	10	35.0

$$\sigma_{rating > 8}(S2)$$

# Composition of Operators

- Result relation can be the input for another relational algebra operation
  - Operator composition

sid	sname	rating	age
28	yuppy	9	35.0
58	rusty	10	35.0

$$\sigma_{rating > 8}(S2)$$

sname	rating
yuppy	9
rusty	10

$$\pi_{sname, rating}(\sigma_{rating > 8}(S2))$$

# Union, Intersection, Set-Difference

S1

<u>sid</u>	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

S2

<u>sid</u>	sname	rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

- All of these operations take two input relations, which must be **union-compatible**:
  - Same number of fields.
  - ‘Corresponding’ fields have the same type
  - same schema as the inputs

<u>sid</u>	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0
44	guppy	5	35.0
28	yuppy	9	35.0



# Union, Intersection, Set-Difference

S1

<u>sid</u>	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

S2

<u>sid</u>	sname	rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

- Note: no duplicate
  - “Set semantic”
  - SQL: **UNION**
  - SQL allows “bag semantic” as well:  
**UNION ALL**

sid	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0
44	guppy	5	35.0
28	yuppy	9	35.0

# Union, Intersection, Set-Difference

$S_1$

<u>sid</u>	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

$S_2$

<u>sid</u>	sname	rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

sid	sname	rating	age
22	dustin	7	45.0

$S_1 - S_2$

sid	sname	rating	age
31	lubber	8	55.5
58	rusty	10	35.0

$S_1 \cap S_2$

# Cross-Product

- Each row of S1 is paired with each row of R.
- **Result schema** has one field per field of S1 and R, with field names 'inherited' if possible.
  - Conflict: Both S1 and R have a field called sid.

<u>sid</u>	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

<u>sid</u>	<u>bid</u>	<u>day</u>
22	101	10/10/96
58	103	11/12/96

(sid)	sname	rating	age	(sid)	bid	day
22	dustin	7	45.0	22	101	10/10/96
22	dustin	7	45.0	58	103	11/12/96
31	lubber	8	55.5	22	101	10/10/96
31	lubber	8	55.5	58	103	11/12/96
58	rusty	10	35.0	22	101	10/10/96
58	rusty	10	35.0	58	103	11/12/96

# Renaming Operator $\rho$

$$(\rho_{\text{sid} \rightarrow \text{sid1}} S1) \times (\rho_{\text{sid} \rightarrow \text{sid1}} R1)$$

or

$$\rho(C(1 \rightarrow \text{sid1}, 5 \rightarrow \text{sid2}), S1 \times R1)$$

C is the  
new relation  
name

(sid)	sname	rating	age	(sid)	bid	day
22	dustin	7	45.0	22	101	10/10/96
22	dustin	7	45.0	58	103	11/12/96
31	lubber	8	55.5	22	101	10/10/96
31	lubber	8	55.5	58	103	11/12/96
58	rusty	10	35.0	22	101	10/10/96
58	rusty	10	35.0	58	103	11/12/96

- In general, can use  $\rho(\langle \text{Temp} \rangle, \langle \text{RA-expression} \rangle)$

# Joins

$$R \bowtie_c S = \sigma_c (R \times S)$$

(sid)	sname	rating	age	(sid)	bid	day
22	dustin	7	45.0	58	103	11/12/96
31	lubber	8	55.5	58	103	11/12/96

$$S1 \bowtie_{S1.sid < R1.sid} R1$$

- Result schema same as that of cross-product.
- Fewer tuples than cross-product, might be able to compute more efficiently

# Find names of sailors who've reserved boat #103

Sailors(sid, sname, rating, age)

Boats(bid, bname, color)

Reserves(sid, bid, day)

# Find names of sailors who've reserved boat #103

Sailors(sid, sname, rating, age)

Boats(bid, bname, color)

Reserves(sid, bid, day)

- **Solution 1:**  $\pi_{sname}((\sigma_{bid=103} Reserves) \bowtie Sailors)$
- **Solution 2:**  $\pi_{sname}(\sigma_{bid=103}(Reserves \bowtie Sailors))$

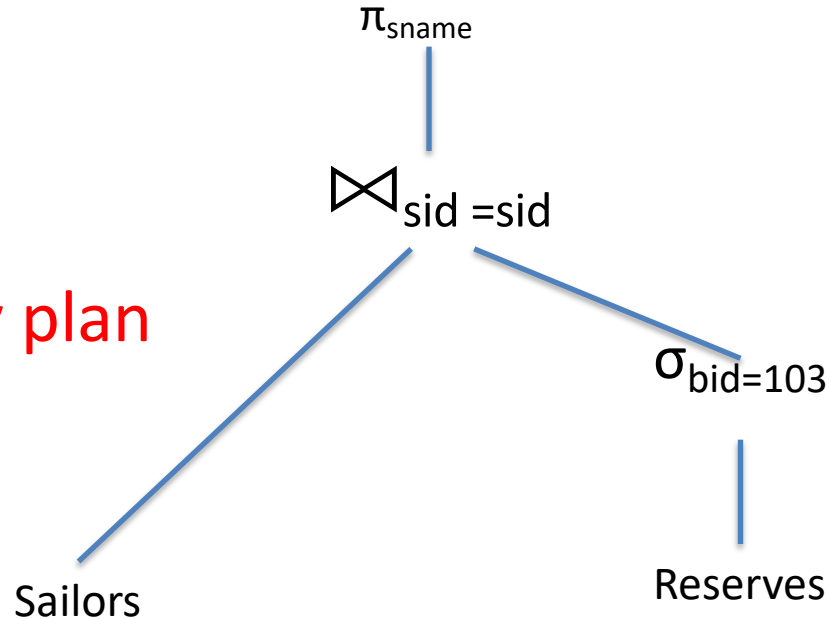
# Expressing an RA expression as a Tree

Sailors(sid, sname, rating, age)

Boats(bid, bname, color)

Reserves(sid, bid, day)

Also called a  
**logical query plan**



$\pi_{sname}((\sigma_{bid=103} \text{Reserves}) \bowtie \text{Sailors})$



# Find sailors who've reserved a red or a green boat

Sailors(sid, sname, rating, age)

Boats(bid, bname, color)

Reserves(sid, bid, day)

Use of rename operation

- Can identify all red or green boats, then find sailors who've reserved one of these boats:

$$\rho (Tempboats, (\sigma_{color='red' \vee color='green'} Boats))$$
$$\pi_{sname}(Tempboats \bowtie Reserves \bowtie Sailors)$$

Can also define Tempboats using union  
Try the “AND” version yourself

# What about aggregates?

Sailors(sid, sname, rating, age)

Boats(bid, bname, color)

Reserves(sid, bid, day)

- Extended relational algebra
- $\gamma_{age, avg(rating)} \rightarrow avgr$  Sailors
- Also extended to “bag semantic”: allow duplicates
  - Take into account cardinality
  - R and S have tuple t resp. m and n times
  - $R \cup S$  has t m+n times
  - $R \cap S$  has t  $\min(m, n)$  times
  - $R - S$  has t  $\max(0, m-n)$  times
  - sorting( $\tau$ ), duplicate removal ( $\delta$ ) operators